

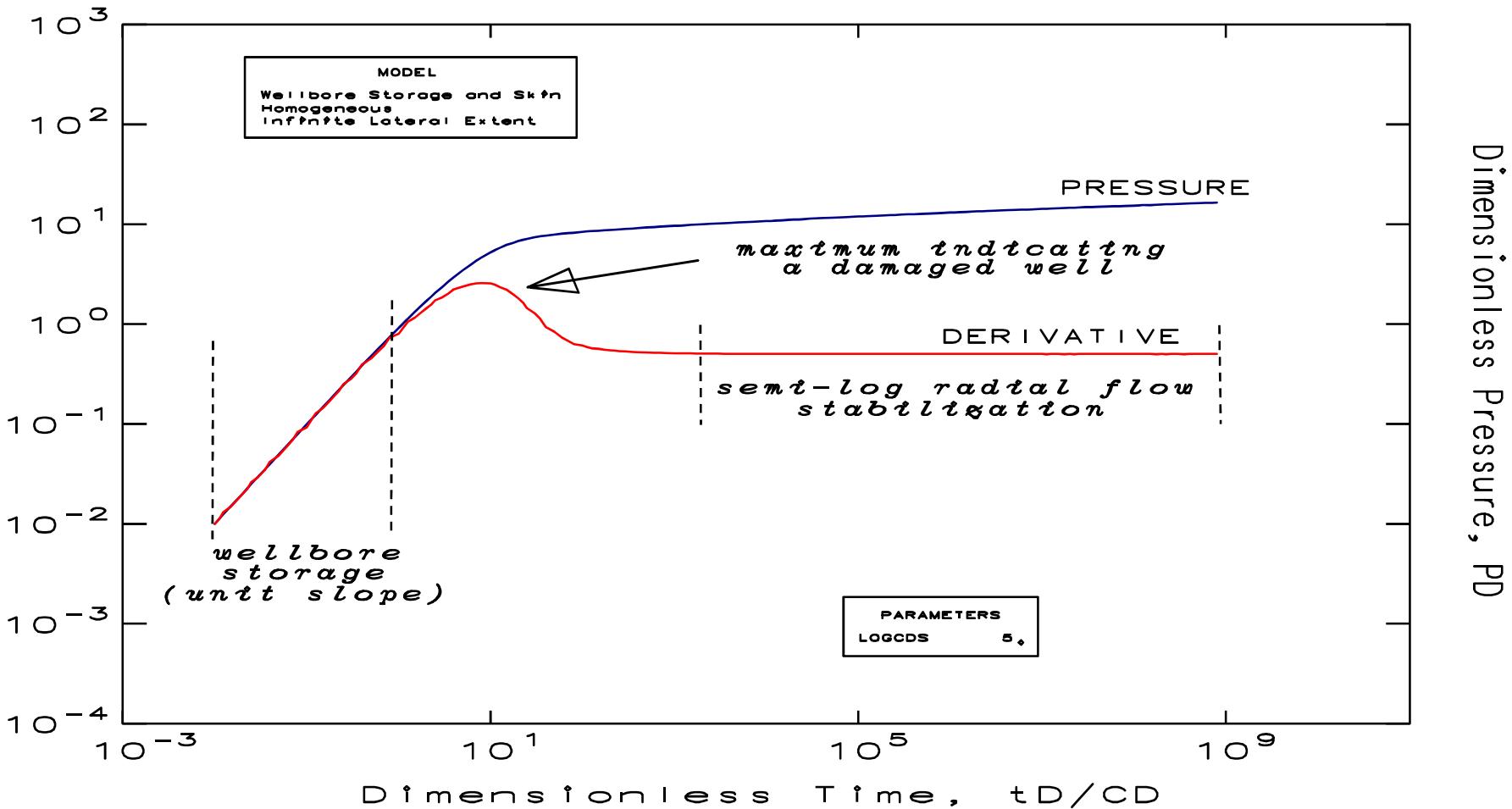
# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
Wellbore Storage	Homogeneous	Infinite extent
Skin	Heterogeneous	Specified Rate
Fractures	-2-Porosity	Specified Pressure
Partial Penetration	-2-Permeability	Leaky Boundary
Horizontal Well	-Composite	
EARLY TIMES	MIDDLE TIMES	LATE TIMES

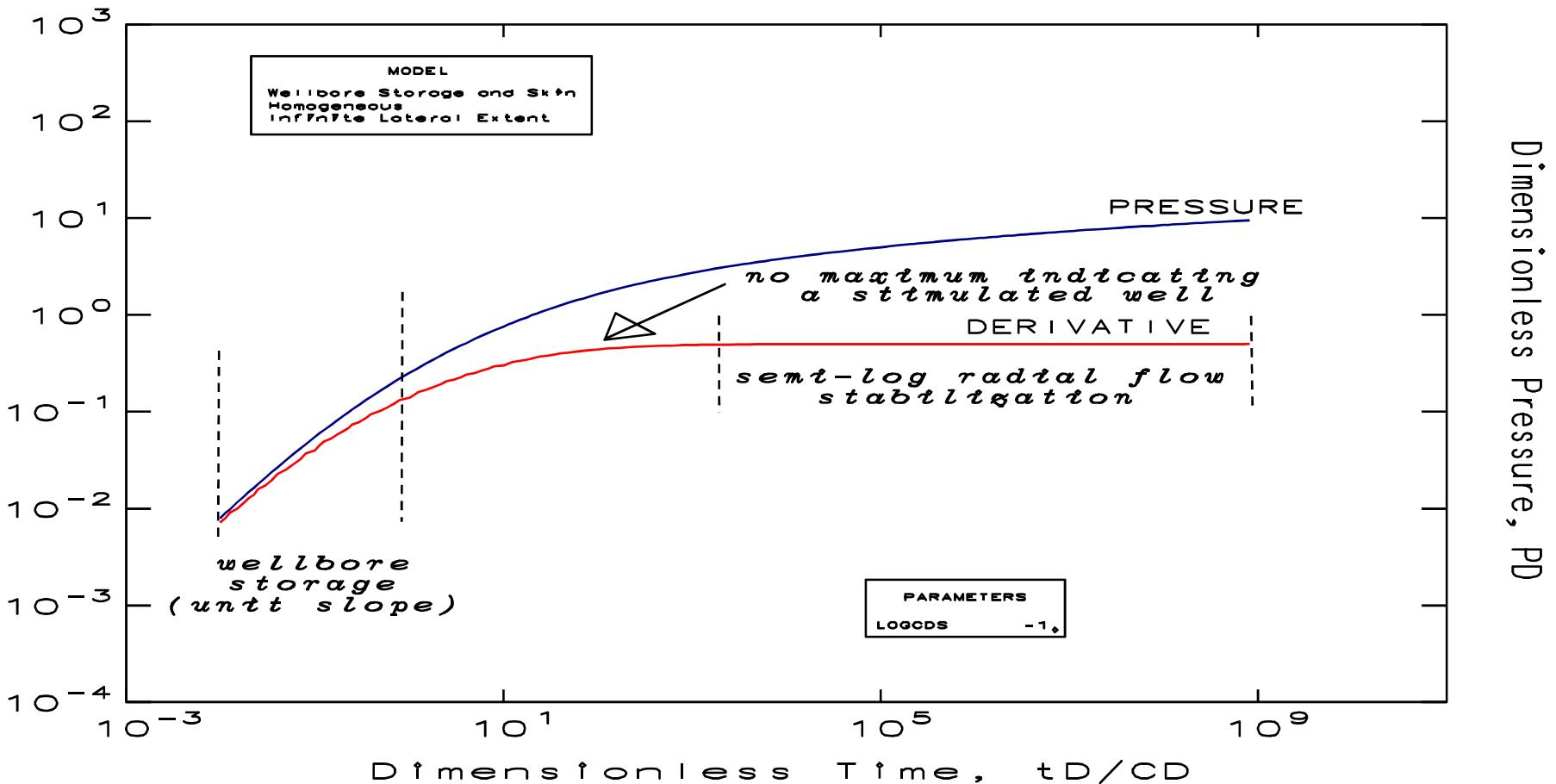
# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
<b>Wellbore Storage</b> <b>Skin</b> <b>Fracture</b>	<b>Homogeneous</b>  Heterogeneous -2-Porosity -2-Permeability -Composite	<b>Infinite extent</b>  Specified Rate Specified Pressure Leaky Boundary
Partial Penetration  Horizontal Well		
EARLY TIMES	MIDDLE TIMES	LATE TIMES

# Wellbore Storage and Skin, Homogeneous Behaviour, Infinite Acting



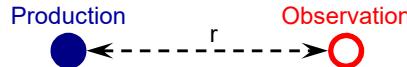
# Wellbore Storage and Skin, Homogeneous Behaviour, Infinite Acting



# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
Wellbore Storage	Homogeneous	Infinite extent
Skin	Heterogeneous	Specified Rate
Fracture	-2-Porosity	Specified Pressure
Partial Penetration	-2-Permeability	Leaky Boundary
Horizontal Well	-Composite	
EARLY TIMES	MIDDLE TIMES	LATE TIMES

# INTERFERENCE TEST IN AN INFINITE RESERVOIR WITH HOMOGENEOUS BEHAVIOUR:

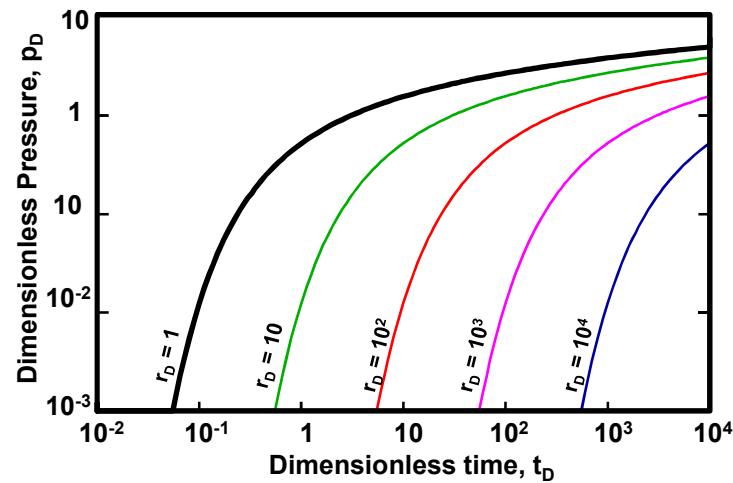


**Dimensionless parameters, non-unique match**

$$p_D = \frac{kh}{141.2\Delta q B \mu} \Delta p$$

$$t_D = \frac{0.000264 k}{\phi \mu c_t r_w^2} \Delta t$$

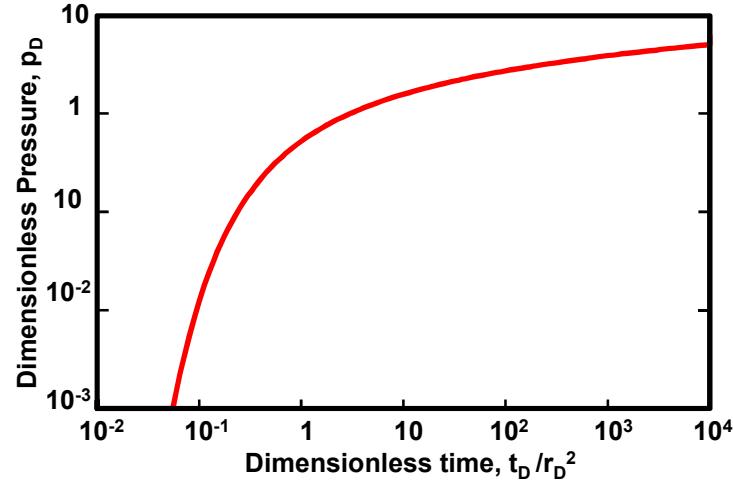
$$r_D = \frac{r}{r_w}$$



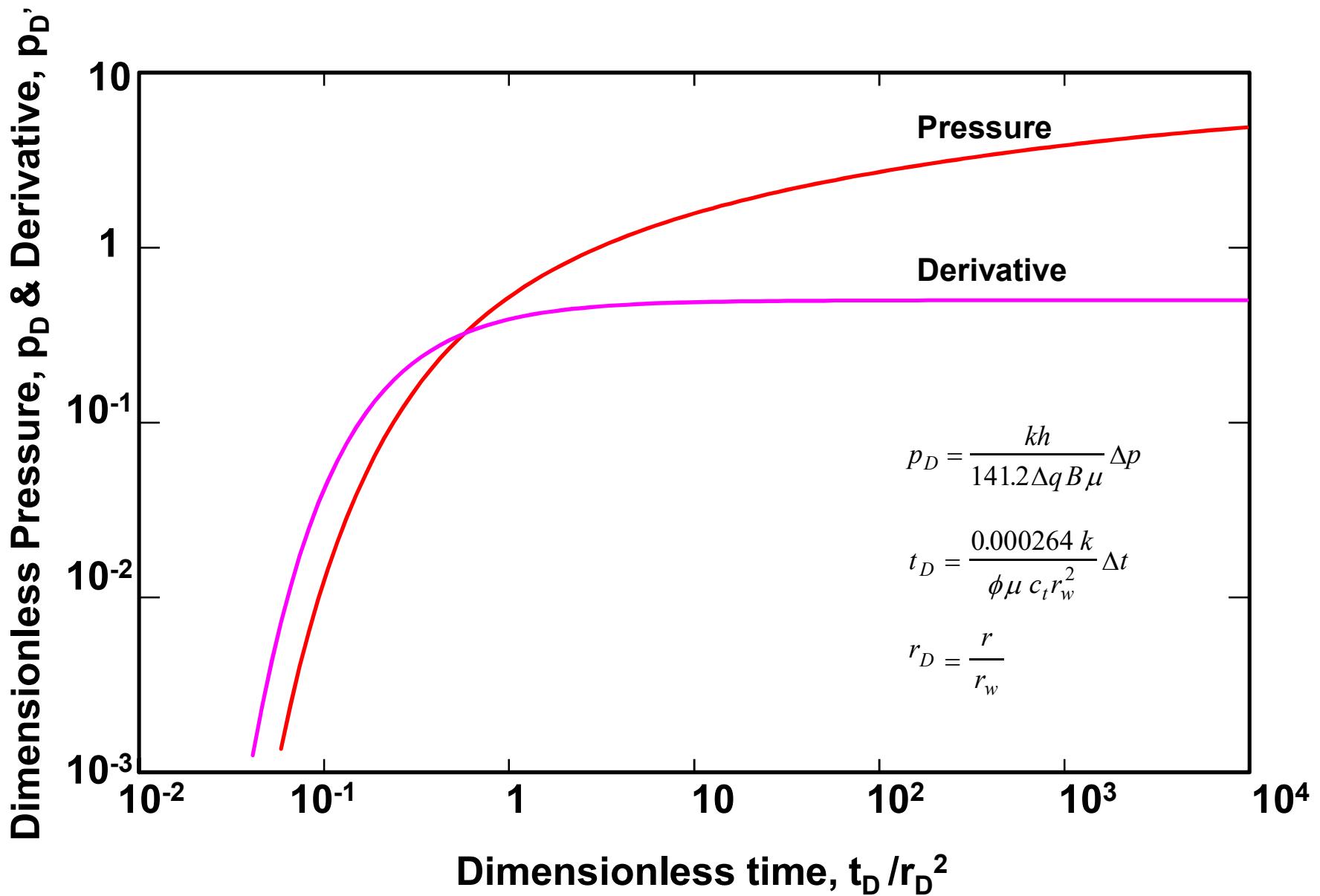
**Independent variables, unique match**

$$p_D = \frac{kh}{141.2\Delta q B \mu} \Delta p$$

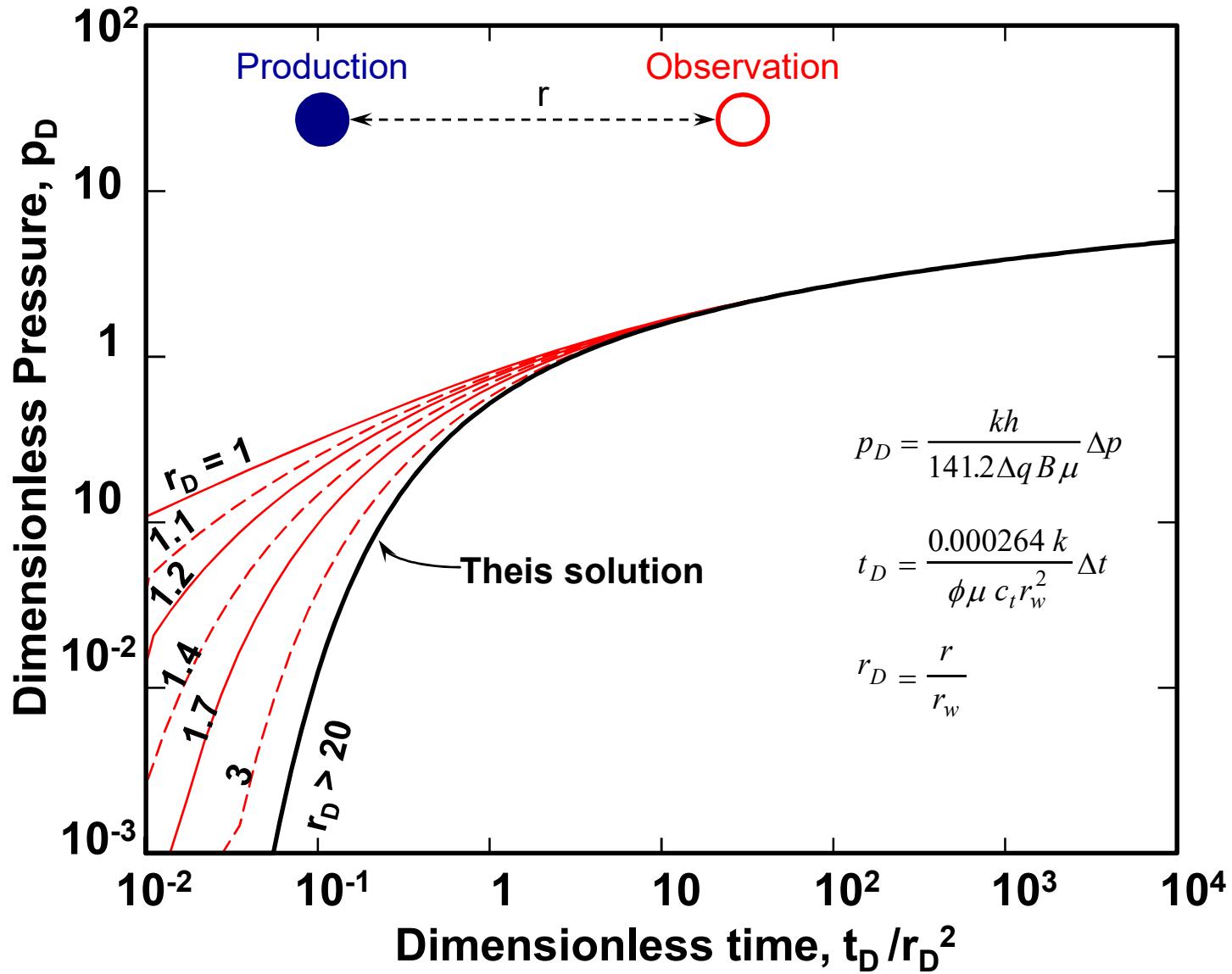
$$\frac{t_D}{r_D^2} = \frac{0.000264 k}{\phi \mu c_t r^2} \Delta t$$



# Drawdown Type Curve for a Line Source well



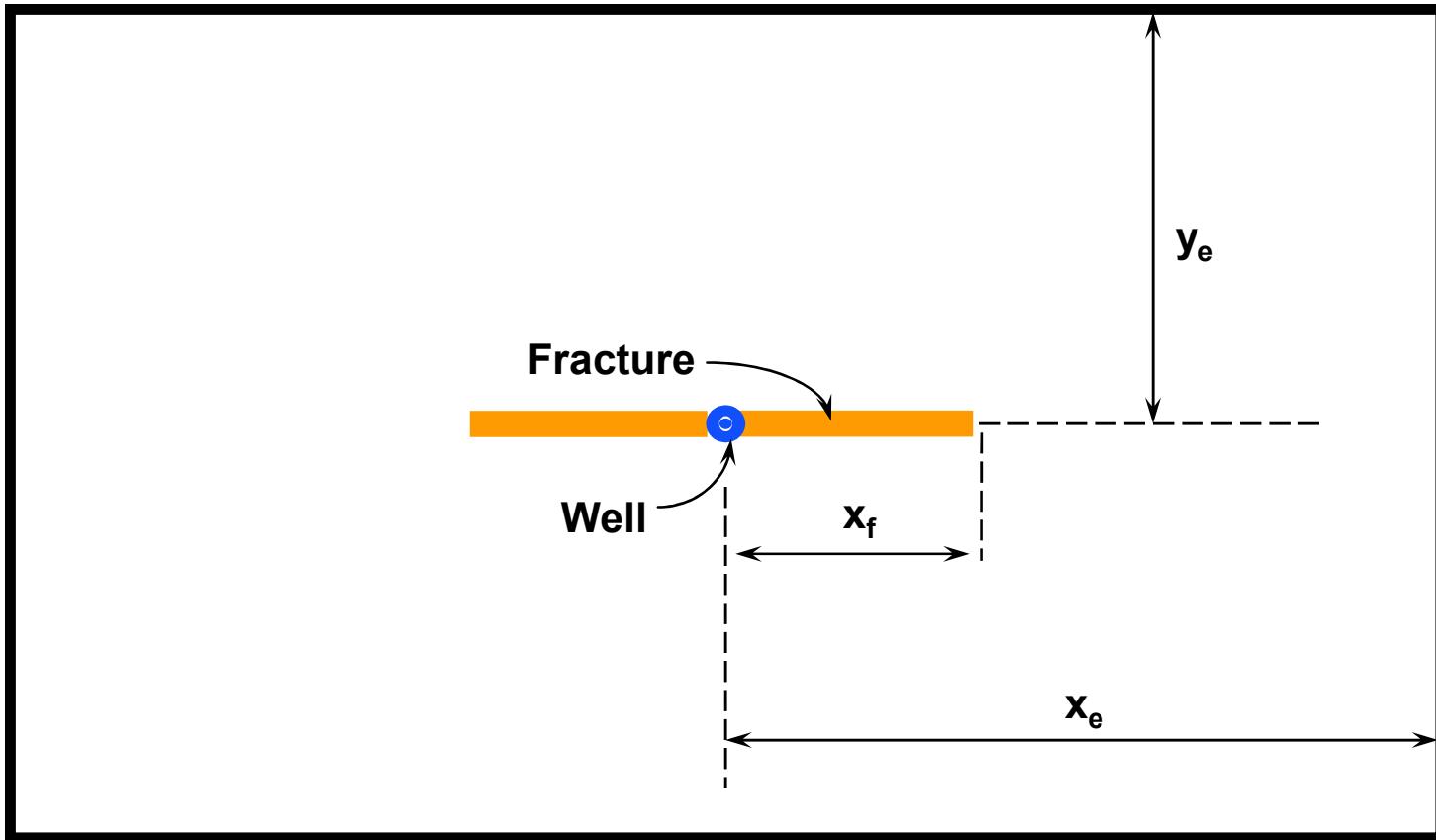
# Drawdown Type Curve for a Line Source well



# WELL TEST INTERPRETATION MODELS

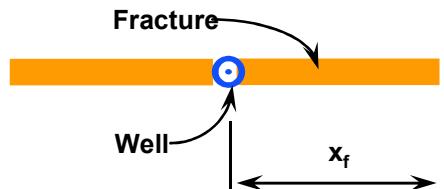
NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
Wellbore Storage	Homogeneous	Infinite extent
Skin	Heterogeneous	Specified Rate
Fracture	-2-Porosity -2-Permeability -Composite	Specified Pressure Leaky Boundary
Partial Penetration		
Horizontal Well		
EARLY TIMES	MIDDLE TIMES	LATE TIMES

# SCHEMATIC OF A VERTICALLY FRACTURED WELL AT THE CENTRE OF A RECTANGULAR RESERVOIR

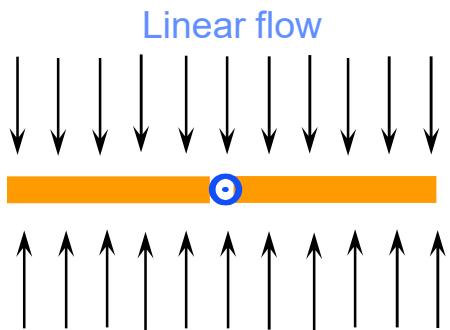


# INFINITE CONDUCTIVITY VERTICAL FRACTURE

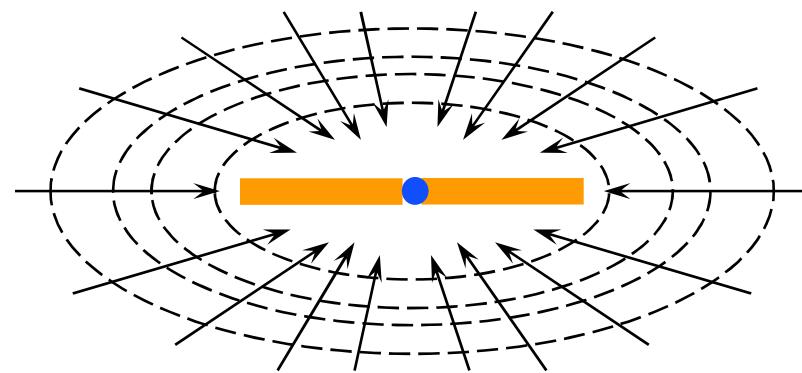
## Flow Regimes



**Linear Flow**

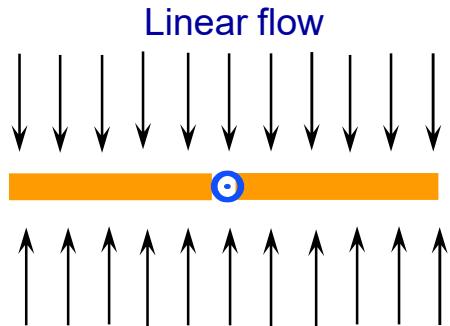


**Pseudo-Radial Flow**



# DERIVATIVE FOR HIGH CONDUCTIVITY FRACTURE (Early Times)

## High conductivity fracture



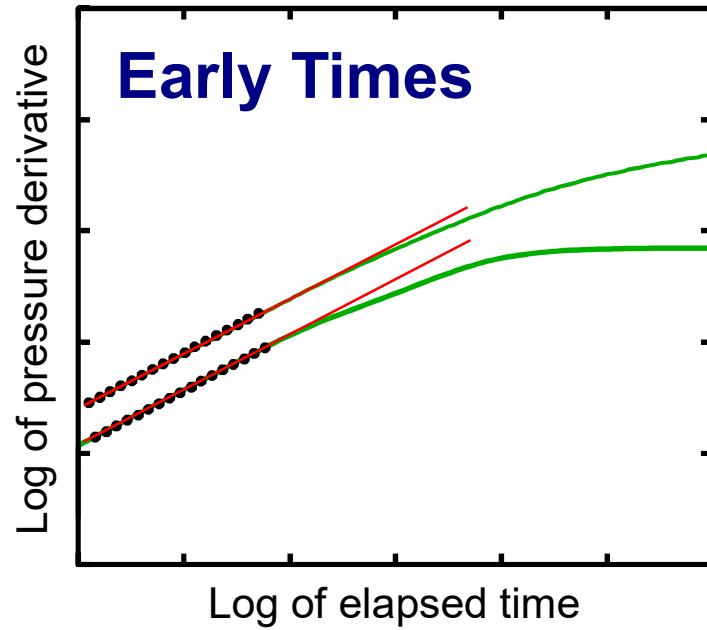
$$p_D = (\pi t_{Df})^{1/2}$$

$$p_D = \frac{kh}{141.2\Delta q B \mu} \Delta p$$

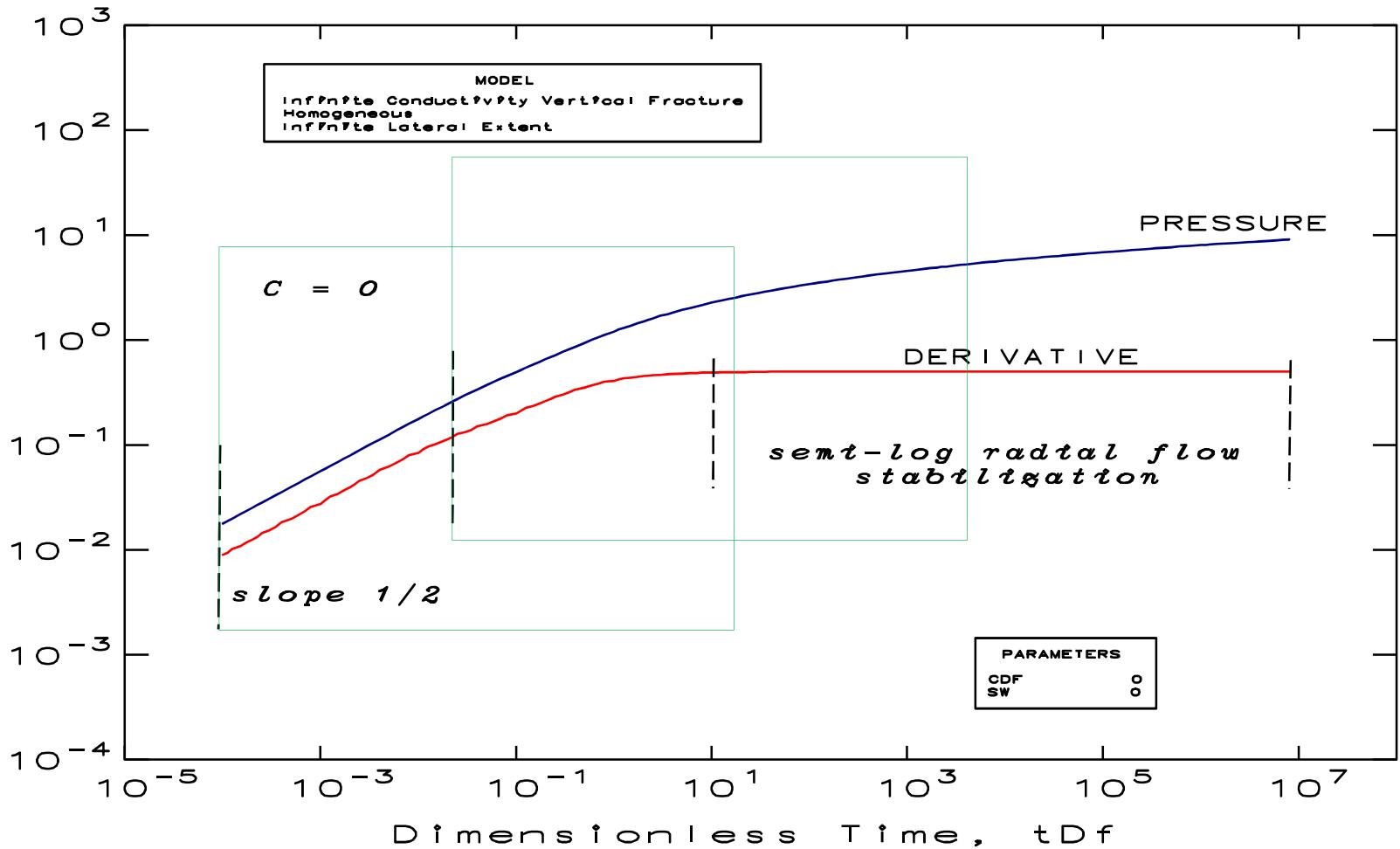
$$t_{Df} = \frac{0.000264 k}{\phi \mu c_t x_f^2} \Delta t$$

$$\frac{dp_D}{d \ln(t_{Df})} = 0.5 (\pi t_{Df})^{1/2} = (0.5) p_D$$

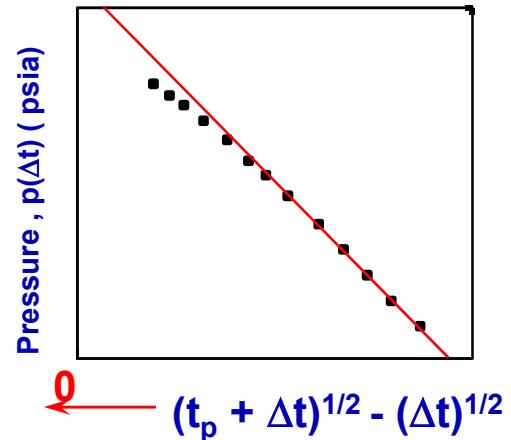
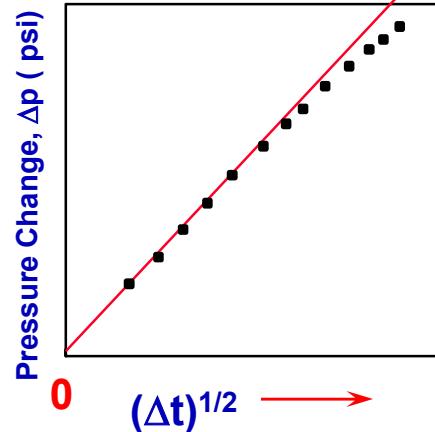
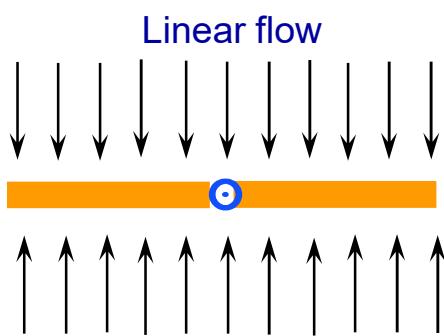
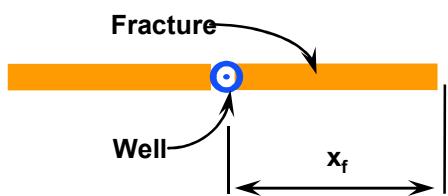
- Half-unit slope log-log straight line
- Derivative is one half the pressure



Dimensionless Pressure, PD



# STRAIGHT LINE METHODS FOR A HIGH CONDUCTIVITY FRACTURE (Early Times)



$$\Delta p = 4.06 \frac{\Delta q B}{hx_f} \sqrt{\frac{\mu}{\phi c_t k}} \sqrt{\Delta t}$$

$$p(\Delta t) = \bar{p}_i - 4.06 \frac{\Delta q B}{hx_f} \sqrt{\frac{\mu}{\phi c_t k}} \left[ (t_p + \Delta t)^{1/2} - (\Delta t)^{1/2} \right]$$

$$m_{HKF} = 4.06 \frac{\Delta q B}{hx_f} \sqrt{\frac{\mu}{\phi c_t k}}$$
 $\text{psi}/(\text{hr})^{1/2}$ 
 $k \cdot x_f^2 = 16.52 \frac{\mu}{\phi c_t} \left( \frac{\Delta q B}{h m_{HKF}} \right)^2 \text{ mD.sqft}$

# **FRACTURED WELL**

## **DIRECT METHOD**

### **INFINITE CONDUCTIVITY FRACTURE**

- Wellbore Storage and Skin type curves
- Infinite Conductivity Fracture

### **FINITE CONDUCTIVITY FRACTURE**

# DIRECT METHOD FOR HIGH CONDUCTIVITY VERTICAL FRACTURE

**PM**

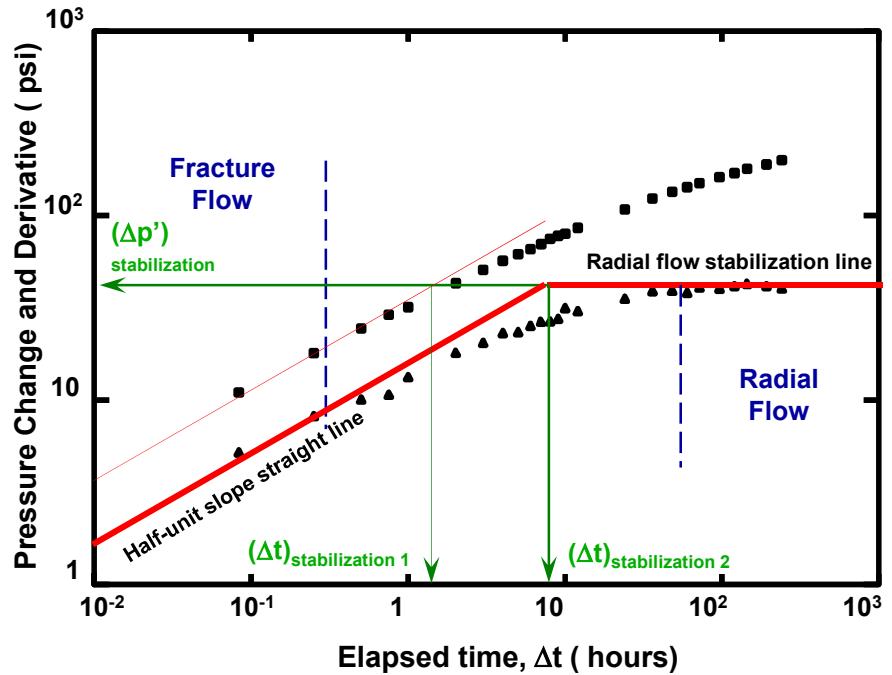
$$p_D = \frac{kh}{141.2 \Delta q B \mu} \Delta p$$

**TM**

$$t_{Df} = \frac{0.000264 k}{\phi \mu c_t x_f^2} \Delta t$$

**Fracture Flow :**  $p_D = \sqrt{\pi t_{Df}}$

$$\frac{dp_D}{d \ln(t_{Df})} = t_{Df} \frac{dp_D}{dt_{Df}} = t_{Df} \frac{1}{2} \sqrt{\frac{\pi}{t_{Df}}} = \frac{1}{2} \sqrt{\pi t_{Df}} = (0.5) p_D$$



$$PM = (p_D / \Delta p)_{match} = (p'_D)_{stabilization} / (\Delta p')_{stabilization} = \frac{kh}{141.2 \Delta q B \mu}$$

$$TM = \left( \frac{t_{Df}}{\Delta t} \right)_{match} = (t_{Df})_{stabilization} / (\Delta t)_{stabilization} = \frac{0.000264 k}{\phi \mu c_t x_f^2}$$

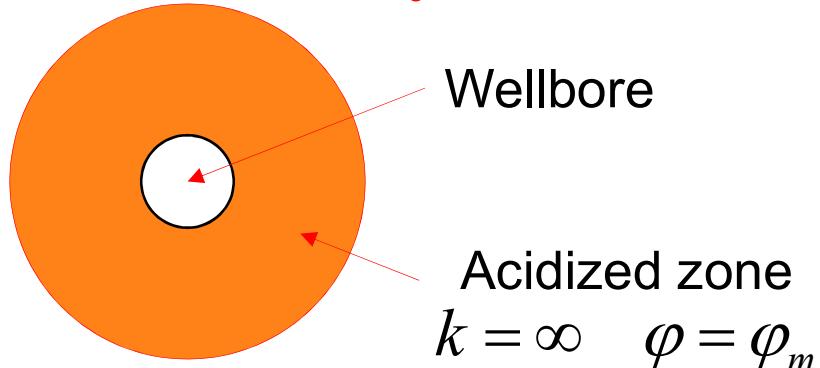
$$(p'_D)_{stabilization 1} = 0.5 = \sqrt{\pi (t_{Df})_{stabilization 1}} \rightarrow (t_{Df})_{stabilization 1} = \frac{0.25}{\pi} \quad TM = 0.25 / \pi (\Delta t)_{stabilization 1} \Rightarrow x_f$$

$$(p'_D)_{stabilization 2} = 0.5 = 0.5 \sqrt{\pi (t_{Df})_{stabilization 2}} \rightarrow (t_{Df})_{stabilization 2} = \frac{1}{\pi} \quad TM = 1 / \pi (\Delta t)_{stabilization 2} \Rightarrow x_f$$

# Well with Wellbore Storage & Skin, in a Reservoir of Infinite Extent with Homogeneous Behaviour

Minimum value of  $C_D e^{2S}$  for an acidized well

Gringarten, Bourdet, Landel and Kniazeff SPE8205 54<sup>th</sup> ATCE Las Vegas 1979



$$C_{w+S} = C_w + \pi (r_{we}^2 - r_w^2) h \varphi c_t$$

$$C_{w+S} = C_w + \pi r_w^2 (e^{-2S} - 1) h \varphi c_t$$

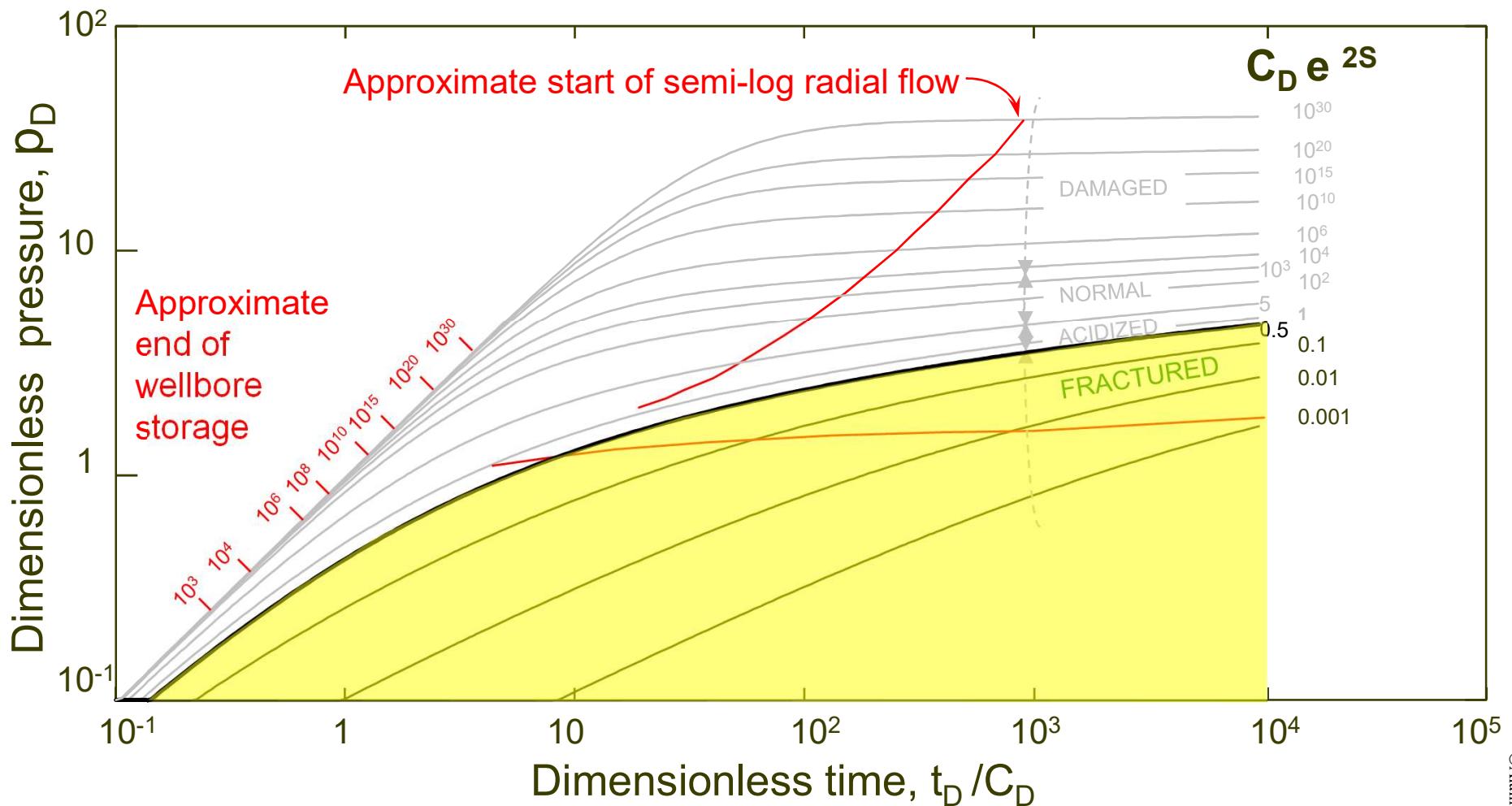
$$(Ce^{2S})_{w+S} = (Ce^{2S})_w + \pi r_w^2 (1 - e^{-2S}) h \varphi c_t$$

$$(C_D e^{2S})_{w+S} = (C_D e^{2S})_w + \frac{\pi r_w^2 (1 - e^{-2S}) h \varphi c_t}{2 \pi h \varphi c_t r_w^2} = (C_D e^{2S})_w + \frac{1 - e^{-2S}}{2}$$

Minimum value of  $(C_D e^{2S})_{w+S} = 0.5$

Lower values of  $(C_D e^{2S})_{w+S}$  must correspond to fractured wells with wellbore storage

## Drawdown Type Curve for a Well with Wellbore Storage & Skin, in a Reservoir of Infinite Extent with Homogeneous Behaviour



$$C_D e^{2S} < 0.5$$

**Yields**

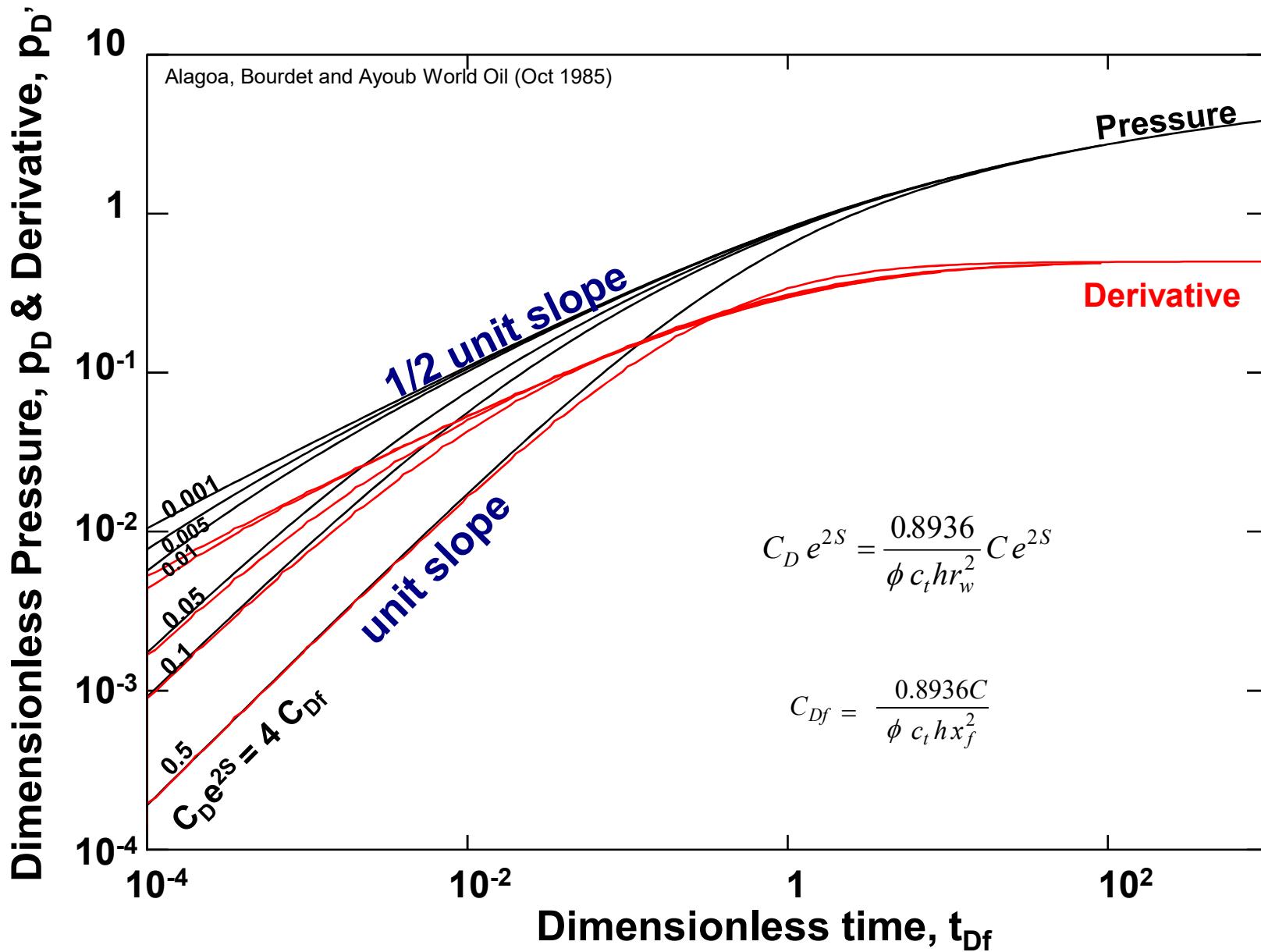
**$kh, C, S$**

$$r_{we} = r_w e^{-s} = x_f / 2$$

**Yields**

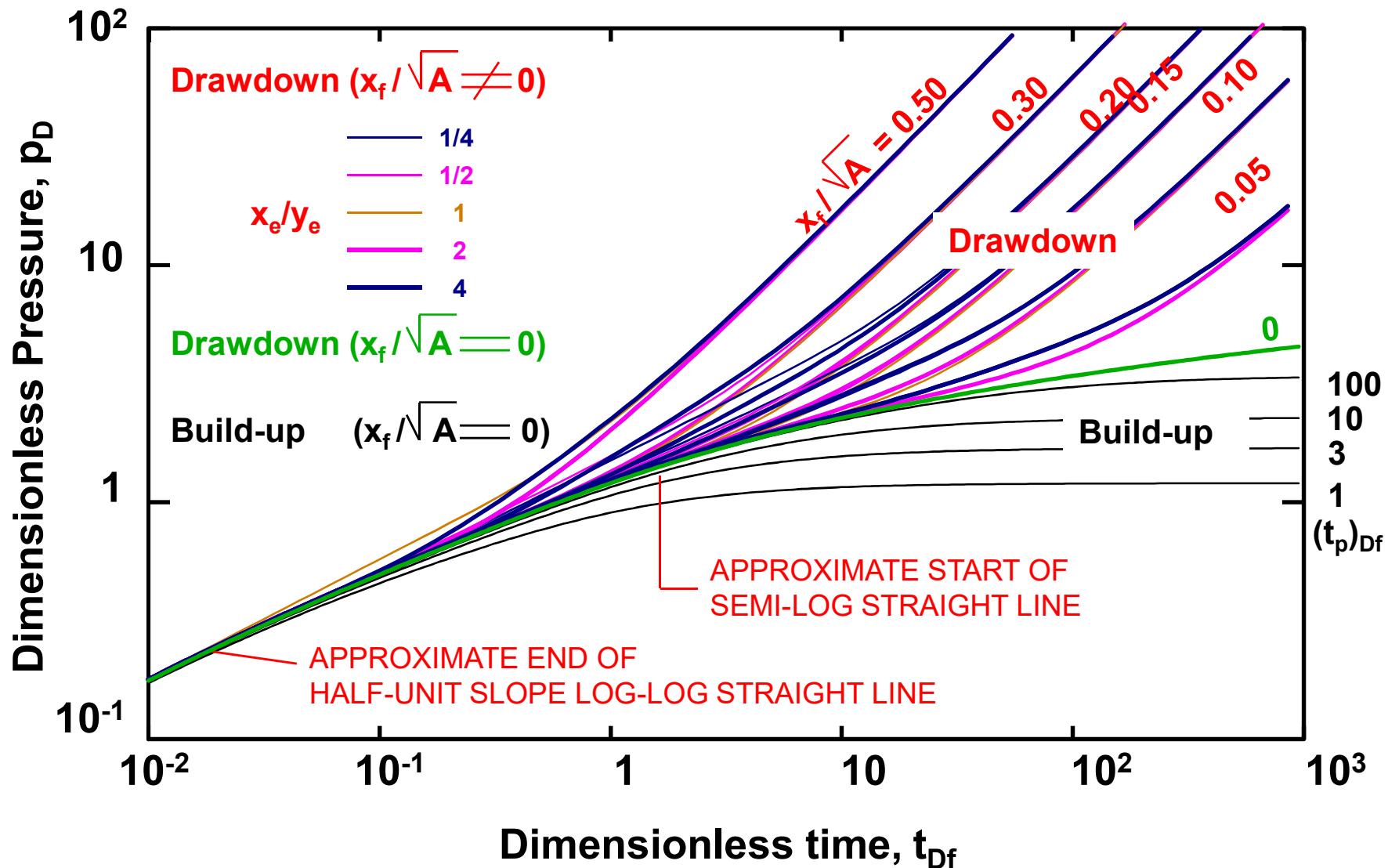
$$x_f = 2r_w e^{-s}$$

## Fractured Well with Wellbore Storage & Skin

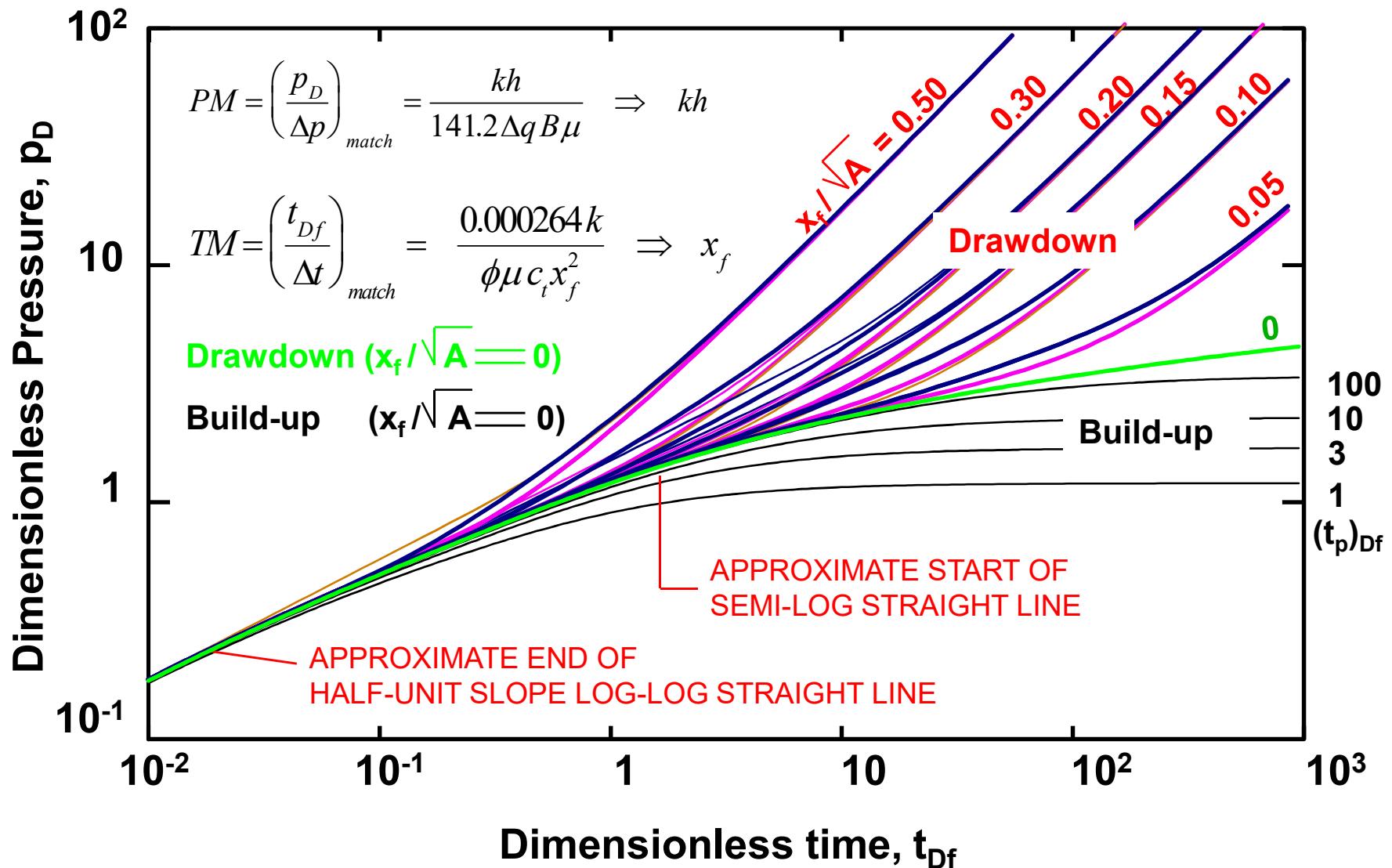


# INFINITE CONDUCTIVITY VERTICAL FRACTURE AT THE CENTRE OF A CLOSED RECTANGLE

Gringarten SPE 7452 1978

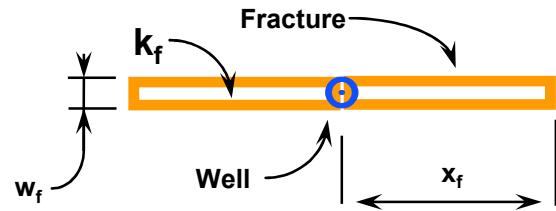


# INFINITE CONDUCTIVITY VERTICAL FRACTURE AT THE CENTRE OF A CLOSED RECTANGLE

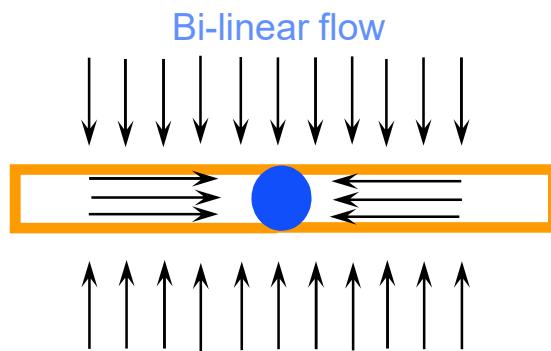


# FINITE CONDUCTIVITY VERTICAL FRACTURE

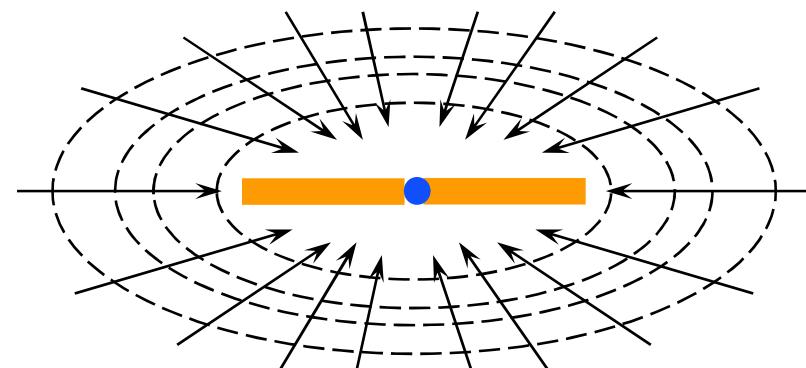
## Flow Regimes



**Bi-Linear &  
Linear Flow**

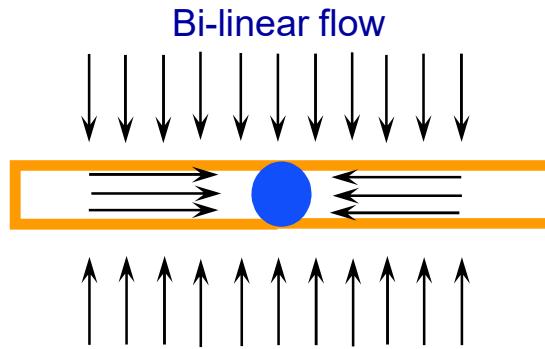


**Pseudo-Radial Flow**



# DERIVATIVE FOR LOW CONDUCTIVITY FRACTURE (Early Times)

## Low conductivity fracture



$$\frac{dp_D}{d \ln(t_{Df})} = (0.25) 2.45 \left( k_{fD} w_D \right)^{-1/2} \left( t_{Df} \right)^{1/4} = (0.25) p_D$$

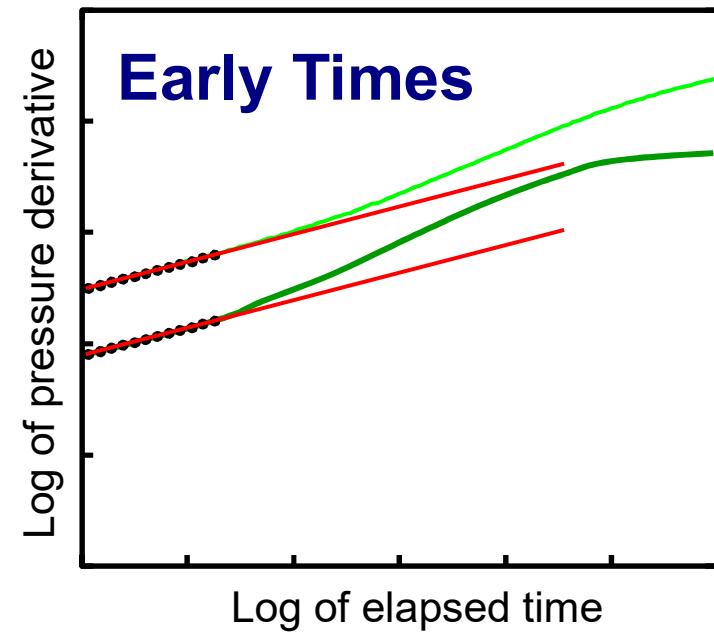
- Quarter-unit slope log-log straight line
- Derivative is one fourth the pressure

$$p_D = 2.45 \left( k_{fD} w_D \right)^{-1/2} \left( t_{Df} \right)^{1/4}$$

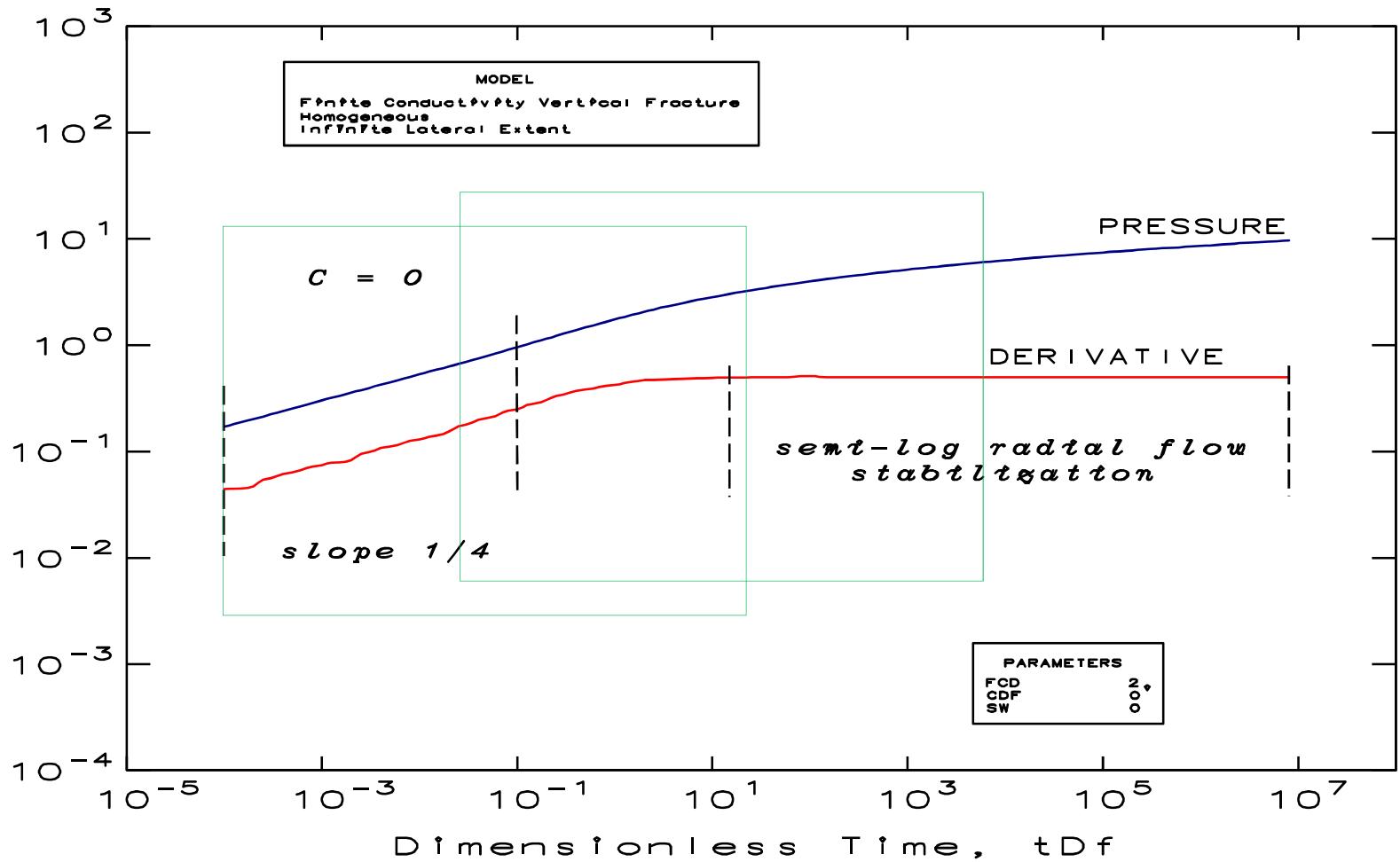
$$p_D = \frac{kh}{141.2 \Delta q B \mu} \Delta p$$

$$t_{Df} = \frac{0.000264 k}{\phi \mu c_t x_f^2} \Delta t$$

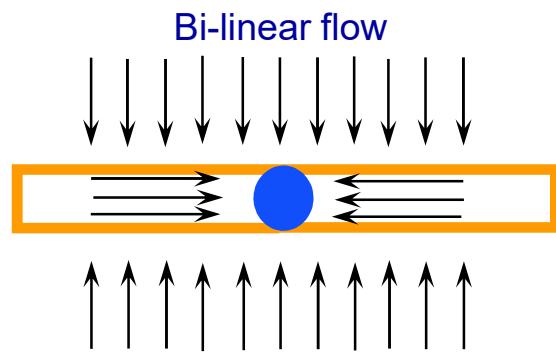
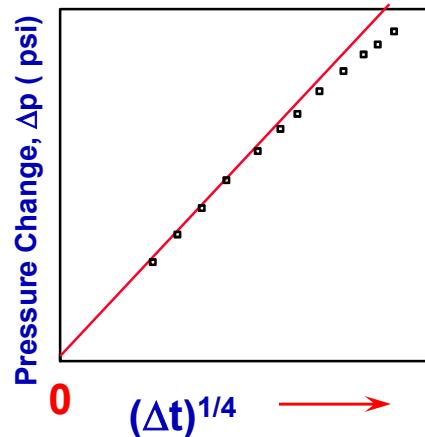
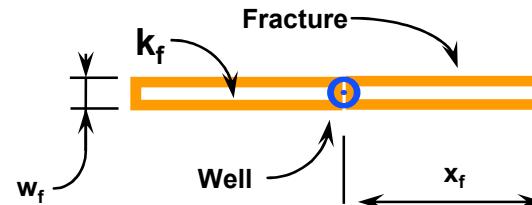
$$k_{fD} w_D = \frac{k_f w_f}{k x_f}$$



Dimensionless Pressure,  $P_D$

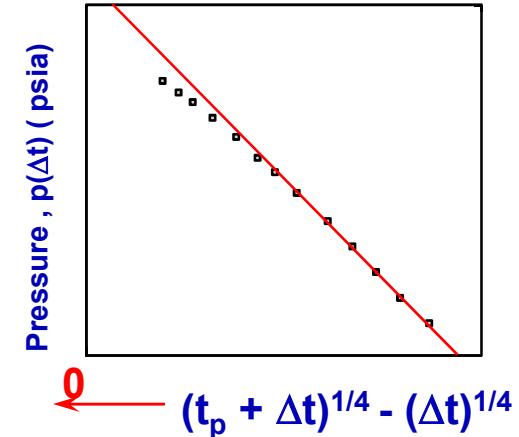


# STRAIGHT LINE METHOD FOR A LOW CONDUCTIVITY FRACTURE (Early Times)



Specialised Plot

$$\Delta p = 44.1 \frac{\Delta q B \mu}{h \sqrt{k_f w_f} \sqrt[4]{\phi \mu c_t k}} \sqrt[4]{\Delta t}$$



Horner Plot

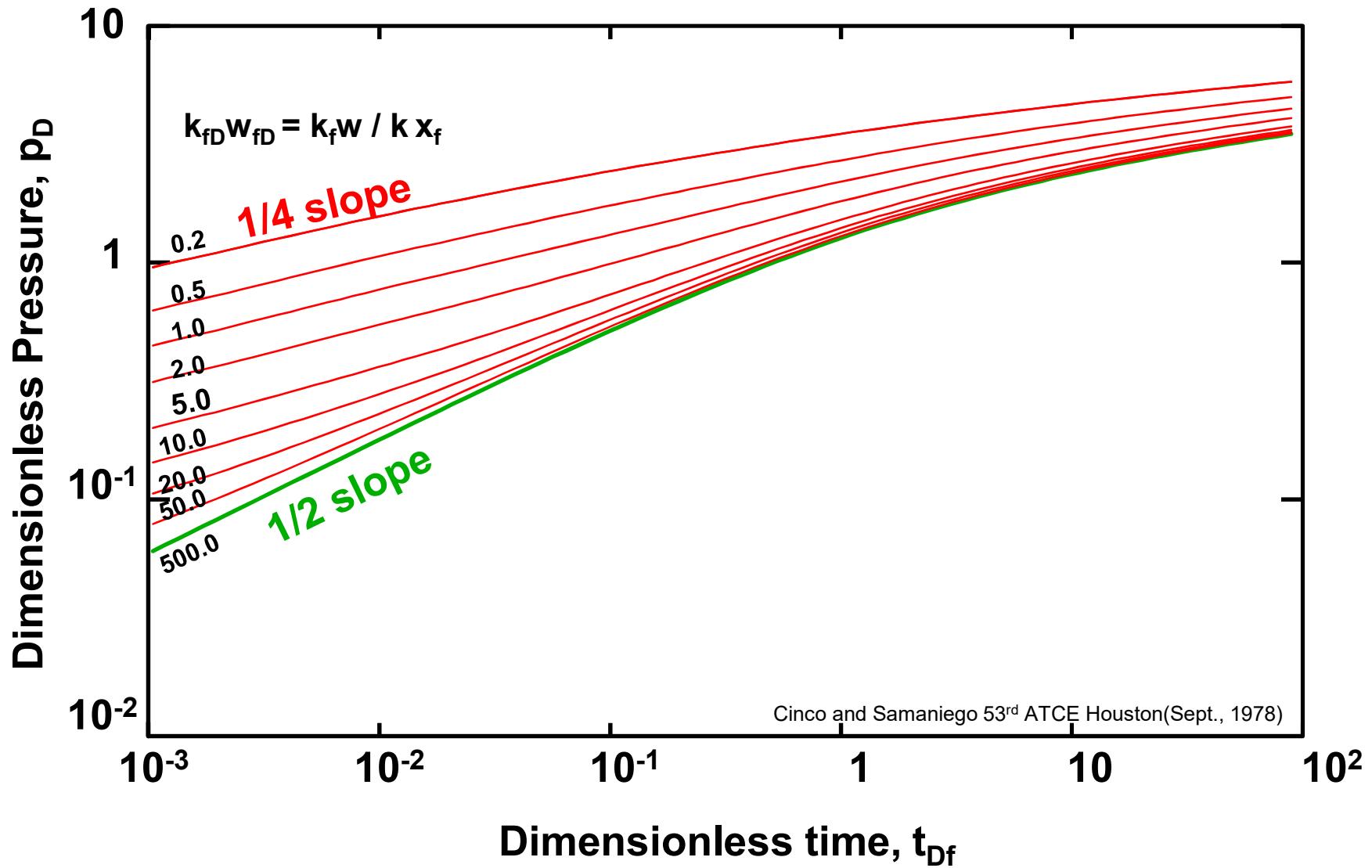
$$p(\Delta t) = \bar{p}_i - 44.1 \frac{\Delta q B \mu}{h \sqrt{k_f w_f} \sqrt[4]{\phi \mu c_t k}} \left[ (t_p + \Delta t)^{1/4} - (\Delta t)^{1/4} \right]$$

$$m_{LKF} = 44.1 \frac{\Delta q B \mu}{h \sqrt{k_f w_f} \sqrt[4]{\phi \mu c_t k}}$$

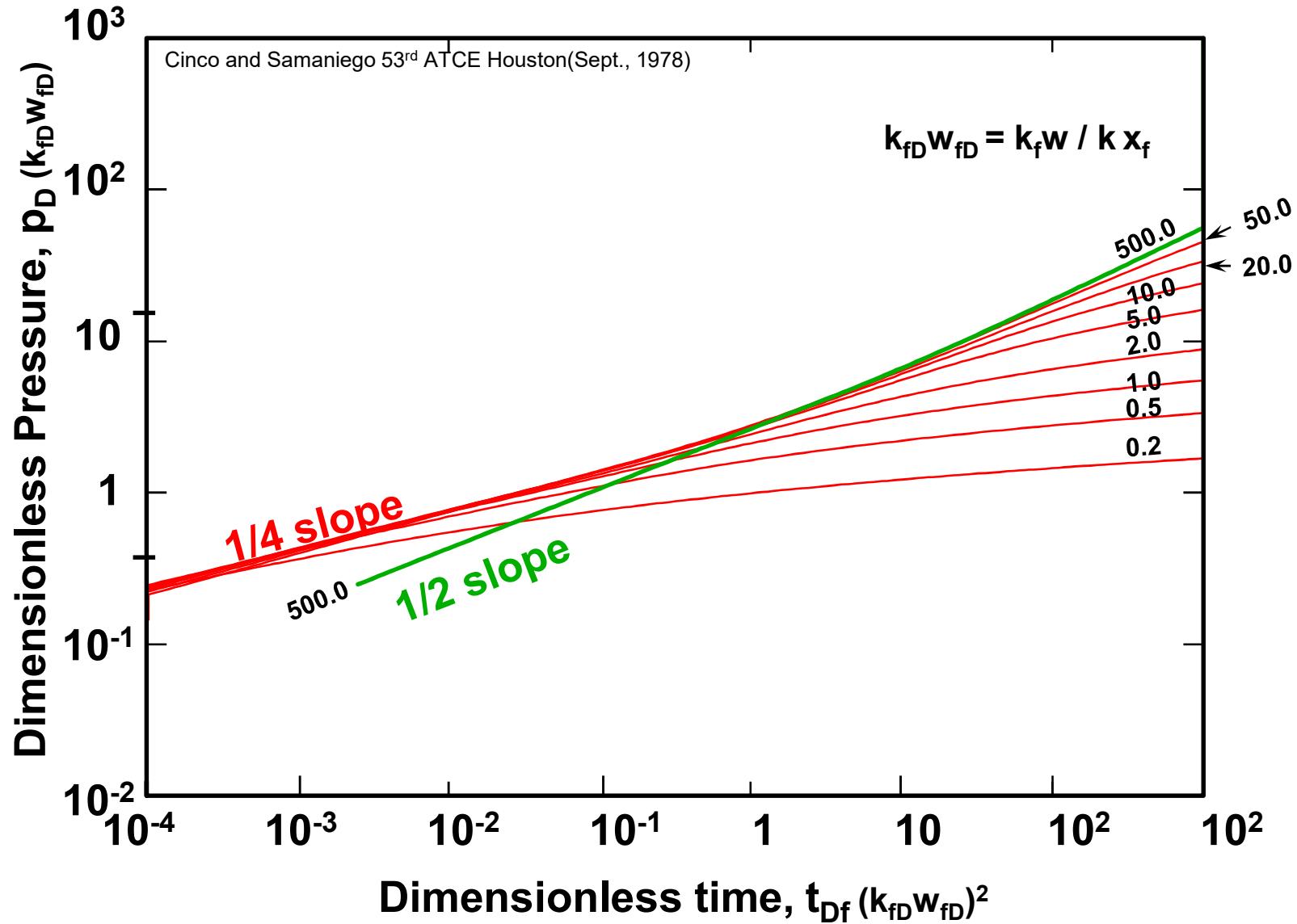
psi/(hr)<sup>1/4</sup>

$$k_f w_f = 1944.8 \left( \frac{\Delta q B \mu}{h m_{LKF}} \right)^2 \frac{1}{\sqrt{\phi \mu c_t k}} \text{ mD.ft}$$

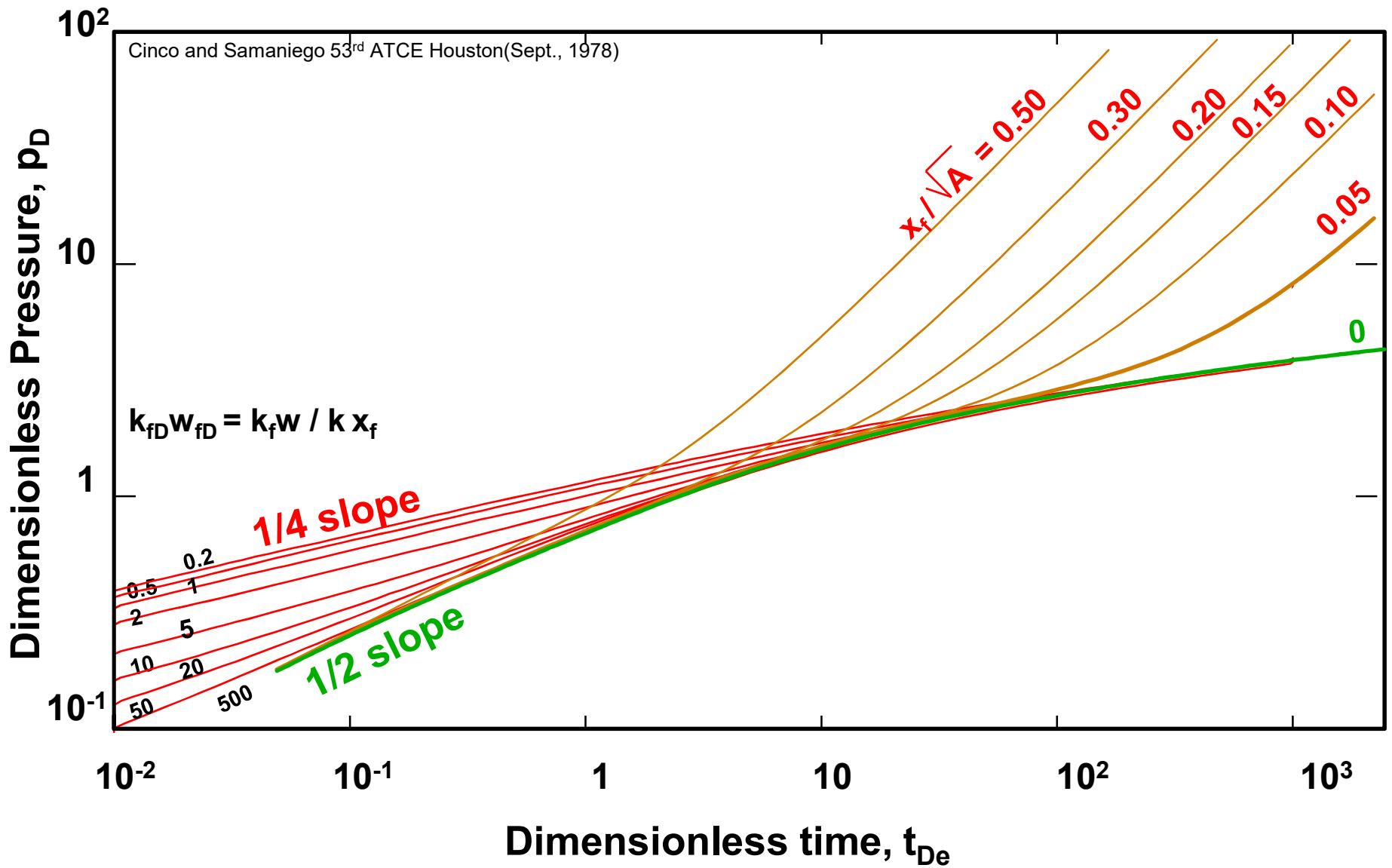
# FINITE CONDUCTIVITY VERTICAL FRACTURE



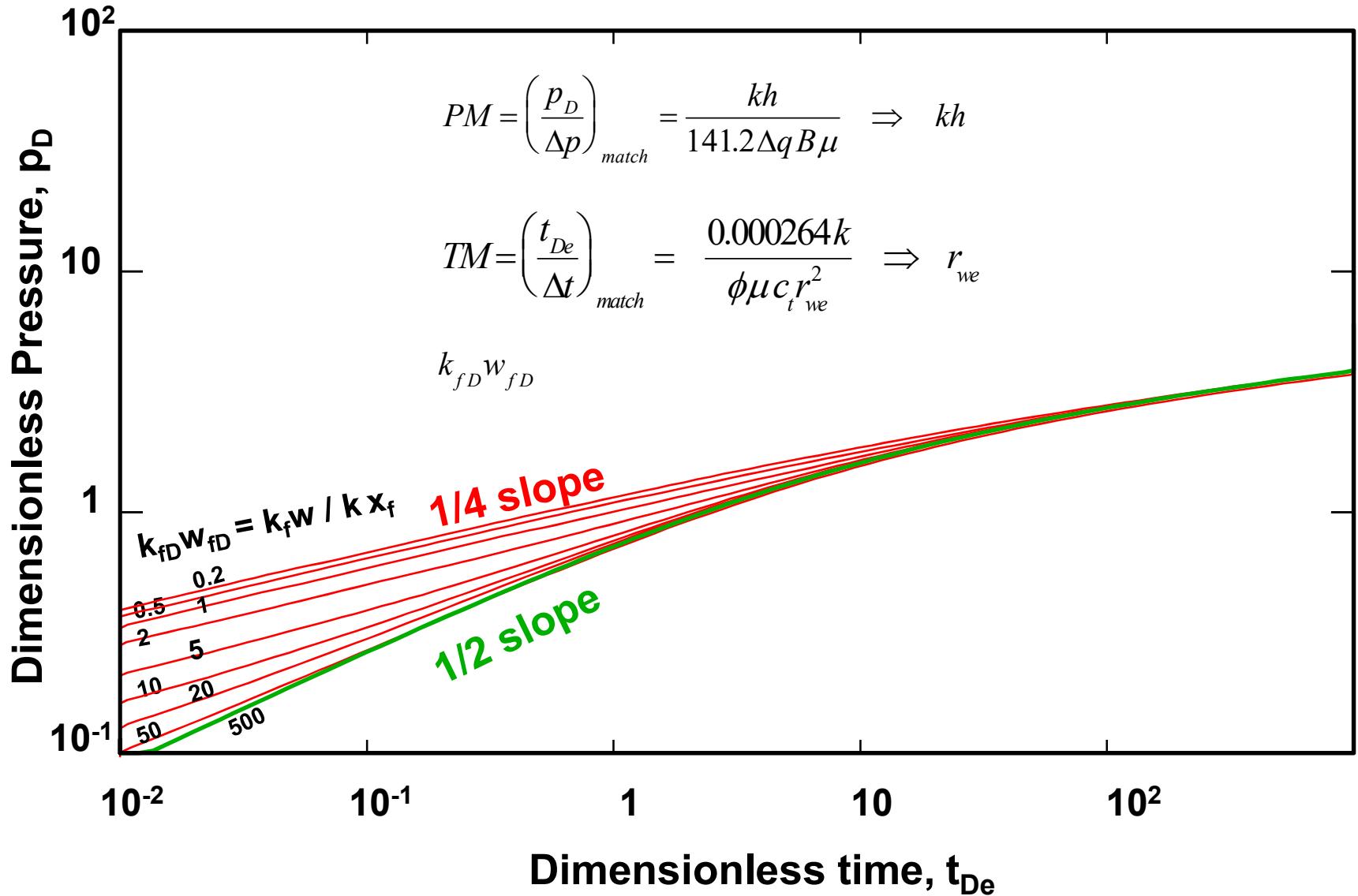
# FINITE CONDUCTIVITY VERTICAL FRACTURE

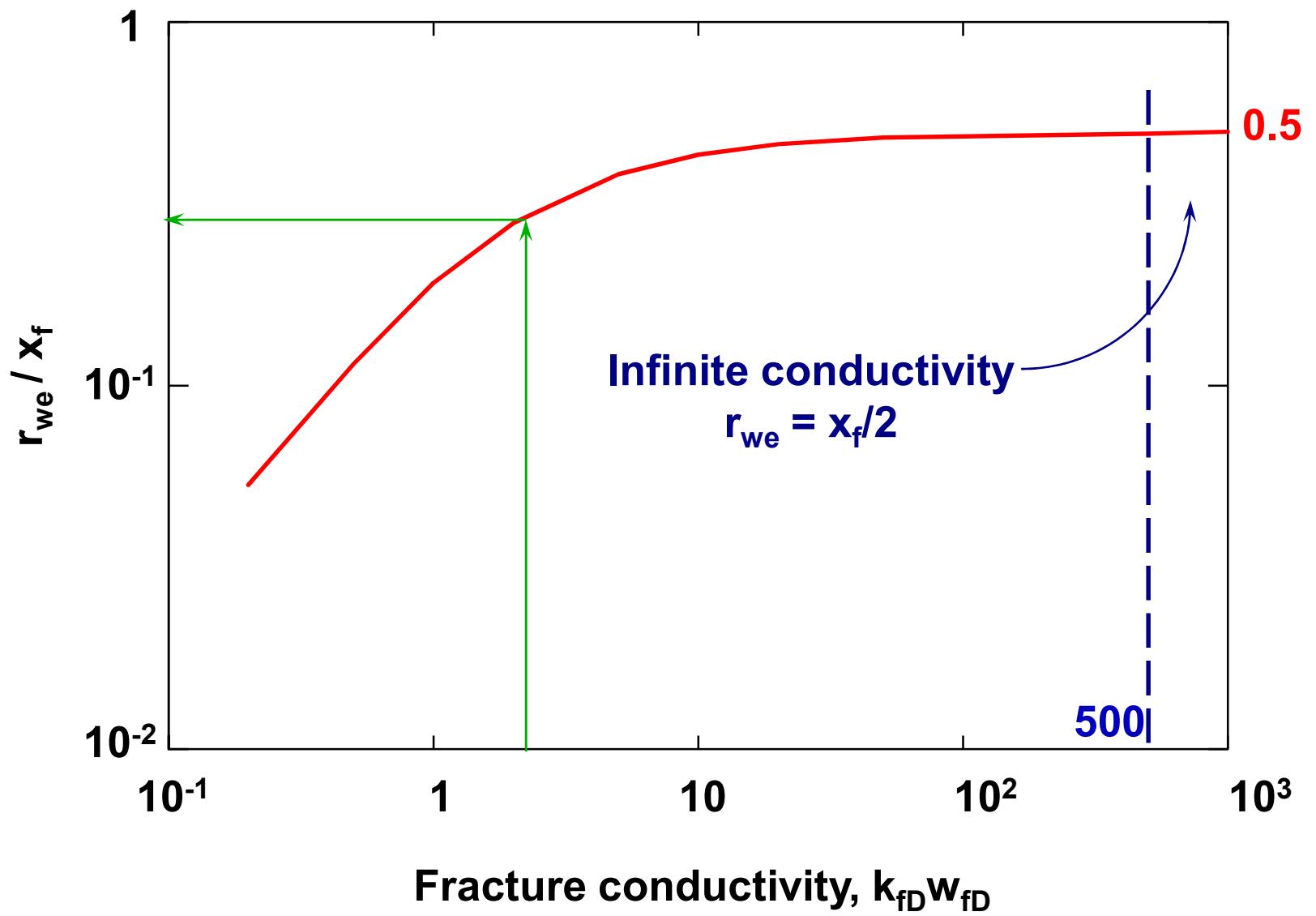


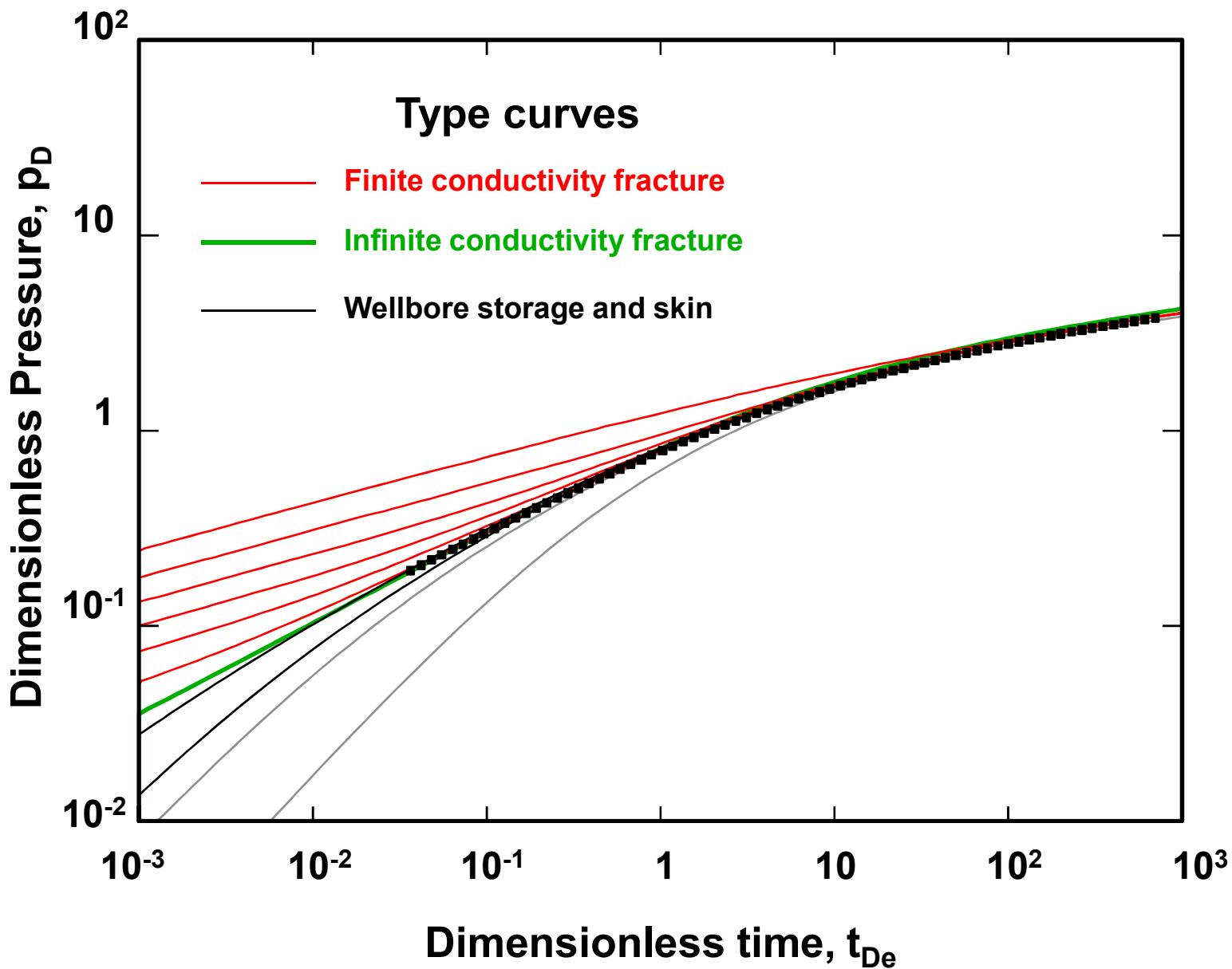
# FINITE CONDUCTIVITY VERTICAL FRACTURE AT THE CENTRE OF A CLOSED SQUARE



# FINITE CONDUCTIVITY VERTICAL FRACTURE







Wellbore storage and skin

Infinite conductivity fracture

Finite conductivity fracture

**PM**

$$p_D = \frac{kh}{141.2 \Delta q B \mu} \Delta p$$

$$p_D = \frac{kh}{141.2 \Delta q B \mu} \Delta p$$

$$p_D = \frac{kh}{141.2 \Delta q B \mu} \Delta p$$

**TM**

$$\frac{t_D}{C_D} = 0.000295 \frac{kh}{\mu C} \Delta t$$

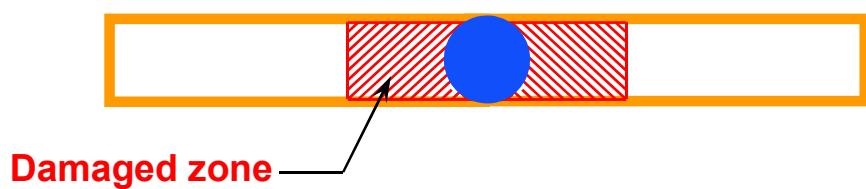
$$t_{Df} = \frac{0.000264 k}{\phi \mu c_t x_f^2} \Delta t$$

$$t_{De} = \frac{0.000264 k}{\phi \mu c_t r_{we}^2} \Delta t$$

# DAMAGED FRACTURE

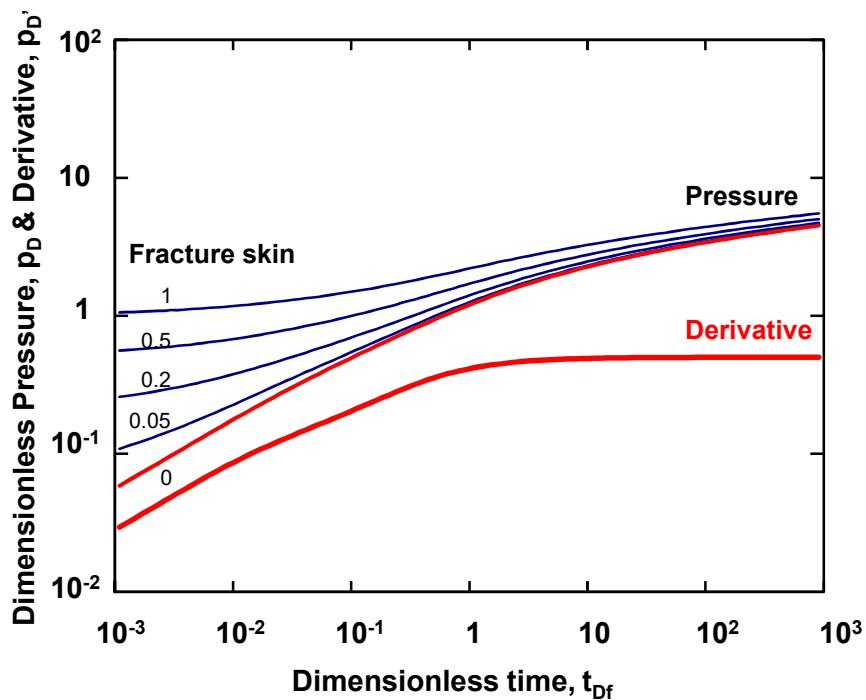
## Choked vertical fracture

Chavez, Alejandro and Cinco-Ley, SPE 104004(Sept., 2006)



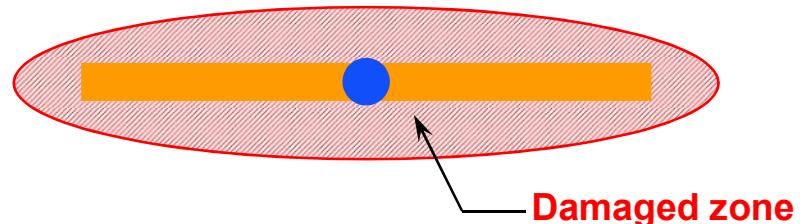
- SKIN ADDITIVE TO DIMENSIONLESS PRESSURE
- NO EFFECT ON DERIVATIVE UNLESS THERE IS WELLBORE STORAGE

## INFINITE CONDUCTIVITY

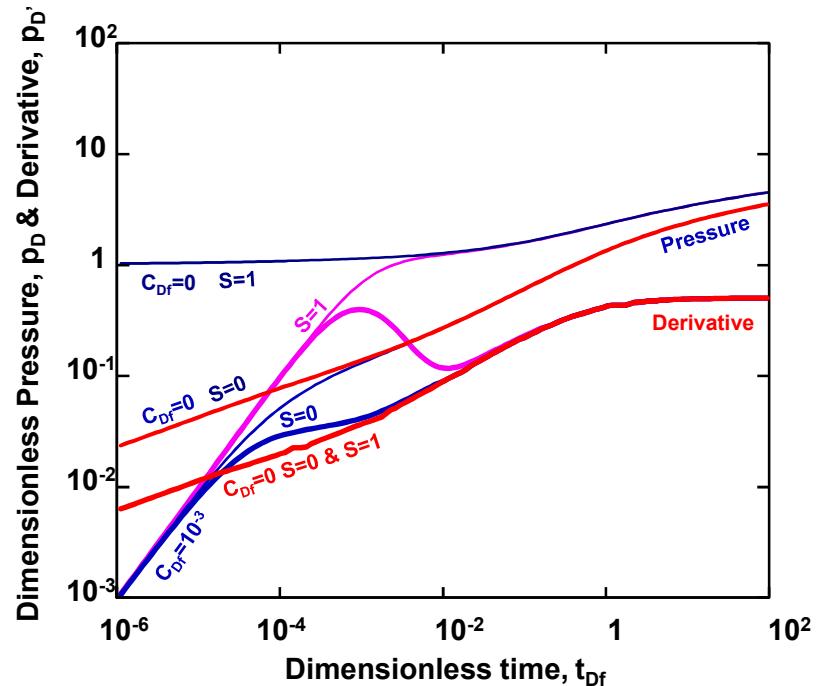


## Vertical fracture with fluid loss damage

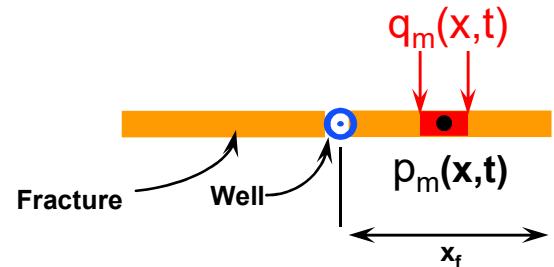
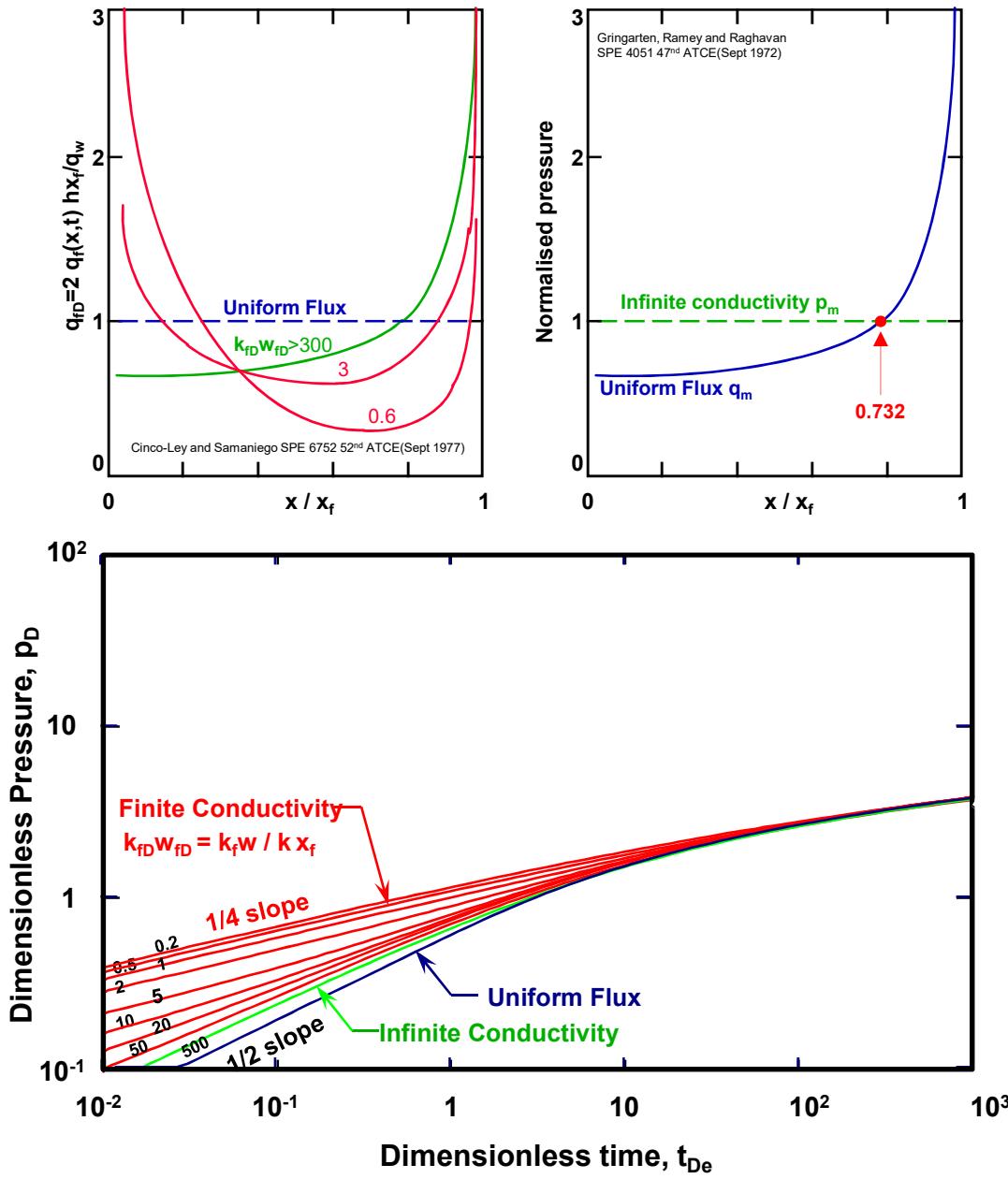
Cinco-Ley and Samaniego SPE 6752 52<sup>nd</sup> ATCE(Sept 1977)



## FINITE CONDUCTIVITY



# UNIFORM FLUX VERTICAL FRACTURE



$q_m(x,t)$  influx / unit area / unit time

- $q_m(x,t)$  uniform (constant) over the fracture length:

**UNIFORM FLUX FRACTURE**

- $p_m(x,t)$  uniform (constant) over the fracture length:

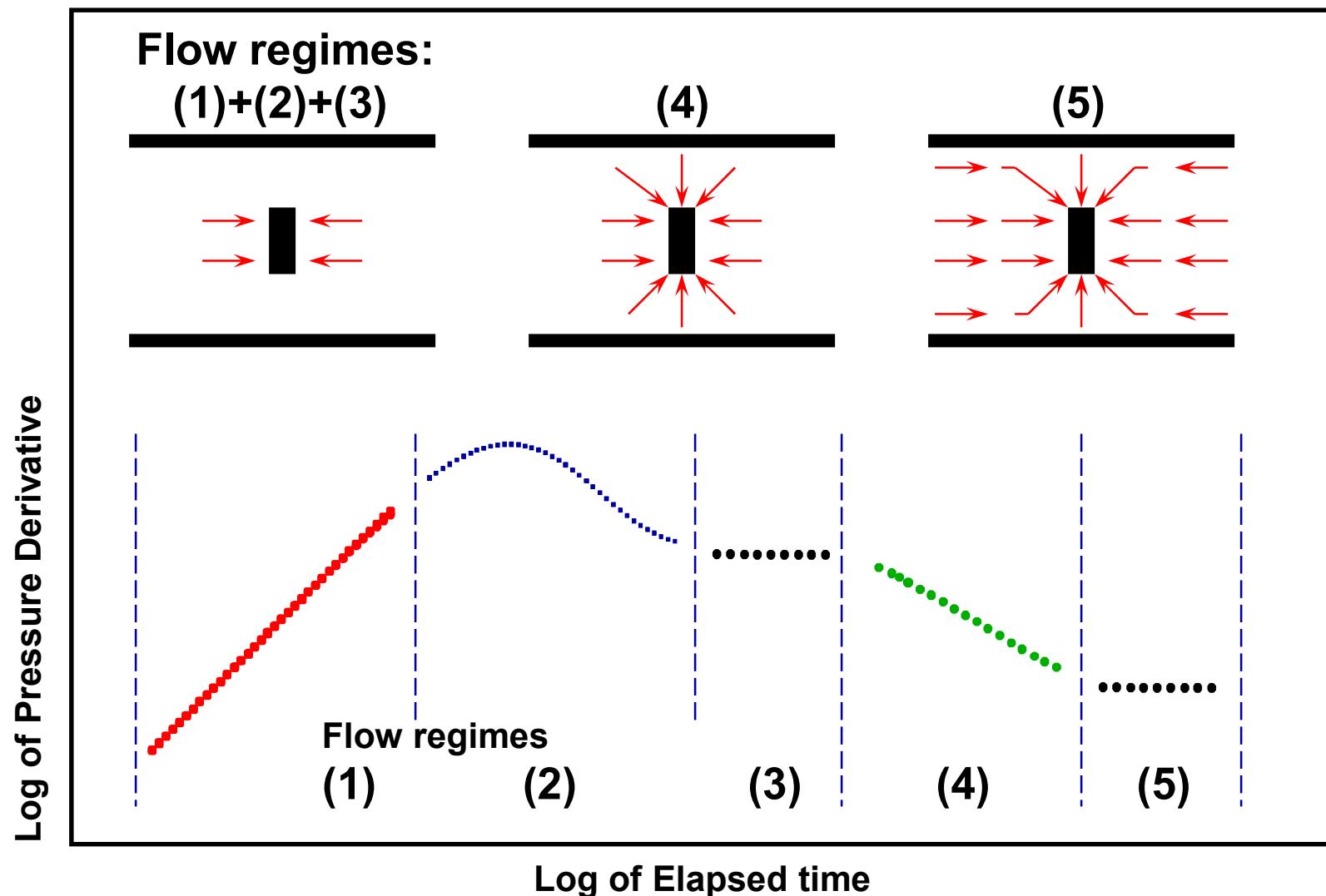
**INFINITE CONDUCTIVITY FRACTURE**

- Infinite fracture is a limiting case of **FINITE CONDUCTIVITY FRACTURE**

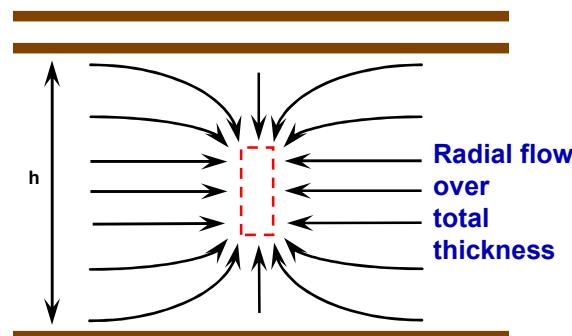
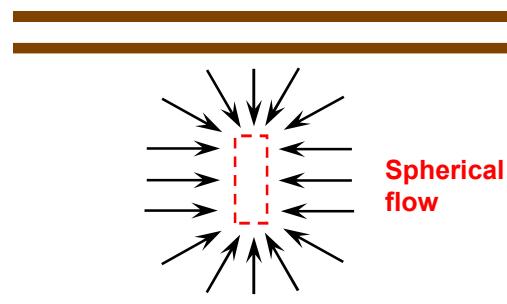
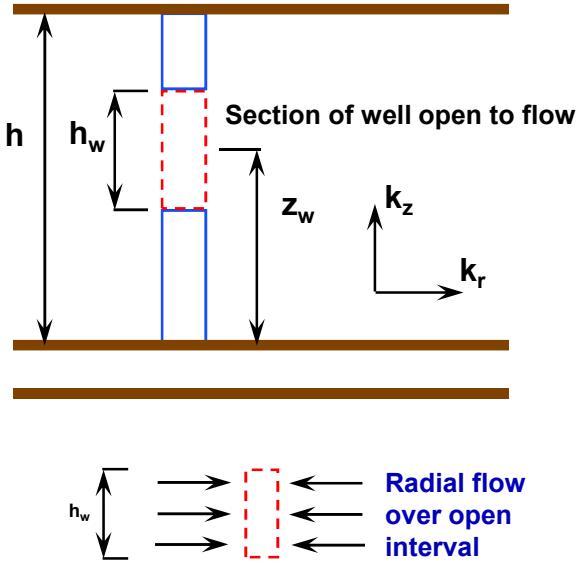
# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
Wellbore Storage Skin Fracture <b>Partial Penetration</b> Horizontal Well	Homogeneous Heterogeneous -2-Porosity -2-Permeability -Composite	Infinite extent Specified Rate Specified Pressure Leaky Boundary
EARLY TIMES	MIDDLE TIMES	LATE TIMES

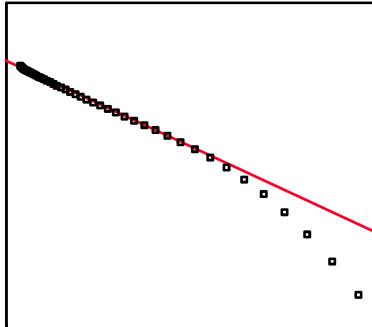
# Well with wellbore storage and skin and limited entry in an infinite reservoir with homogeneous behaviour



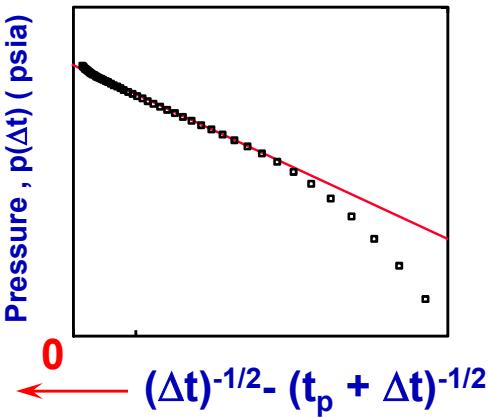
# STRAIGHT LINE METHOD FOR SPHERICAL FLOW (Middle Times)



Pressure Change,  $\Delta p$  (psi)



Pressure,  $p(\Delta t)$  (psia)



Specialised Plot

$$\Delta p = 70.6 \frac{\Delta q B \mu}{k_{SPH} r_{SPH}} - 2452.9 \frac{\Delta q B \mu \sqrt{\phi \mu c_t}}{k_{SPH}^{3/2} \sqrt{\Delta t}}$$

Horner Plot

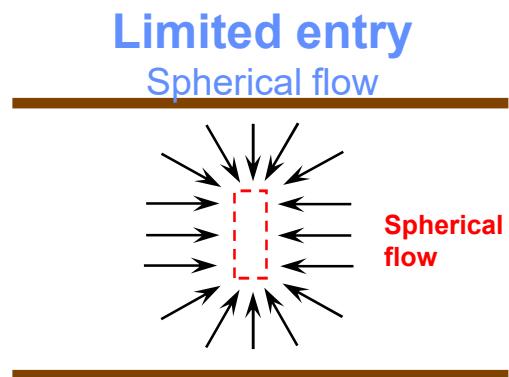
$$p(\Delta t) = \bar{p}_i - 70.6 \frac{\Delta q B \mu}{k_{SPH} r_{SPH}} - 2452.9 \frac{\Delta q B \mu (\phi \mu c_t)^{1/2}}{(k_{SPH})^{3/2}} \left[ (\Delta t)^{-1/2} - (t_p + \Delta t)^{-1/2} \right]$$

$$k_{SPH} = \sqrt[3]{k_r^2 k_z}$$

$$m_{SPH} = 2452.9 \frac{\Delta q B \mu (\phi \mu c_t)^{1/2}}{(k_{SPH})^{3/2}}$$

$$k_{SPH} = \left[ 2452.9 \frac{\Delta q B \mu (\phi \mu c_t)^{1/2}}{m_{SPH}} \right]^{2/3} mD$$

## DERIVATIVE FOR SPHERICAL FLOW (Middle Times)



$$\frac{dp_D}{d \ln(t_{SPH D})} = \frac{1}{2} \left[ \frac{1}{2} \left( \pi t_{SPH D} \right)^{-1/2} \right]$$

✓ Negative Half-unit slope log-log straight line

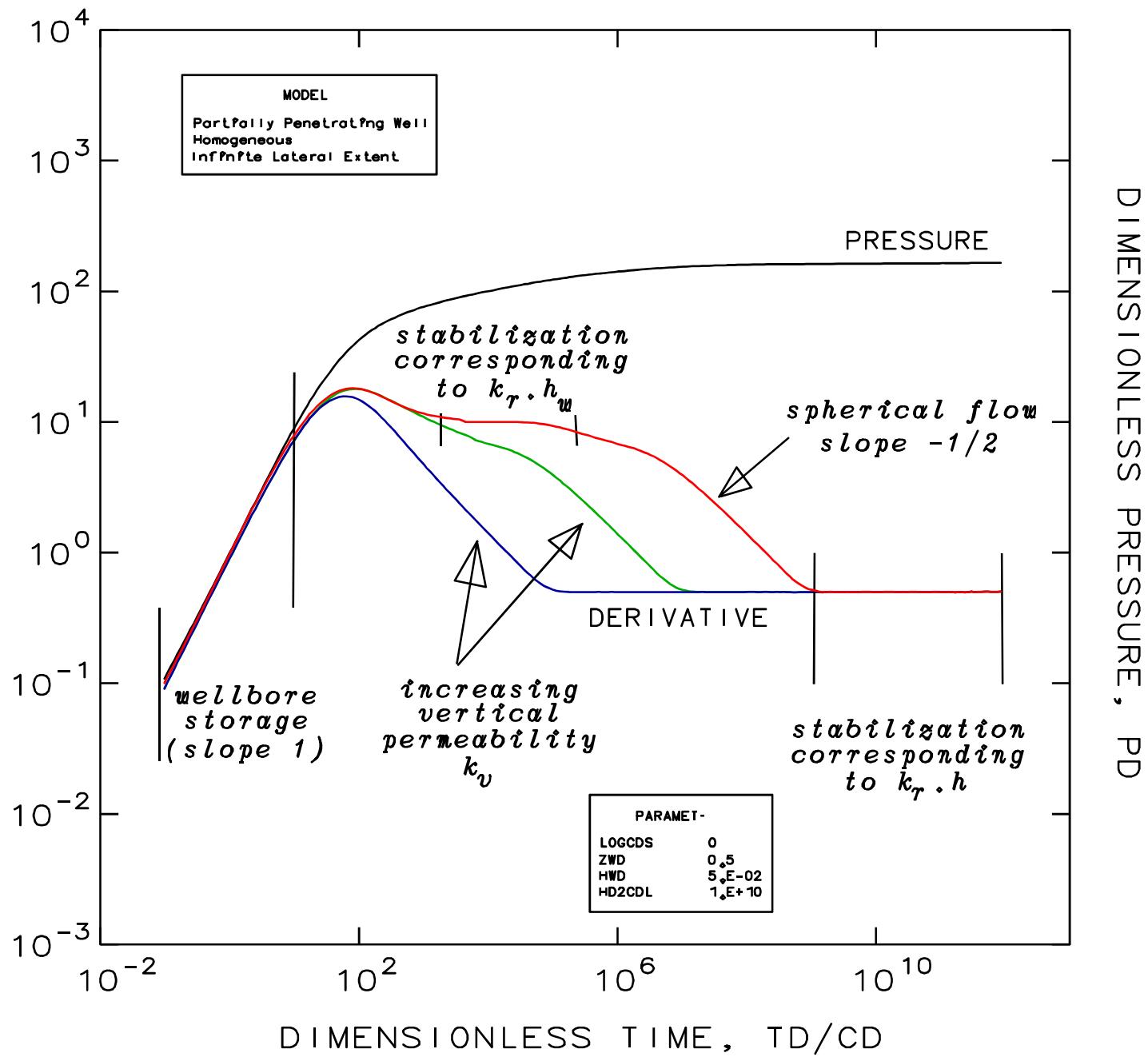
$$p_{SPH D} = \frac{1}{2} \left[ 1 - \left( \pi t_{SPH D} \right)^{-1/2} \right]$$

$$p_{SPH D} = \frac{k_{SPH} r_{SPH}}{141.2 \Delta q B \mu} \Delta p$$

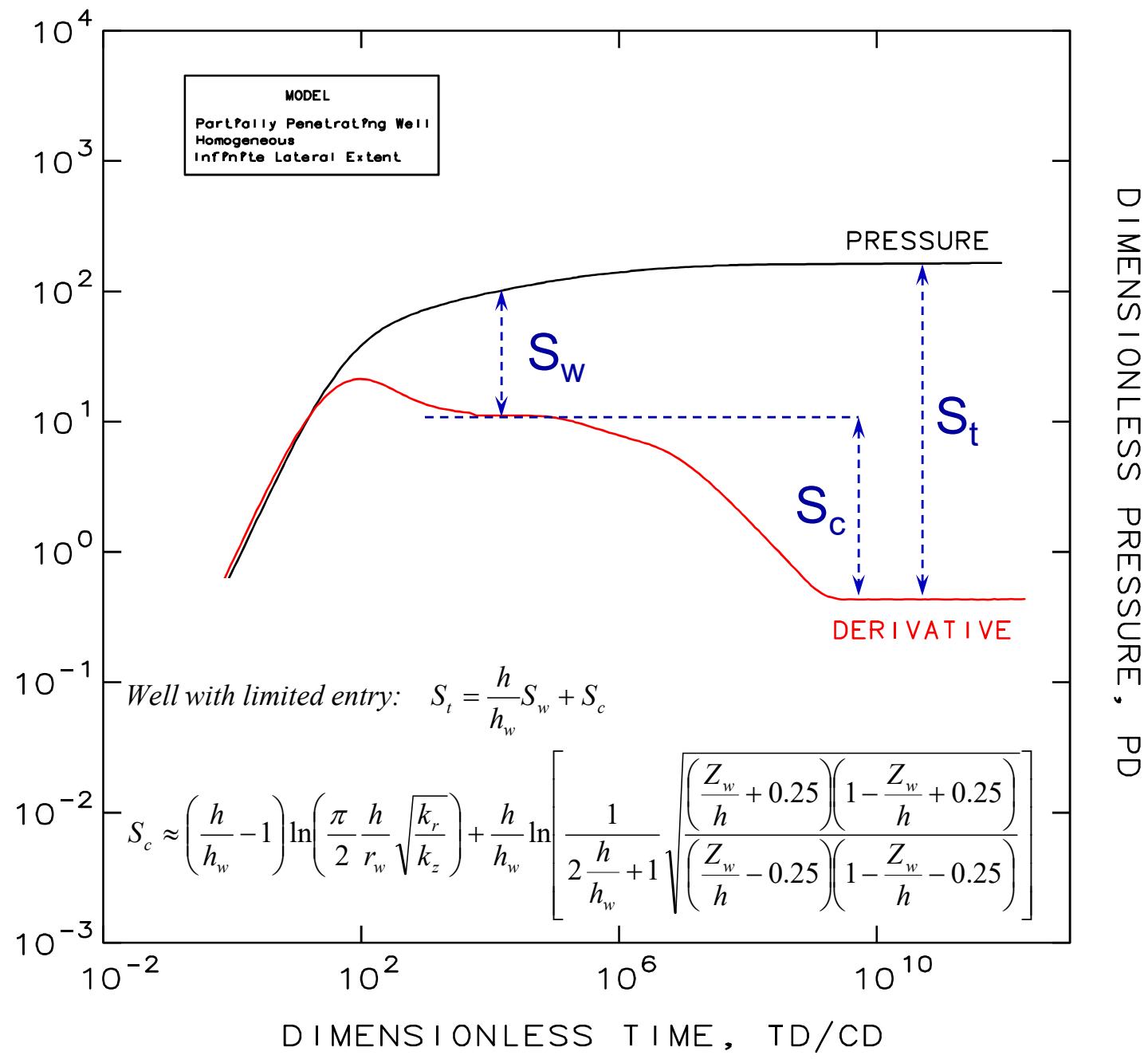
$$t_{SPH D} = \frac{0.00264 k_{SPH}}{\phi \mu c_t r_{SPH}^2} \Delta t$$



# WELL WITH LIMITED ENTRY

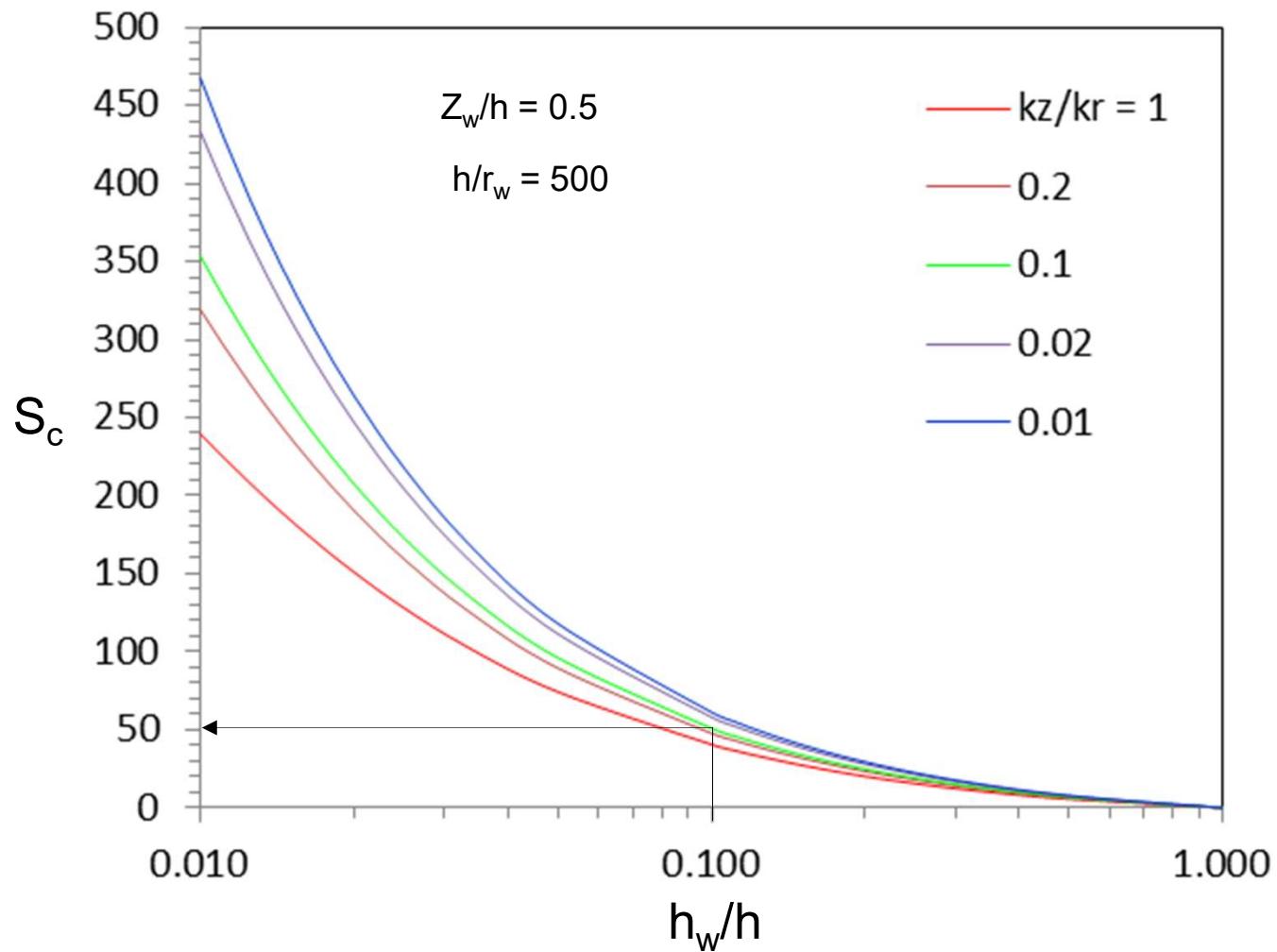


# WELL WITH LIMITED ENTRY

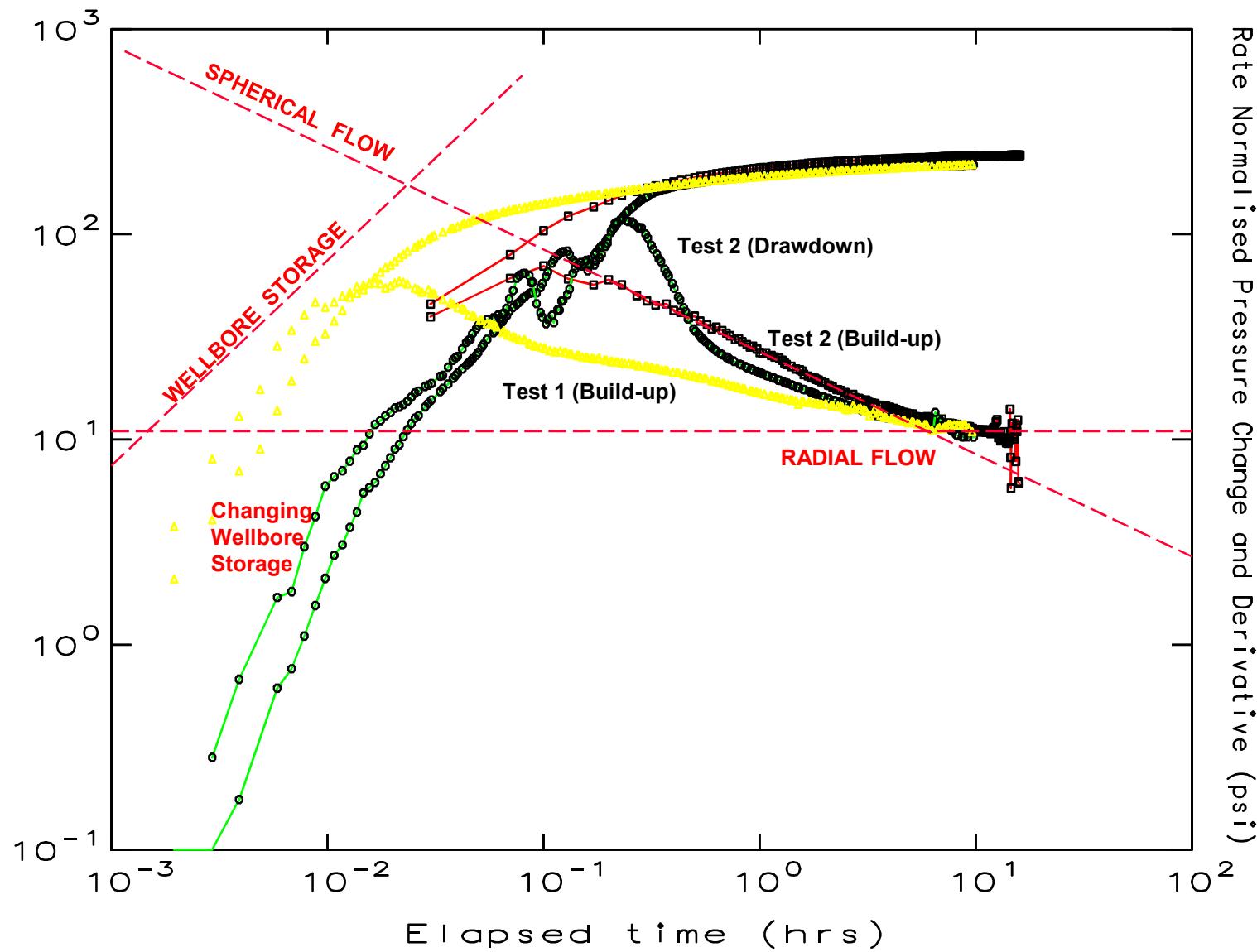


## WELL WITH LIMITED ENTRY

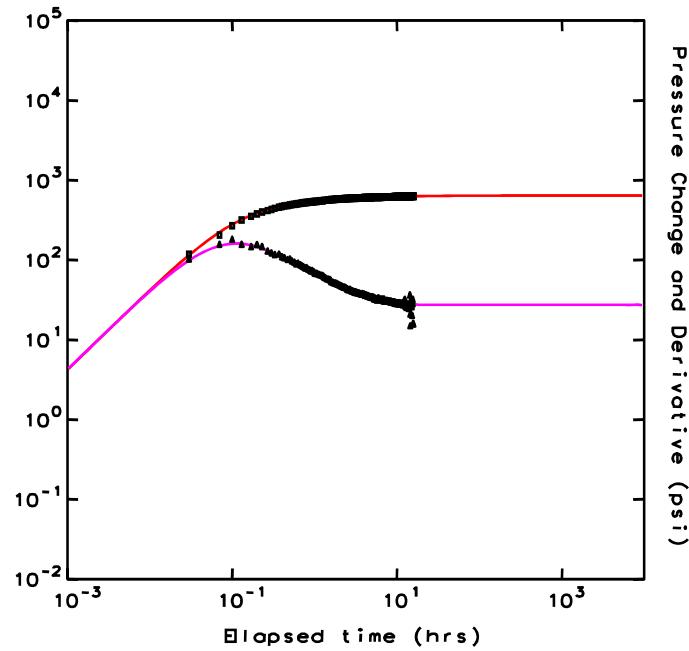
$$S_c \approx \left( \frac{h}{h_w} - 1 \right) \ln \left( \frac{\pi}{2} \frac{h}{r_w} \sqrt{\frac{k_r}{k_z}} \right) + \frac{h}{h_w} \ln \left[ \frac{1}{2 \frac{h}{h_w} + 1} \sqrt{\frac{\left( \frac{Z_w}{h} + 0.25 \right) \left( 1 - \frac{Z_w}{h} + 0.25 \right)}{\left( \frac{Z_w}{h} - 0.25 \right) \left( 1 - \frac{Z_w}{h} - 0.25 \right)}} \right]$$



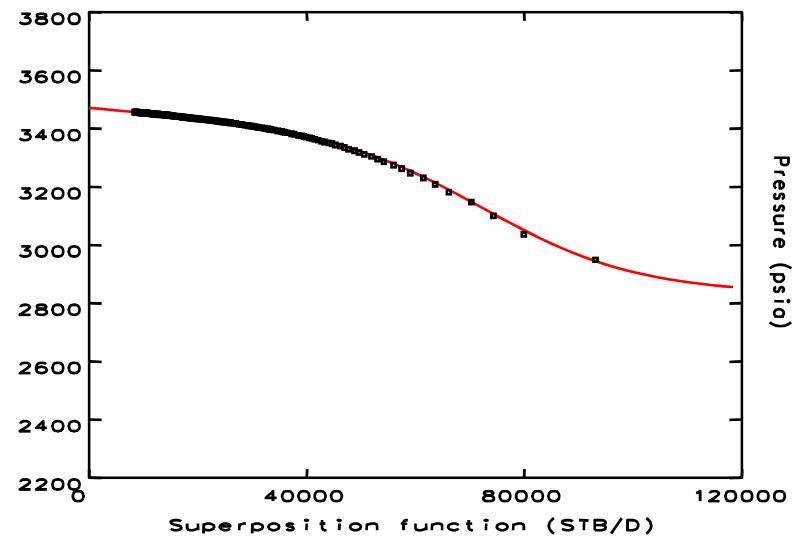
# Maureen A2



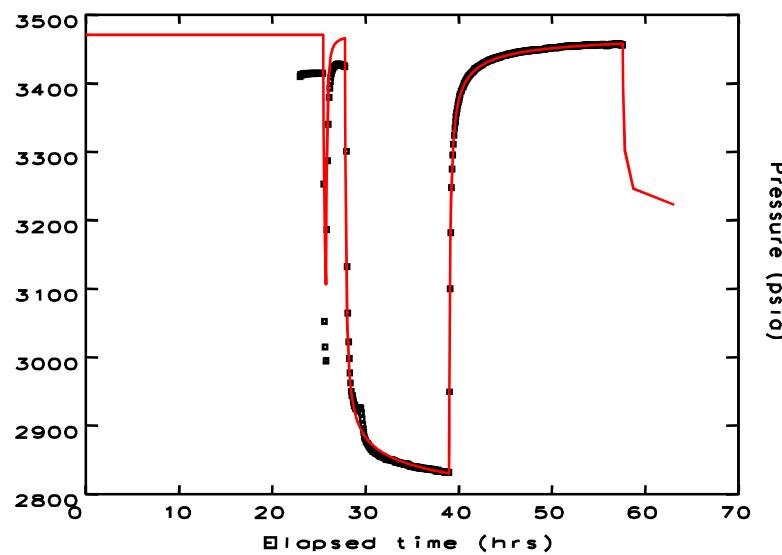
# Maureen A2 Test 1 (Exploration)



Pressure Change and Derivative (psi)



Pressure (psi)

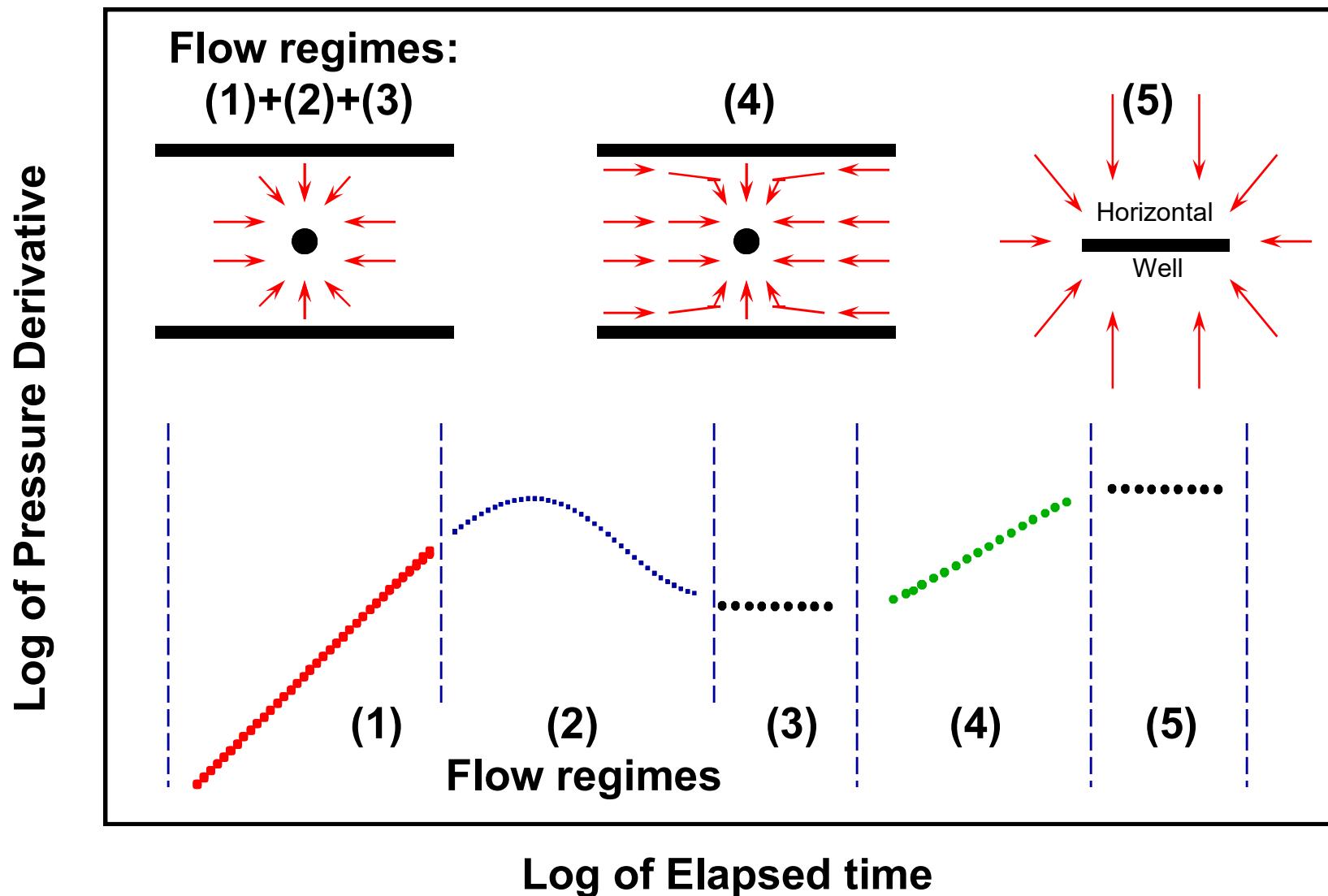


Pressure (psi)

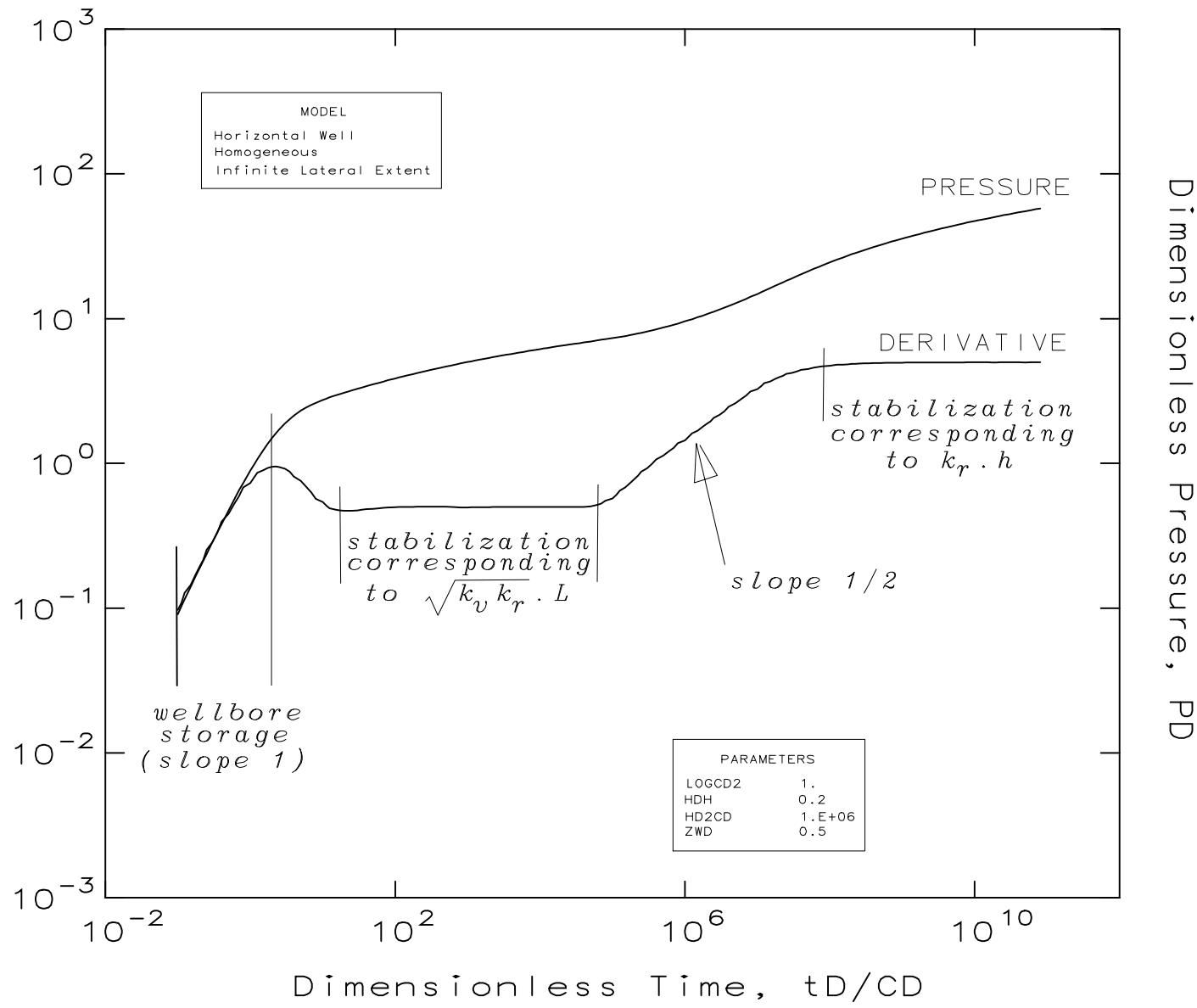
# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
Wellbore Storage	Homogeneous	Infinite extent
Skin	Heterogeneous	Specified Rate
Fracture	-2-Porosity	Specified Pressure
Partial Penetration	-2-Permeability	Leaky Boundary
Horizontal Well	-Composite	
EARLY TIMES	MIDDLE TIMES	LATE TIMES

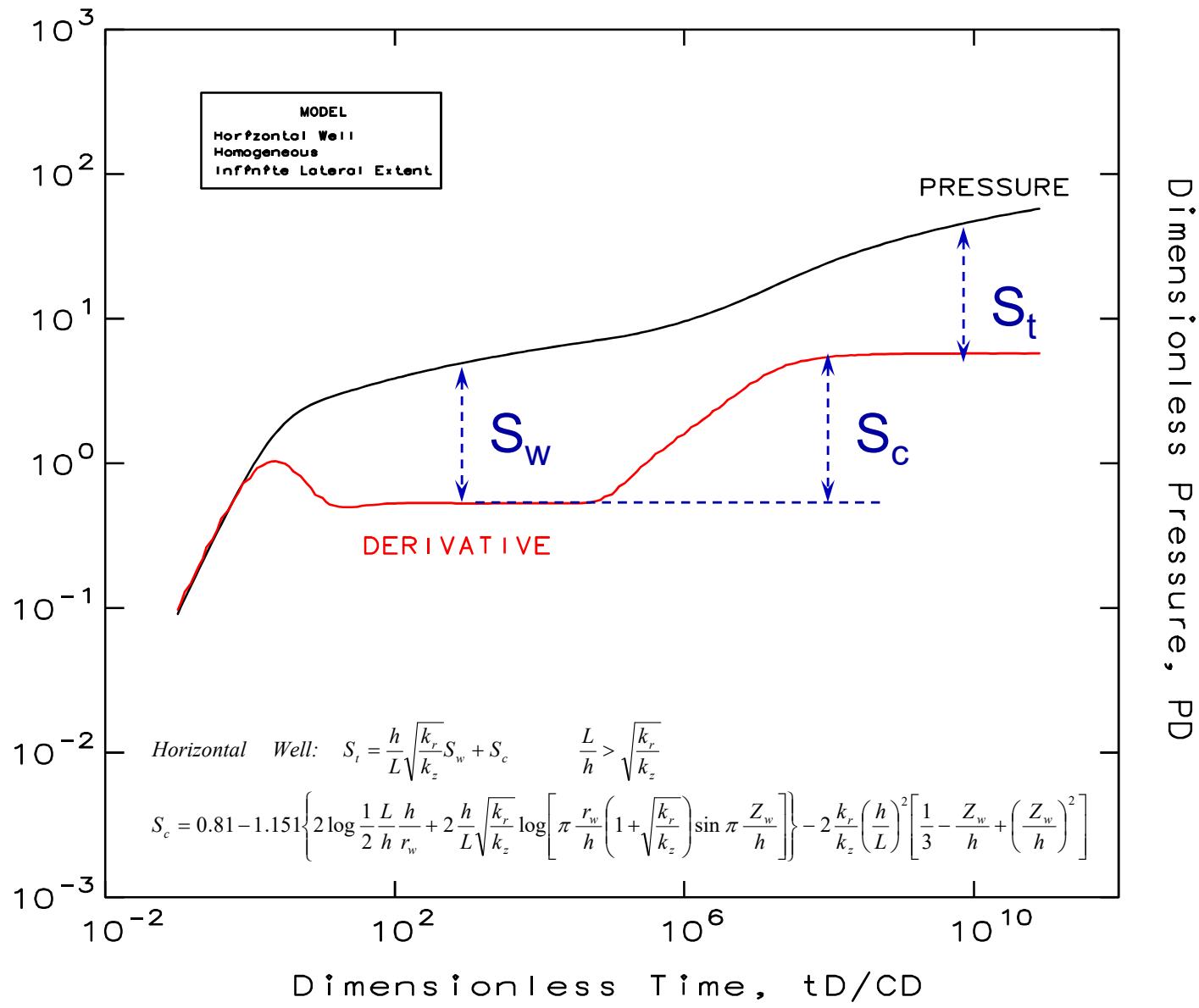
# Horizontal well with wellbore storage and skin in an infinite reservoir with homogeneous behaviour



# HORIZONTAL WELL

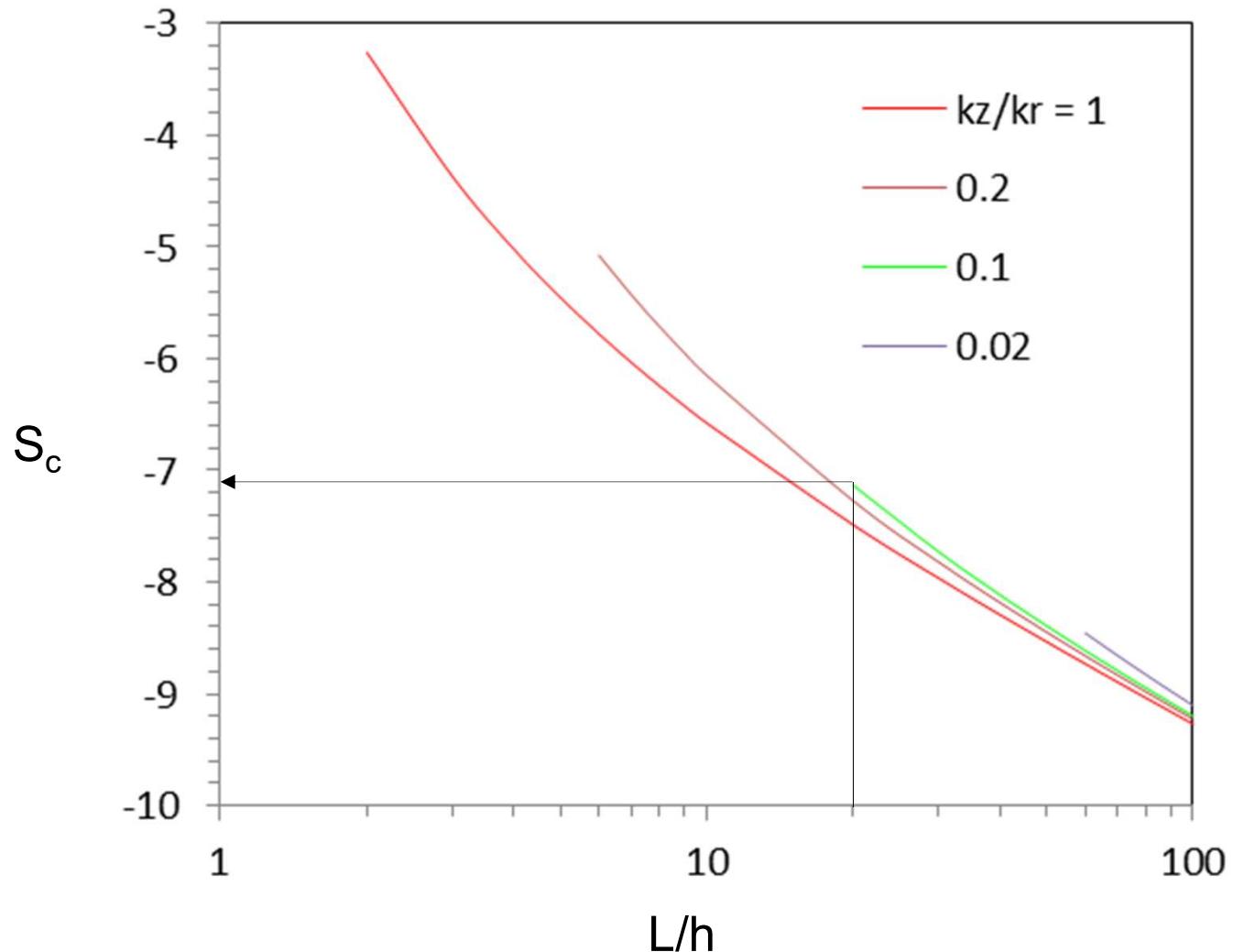


# HORIZONTAL WELL

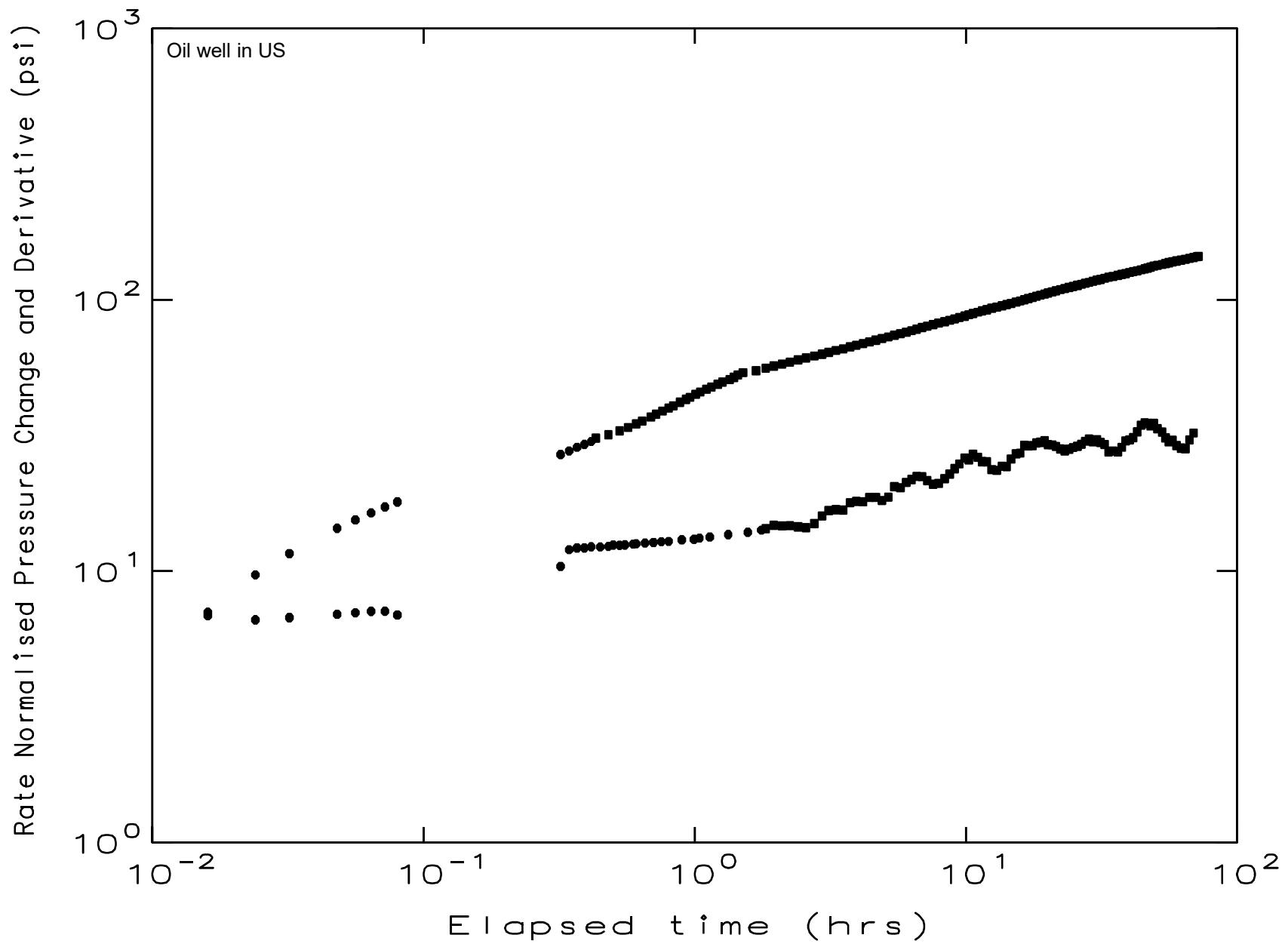


# HORIZONTAL WELL

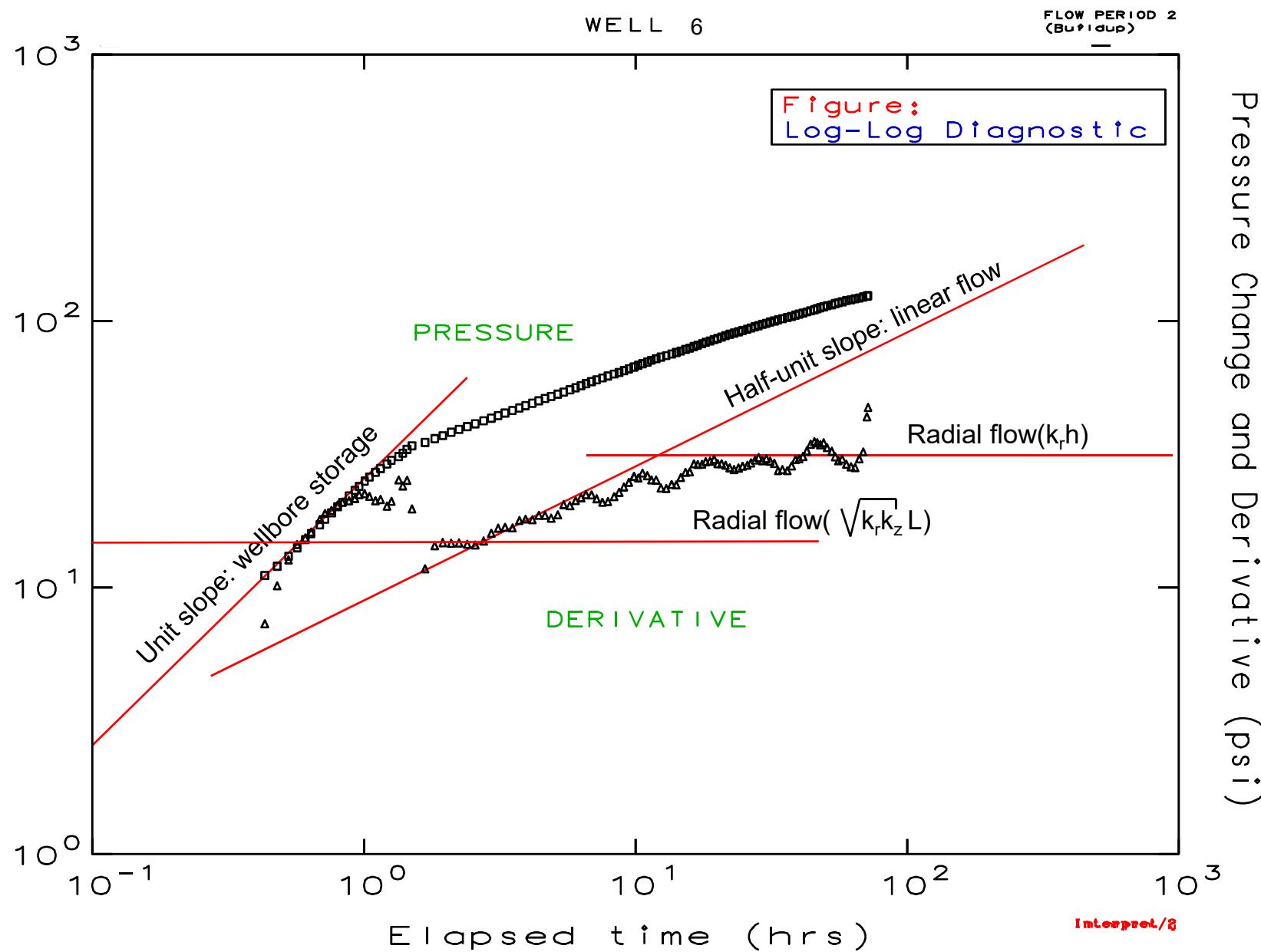
$$S_c = 0.81 - 1.151 \left\{ 2 \log \frac{1}{2} \frac{L}{h} \frac{h}{r_w} + 2 \frac{h}{L} \sqrt{\frac{k_r}{k_z}} \log \left[ \pi \frac{r_w}{h} \left( 1 + \sqrt{\frac{k_r}{k_z}} \right) \sin \pi \frac{Z_w}{h} \right] \right\} - 2 \frac{k_r}{k_z} \left( \frac{h}{L} \right)^2 \left[ \frac{1}{3} - \frac{Z_w}{h} + \left( \frac{Z_w}{h} \right)^2 \right]$$



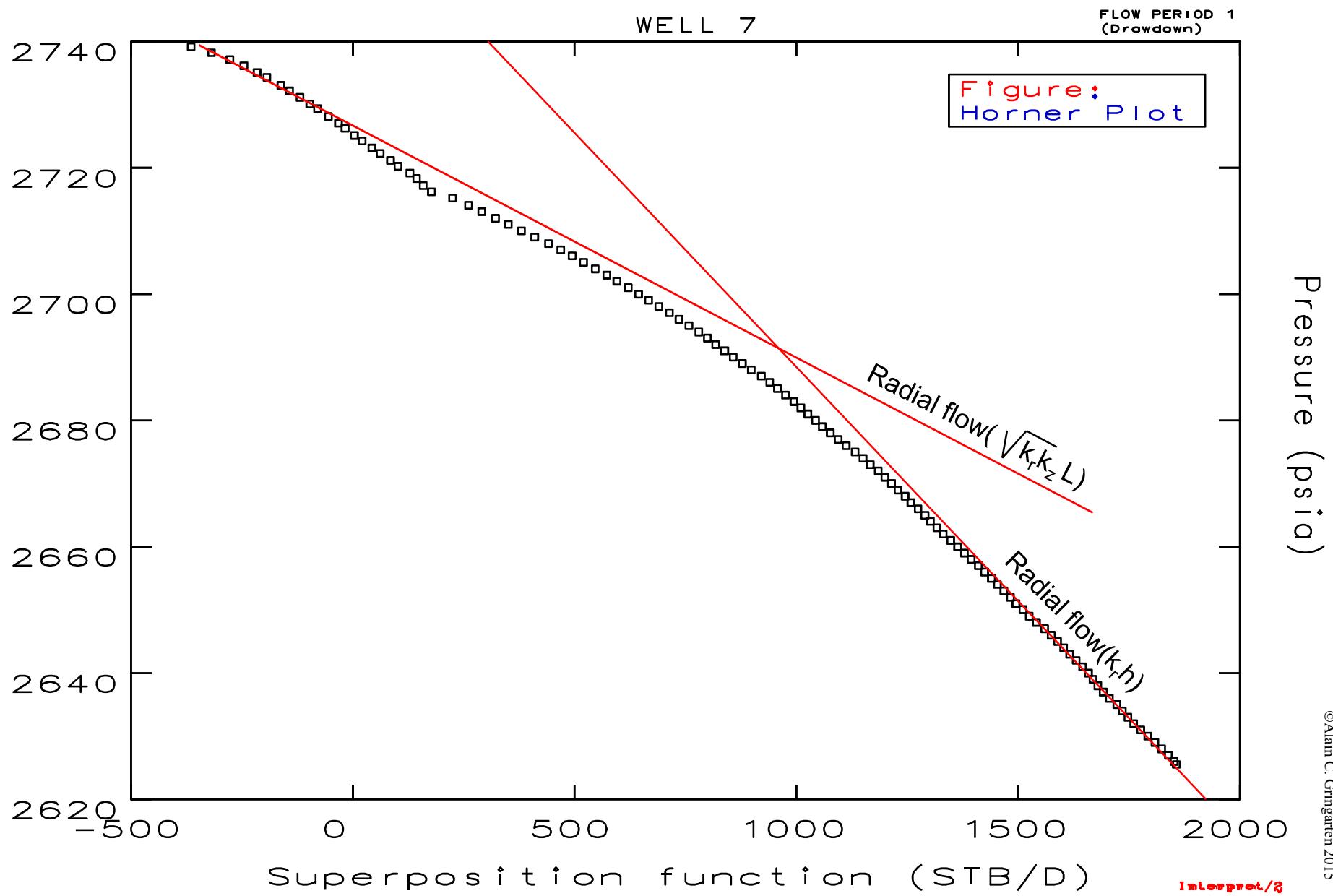
## HORIZONTAL WELL



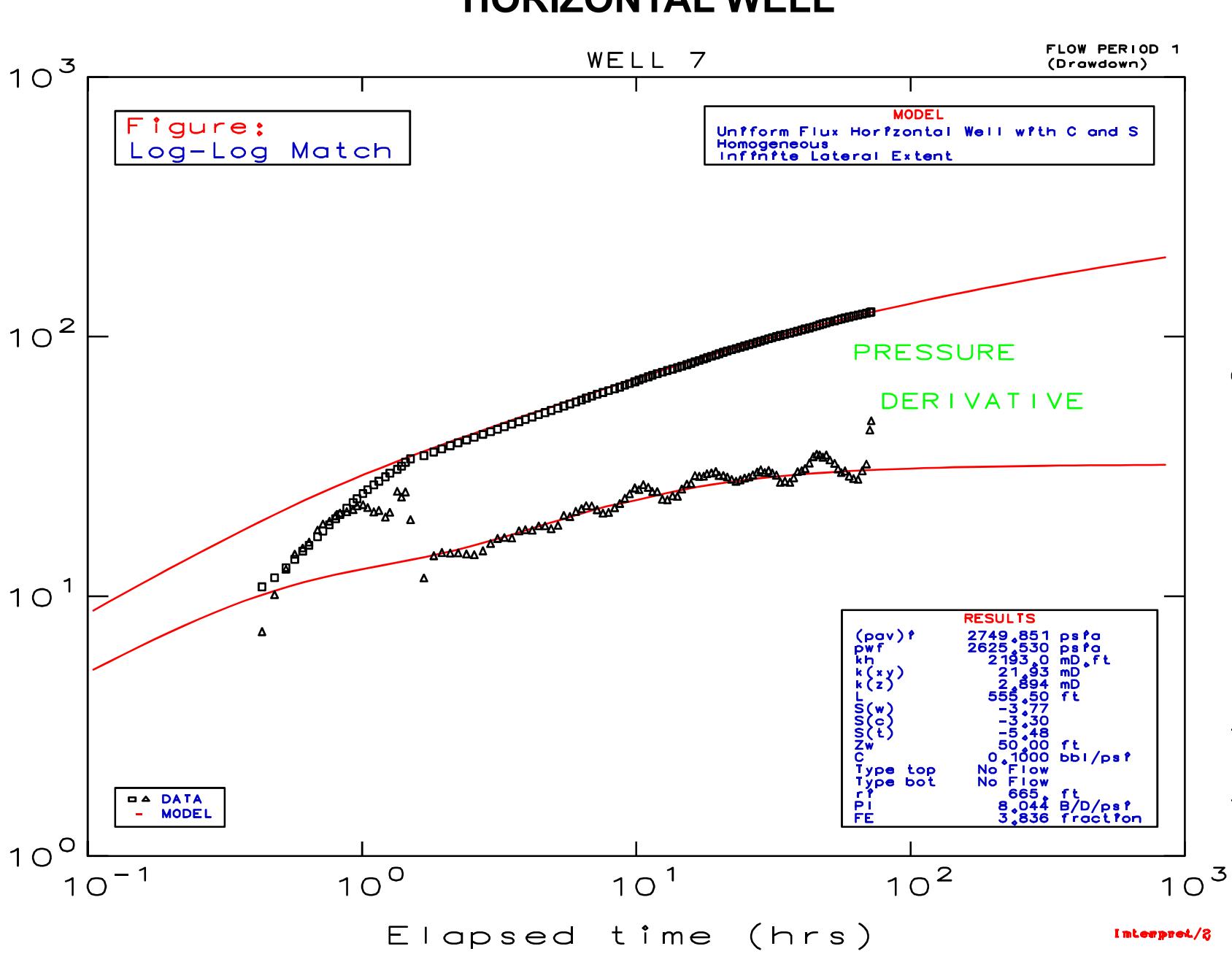
# HORIZONTAL WELL



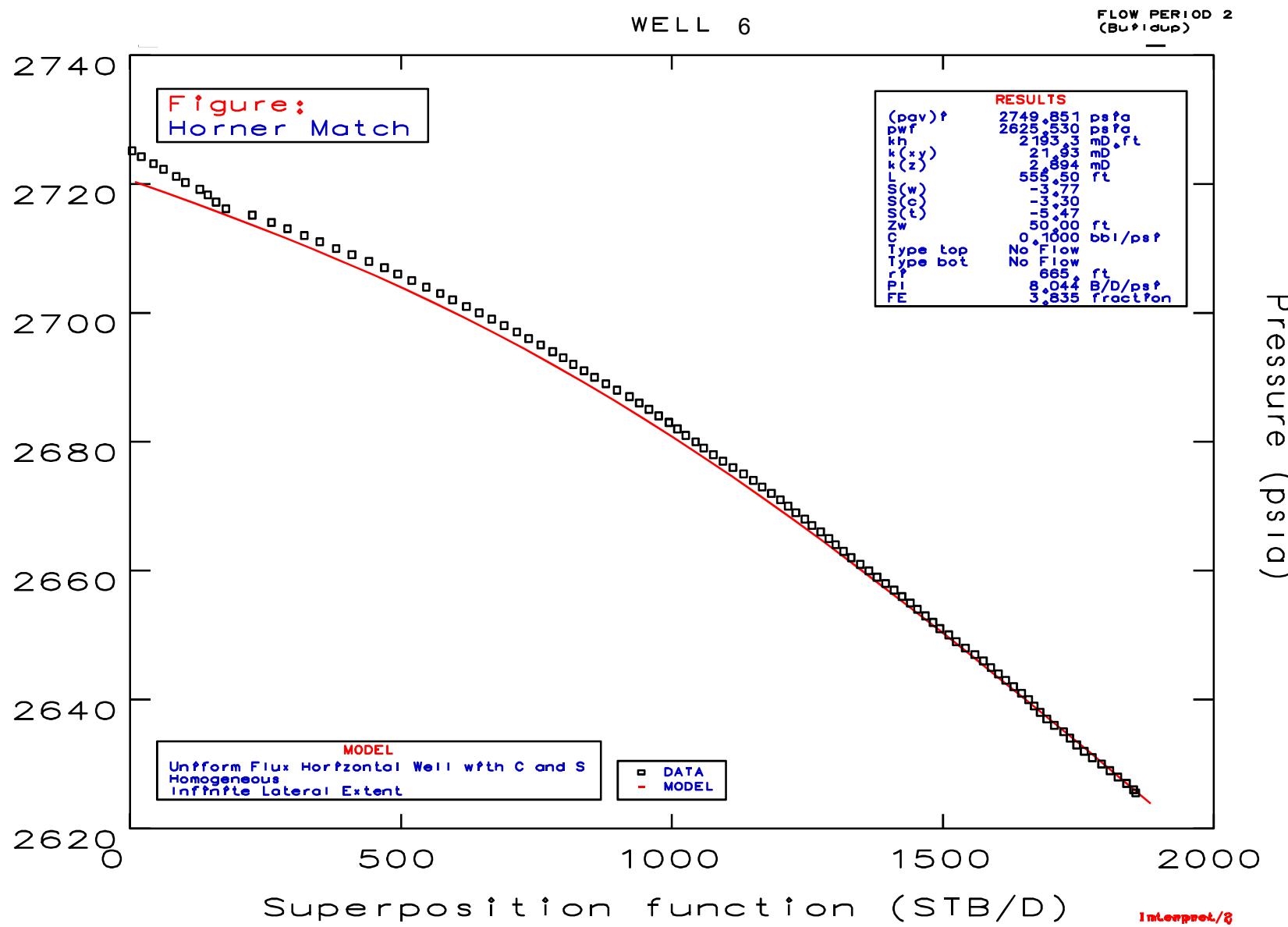
# HORIZONTAL WELL



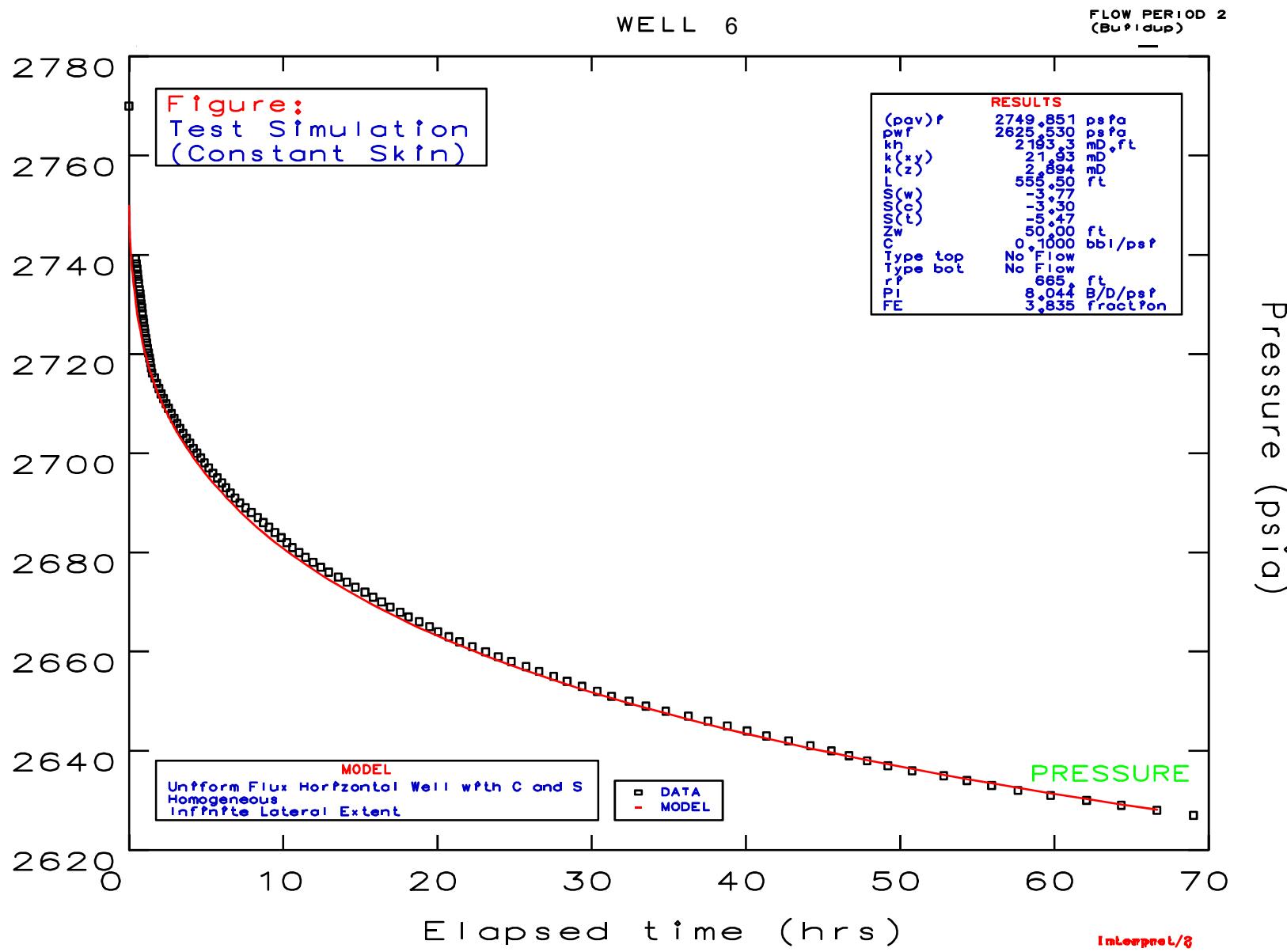
# Pressure Change and Derivative (psi)



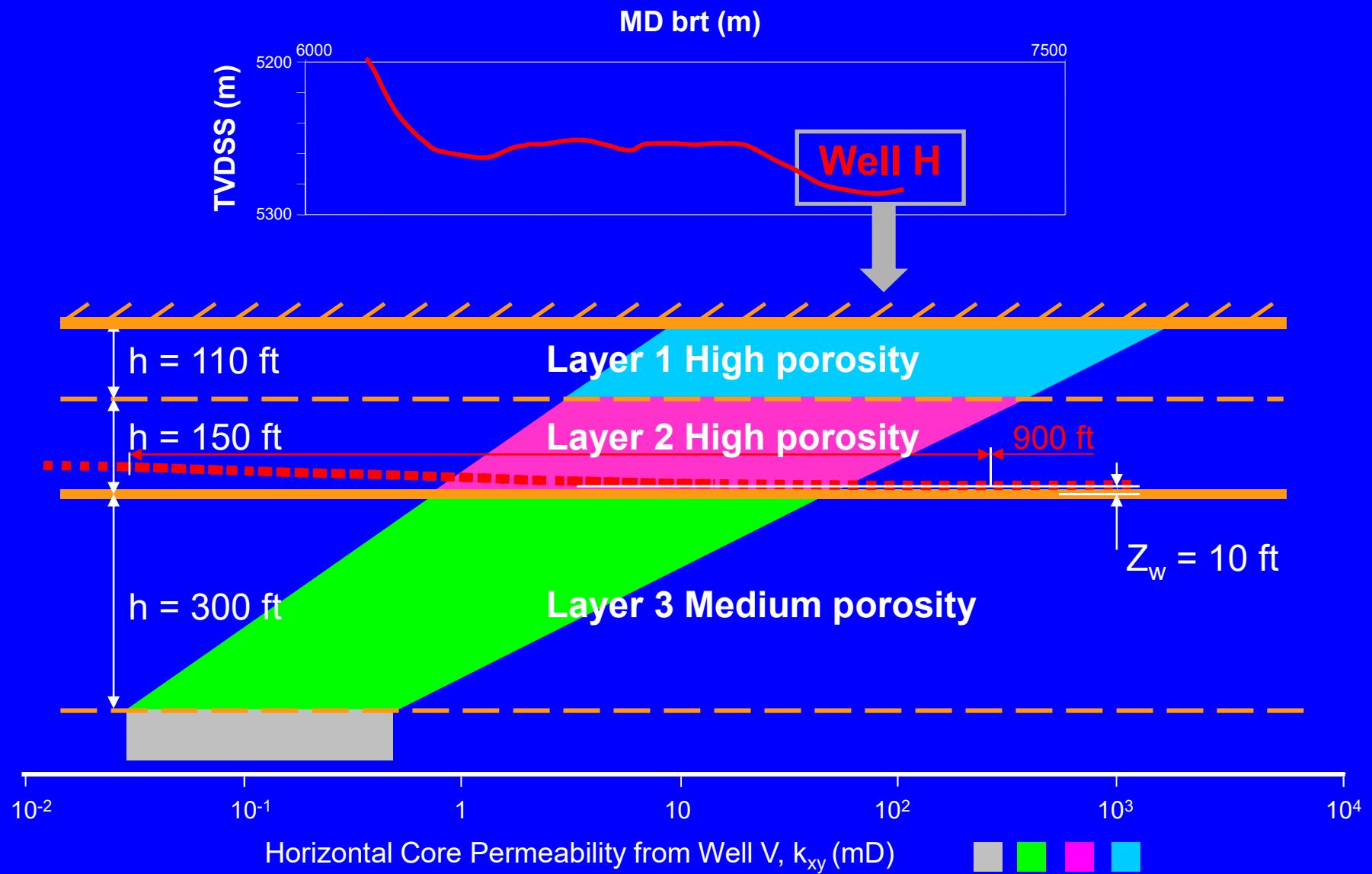
# HORIZONTAL WELL



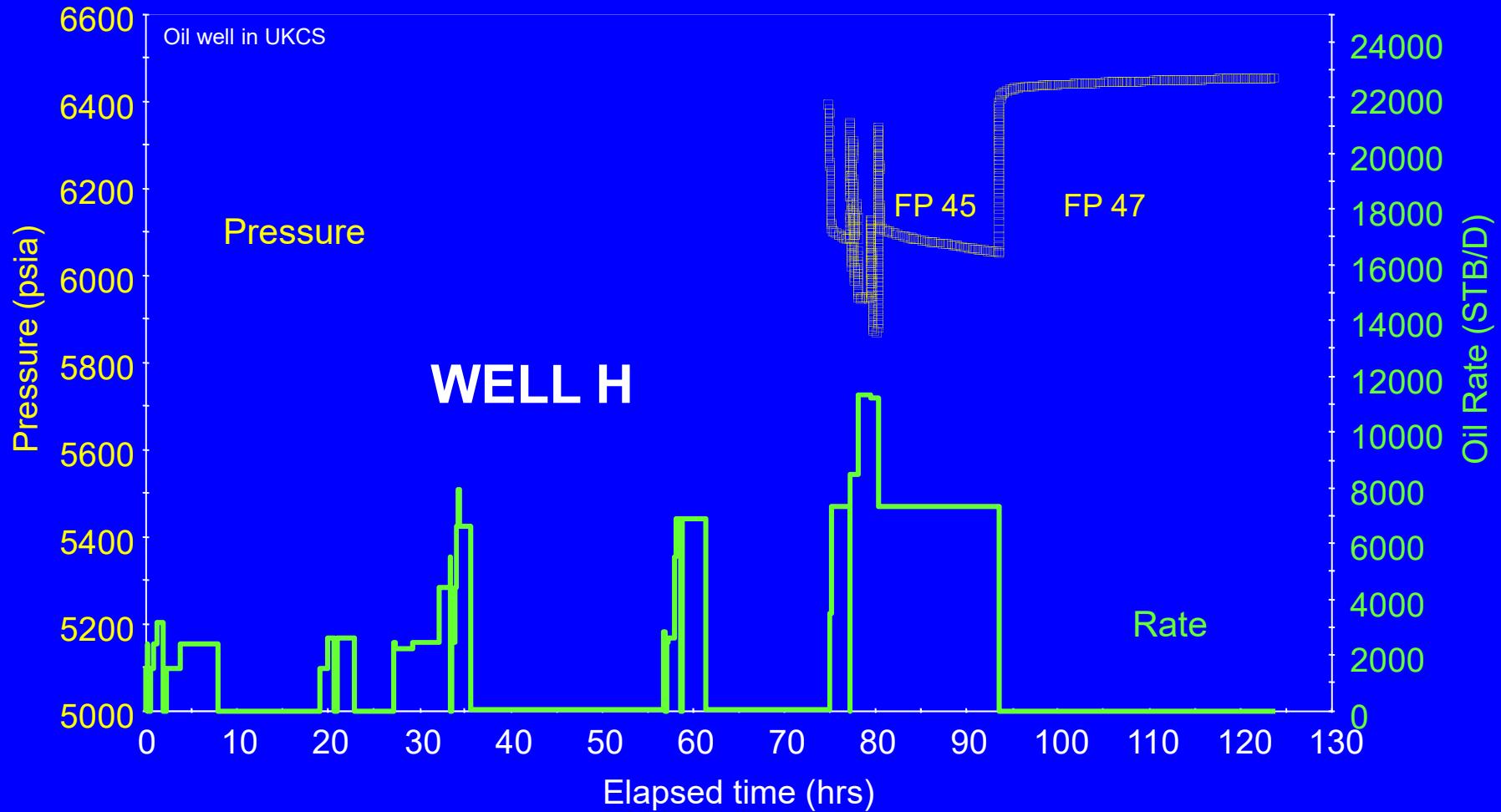
# HORIZONTAL WELL

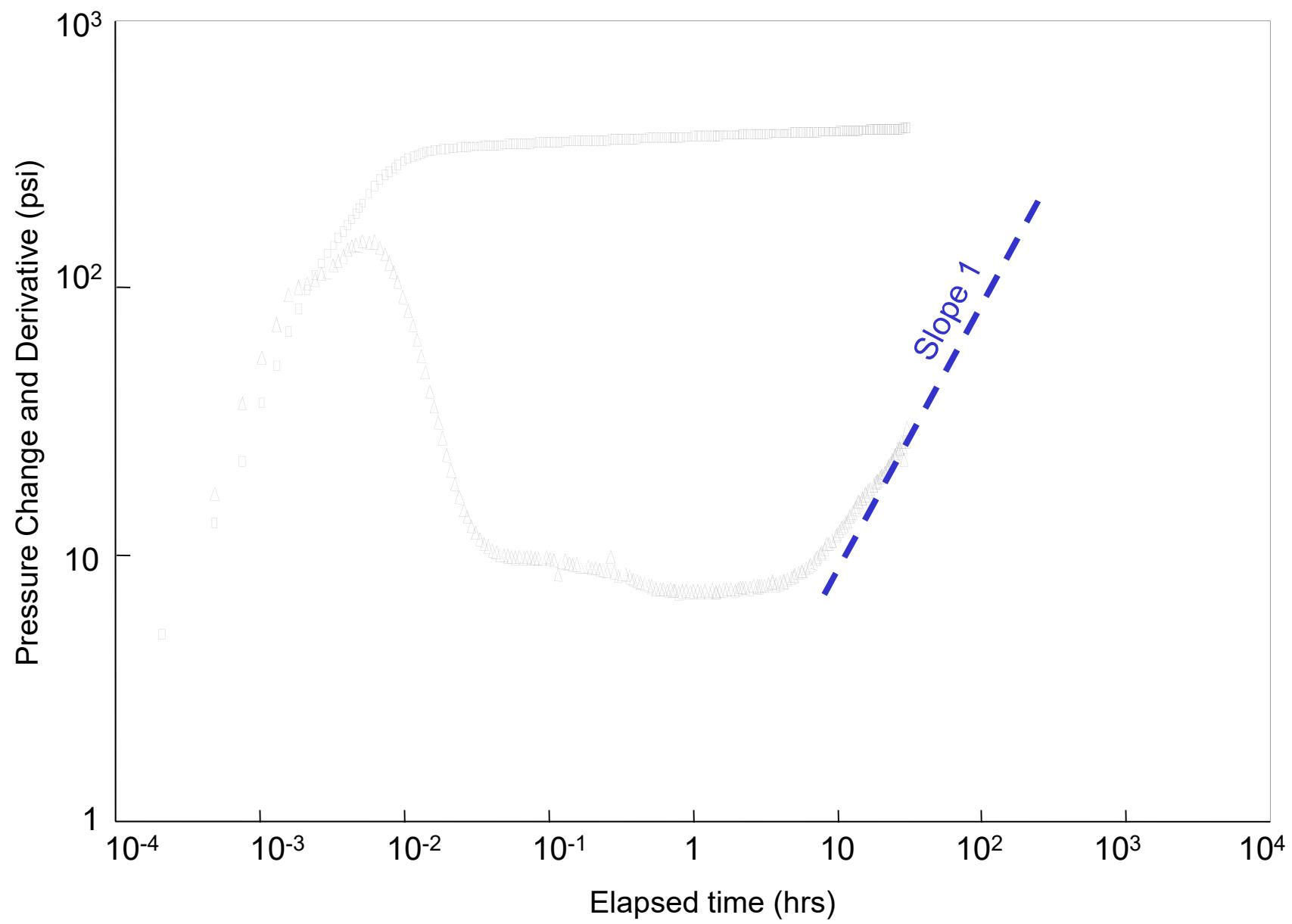


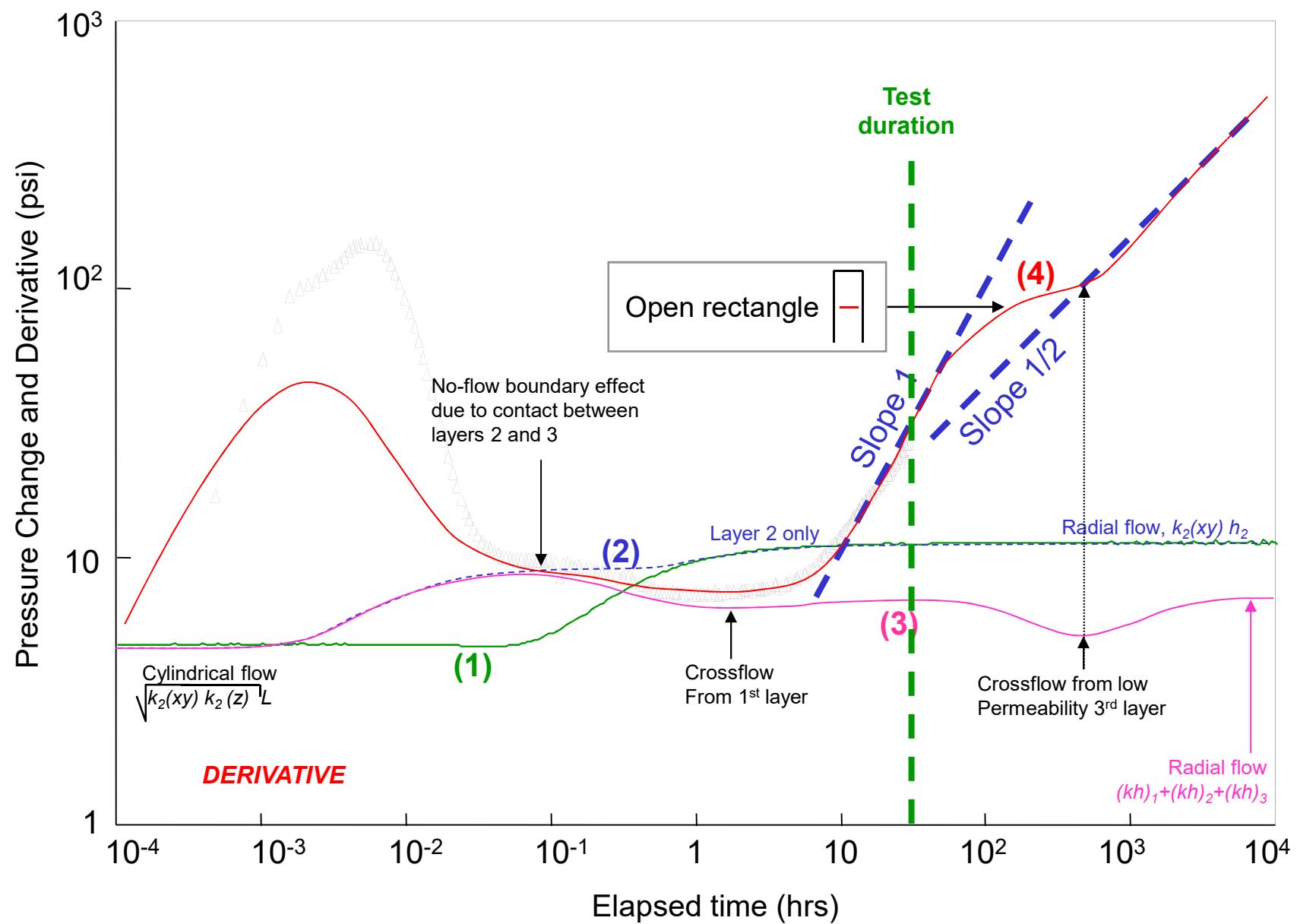
# Cross section Well H



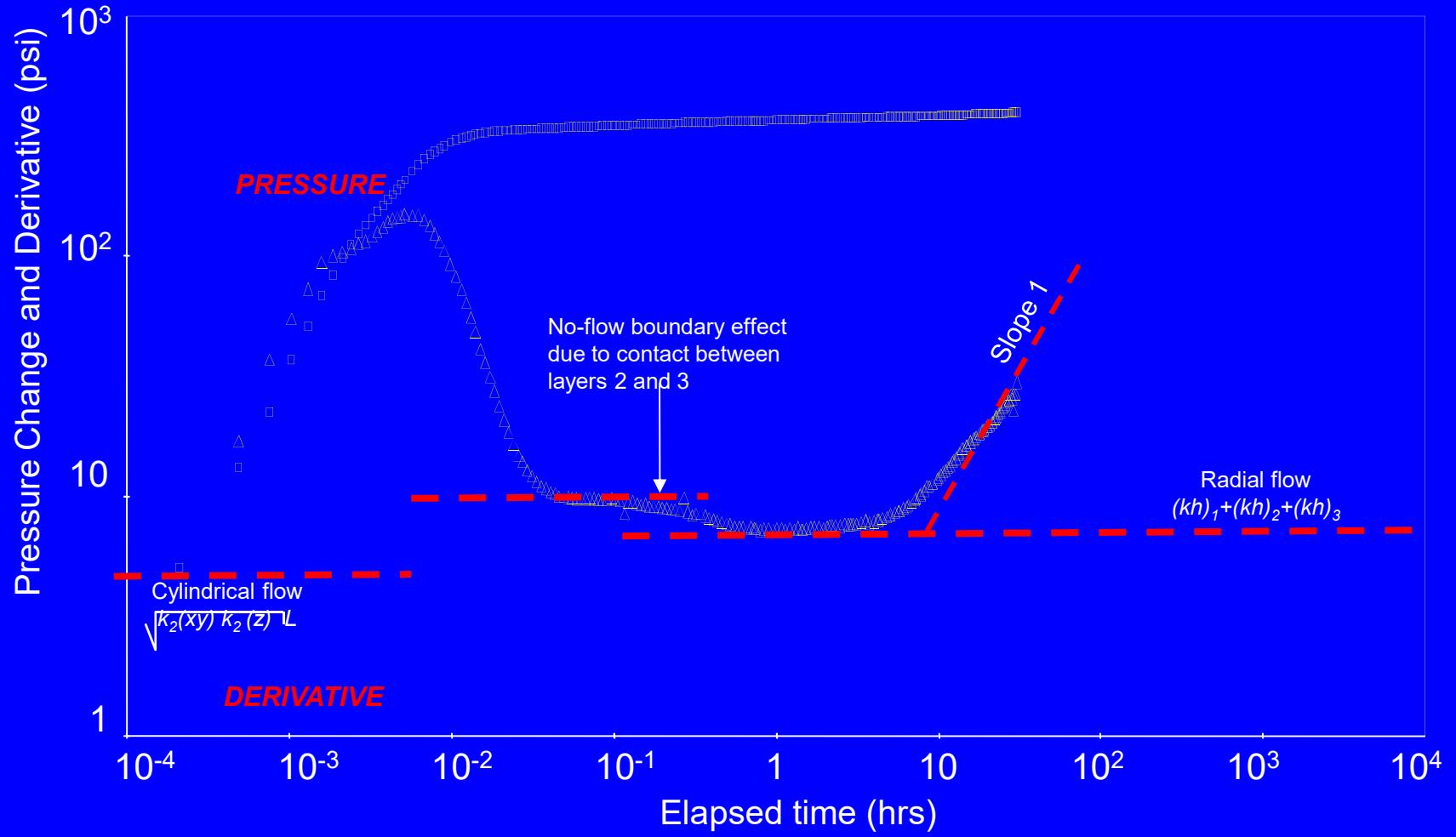
# Test on Well H



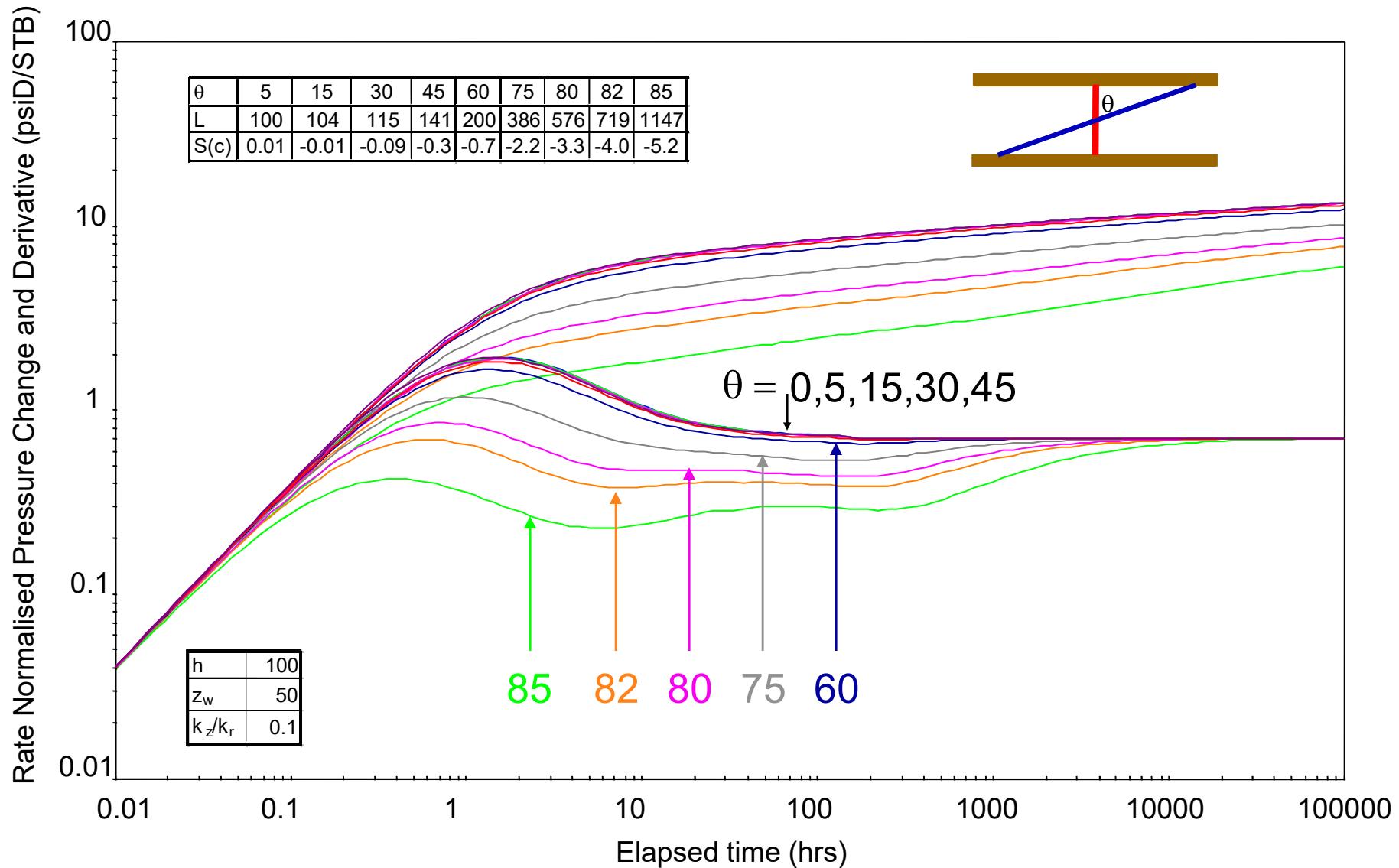




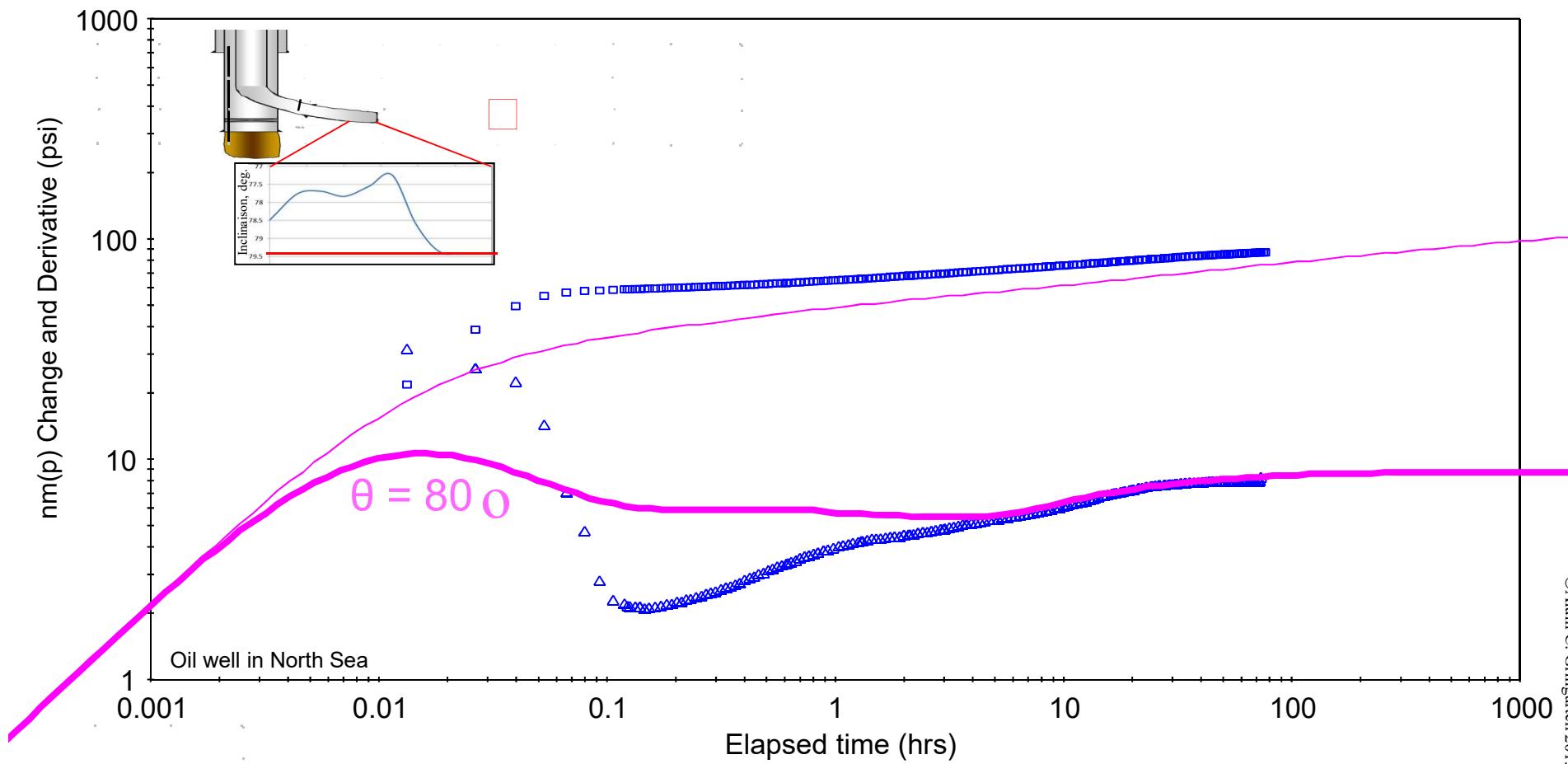
# Analysis of test on Well H



# INCLINED WELL



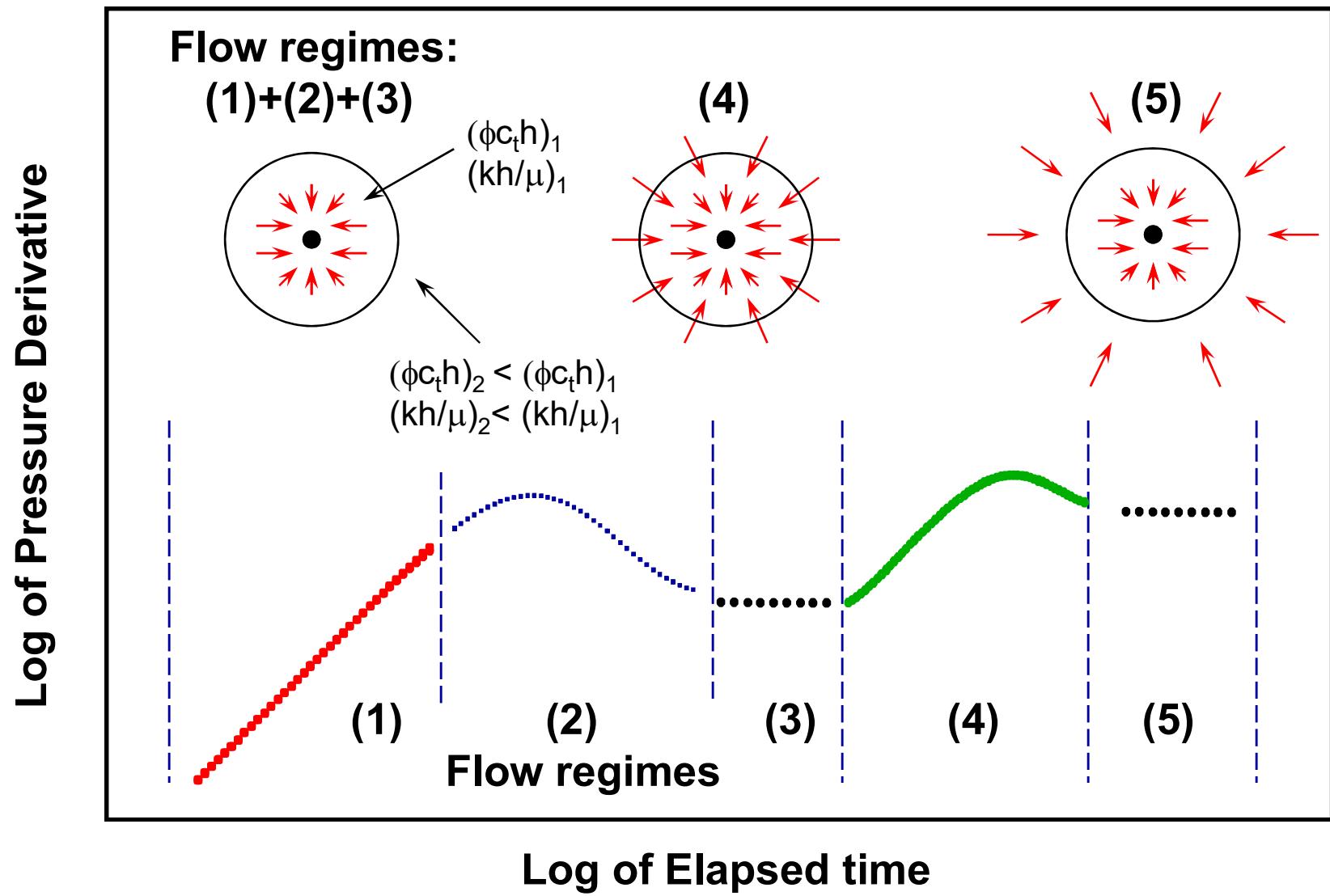
## **80° well**



# WELL TEST INTERPRETATION MODELS

NEAR WELLBORE EFFECTS	RESERVOIR BEHAVIOUR	BOUNDARY EFFECTS
<p>Wellbore Storage</p> <p>Skin</p> <p>Fracture</p> <p>Partial Penetration</p> <p>Horizontal Well</p>	<p>Homogeneous</p> <p>Heterogeneous</p> <ul style="list-style-type: none"><li>- 2-Porosity</li><li>- 2-Permeability</li><li>- Composite</li></ul>	<p>Infinite extent</p> <p>Specified Rate</p> <p>Specified Pressure</p> <p>Leaky Boundary</p>
EARLY TIMES	MIDDLE TIMES	LATE TIMES

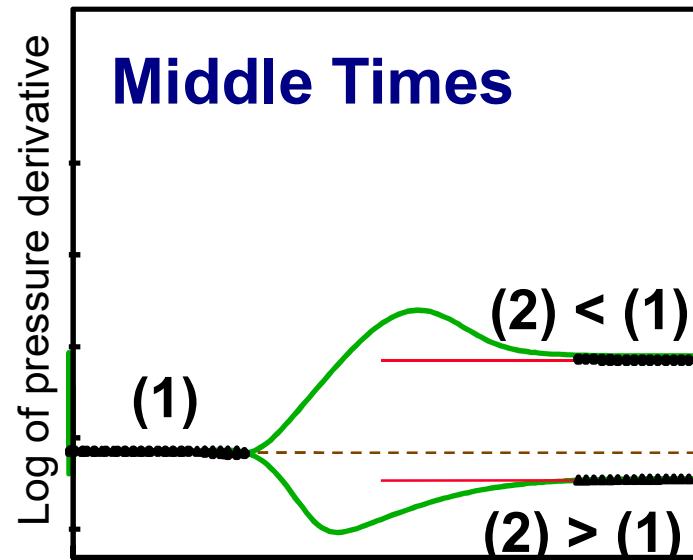
# Well with wellbore storage and skin in an infinite reservoir with composite behaviour



# DERIVATIVE FOR HETEROGENEOUS BEHAVIOUR (Middle Times)

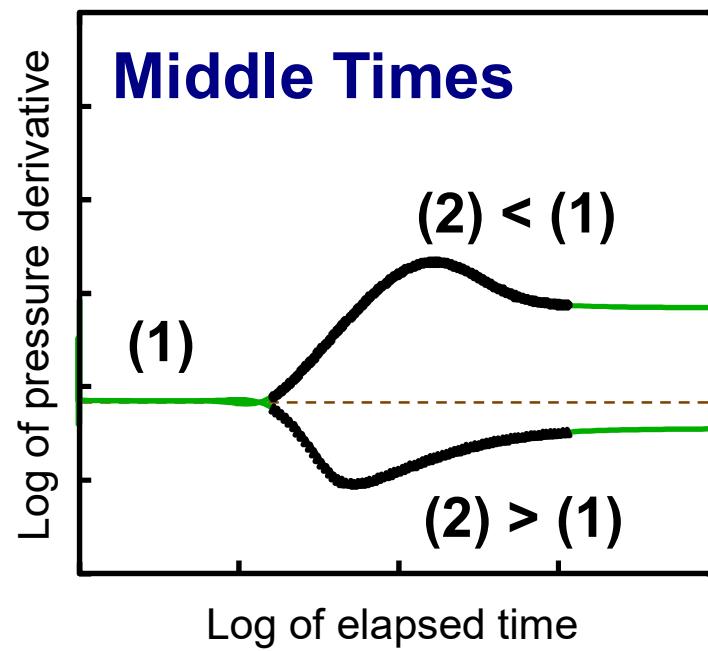
**Mobility change**

$$\left( \frac{kh}{\mu} \right)_1 \rightarrow \left( \frac{kh}{\mu} \right)_2$$

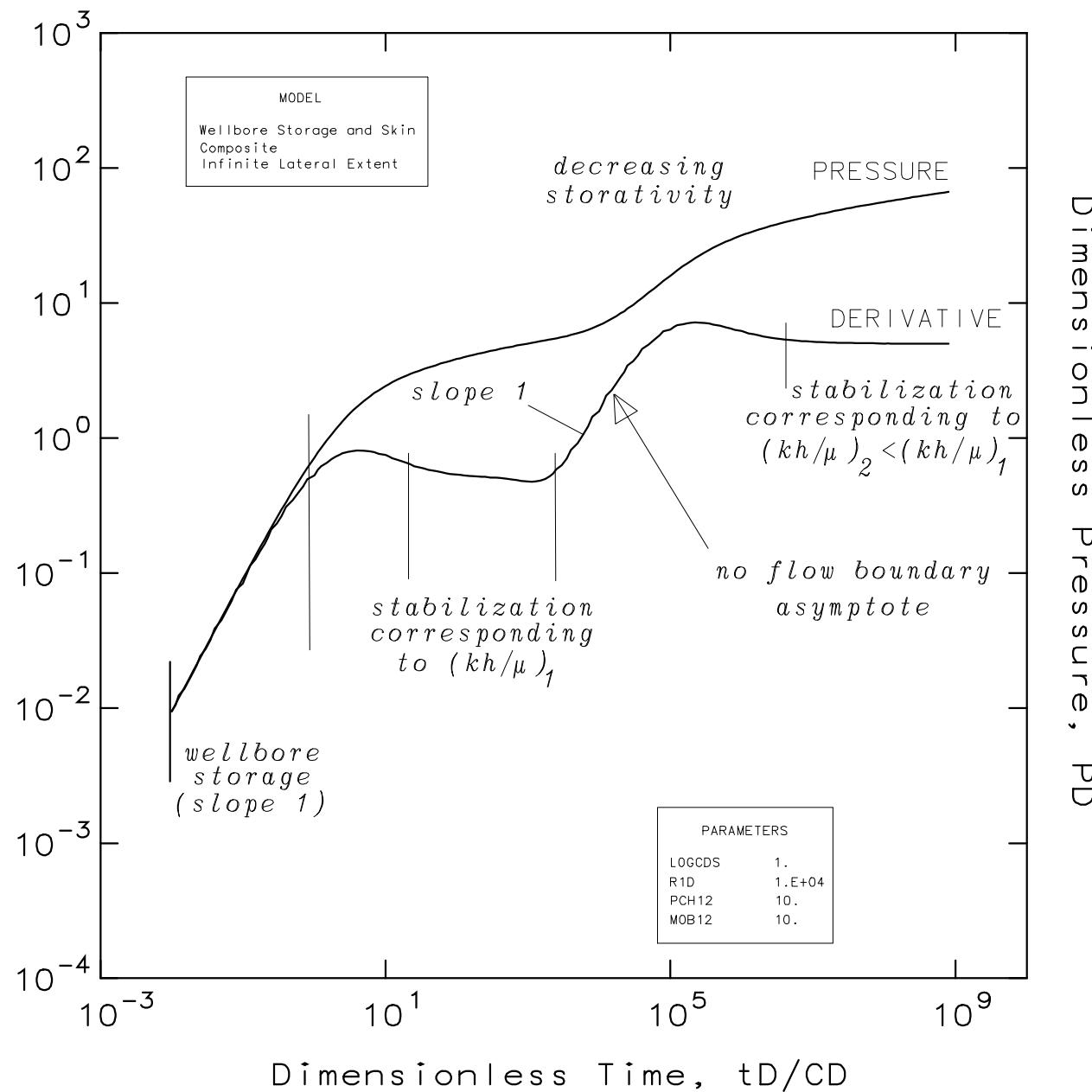


**Storativity change**

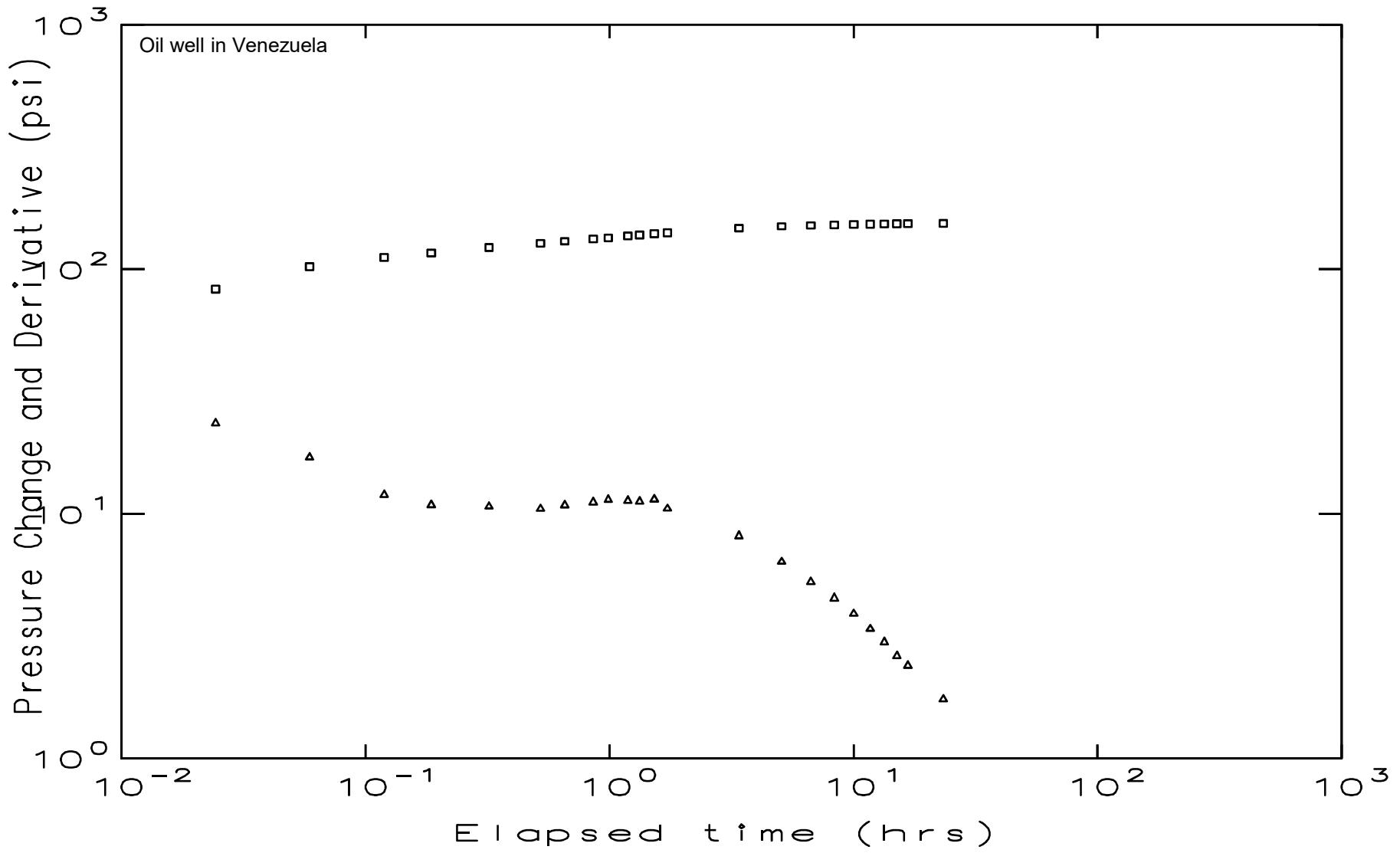
$$(\phi c_t h)_1 \rightarrow (\phi c_t h)_2$$



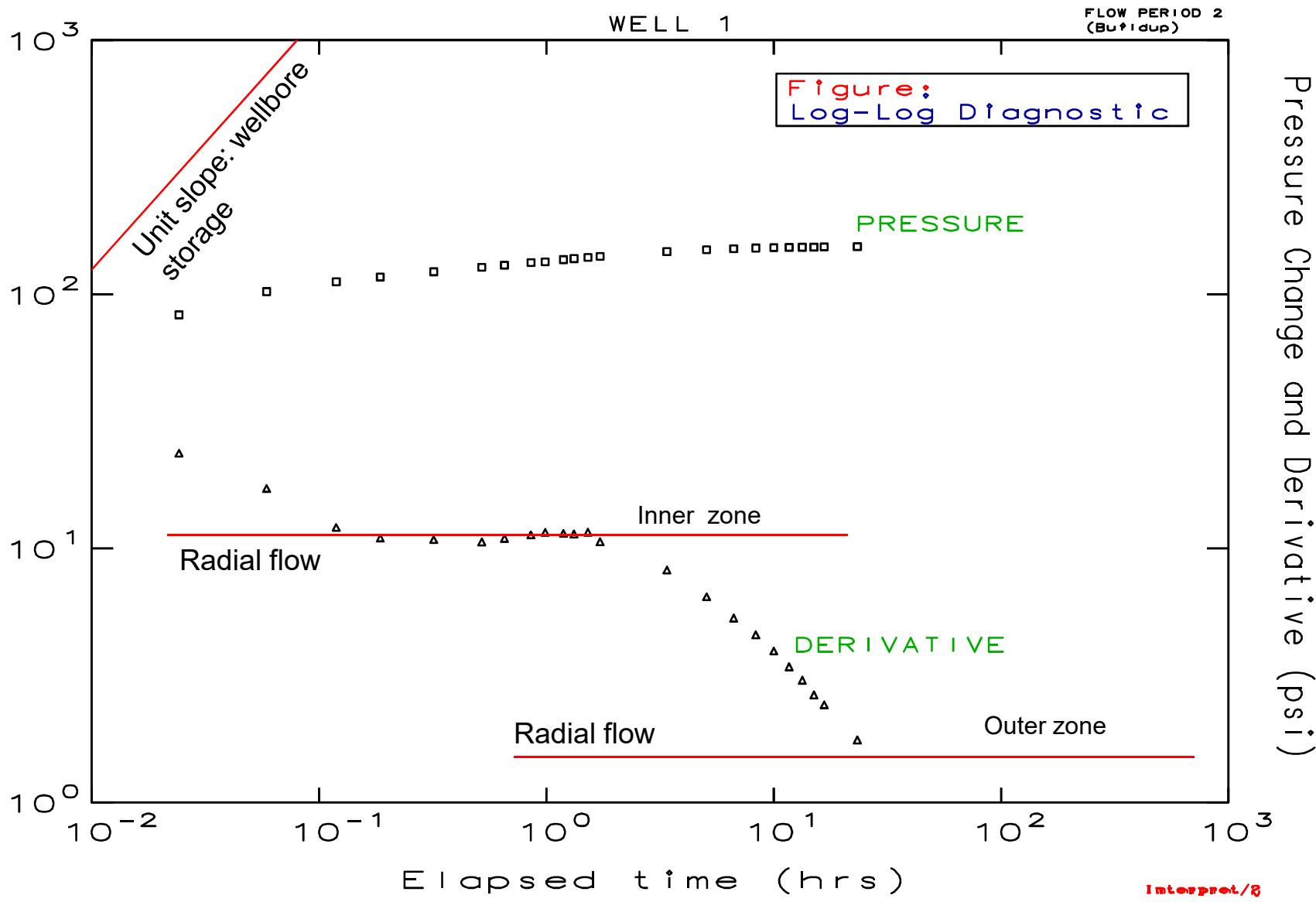
# COMPOSITE BEHAVIOUR



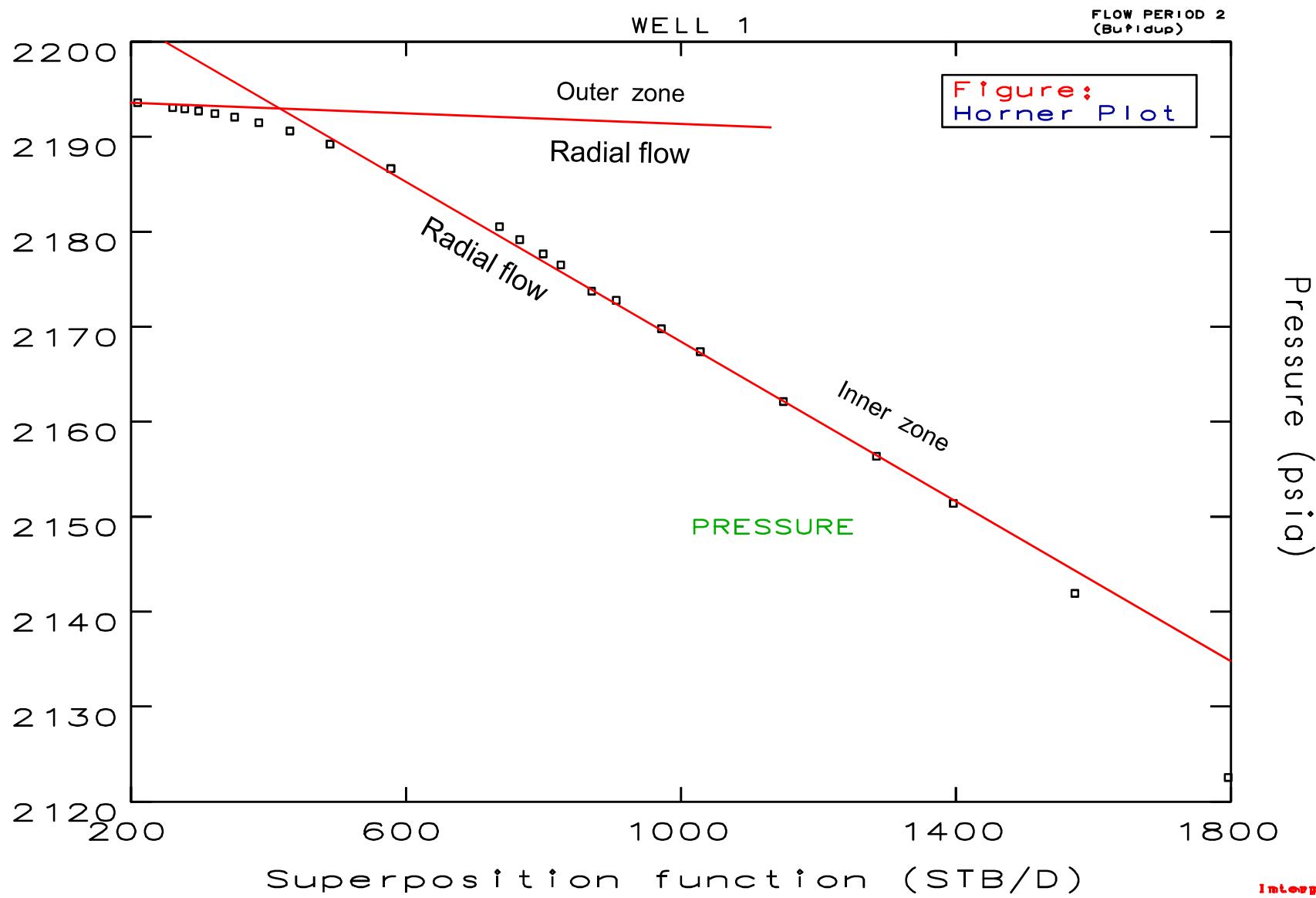
# COMPOSITE BEHAVIOUR



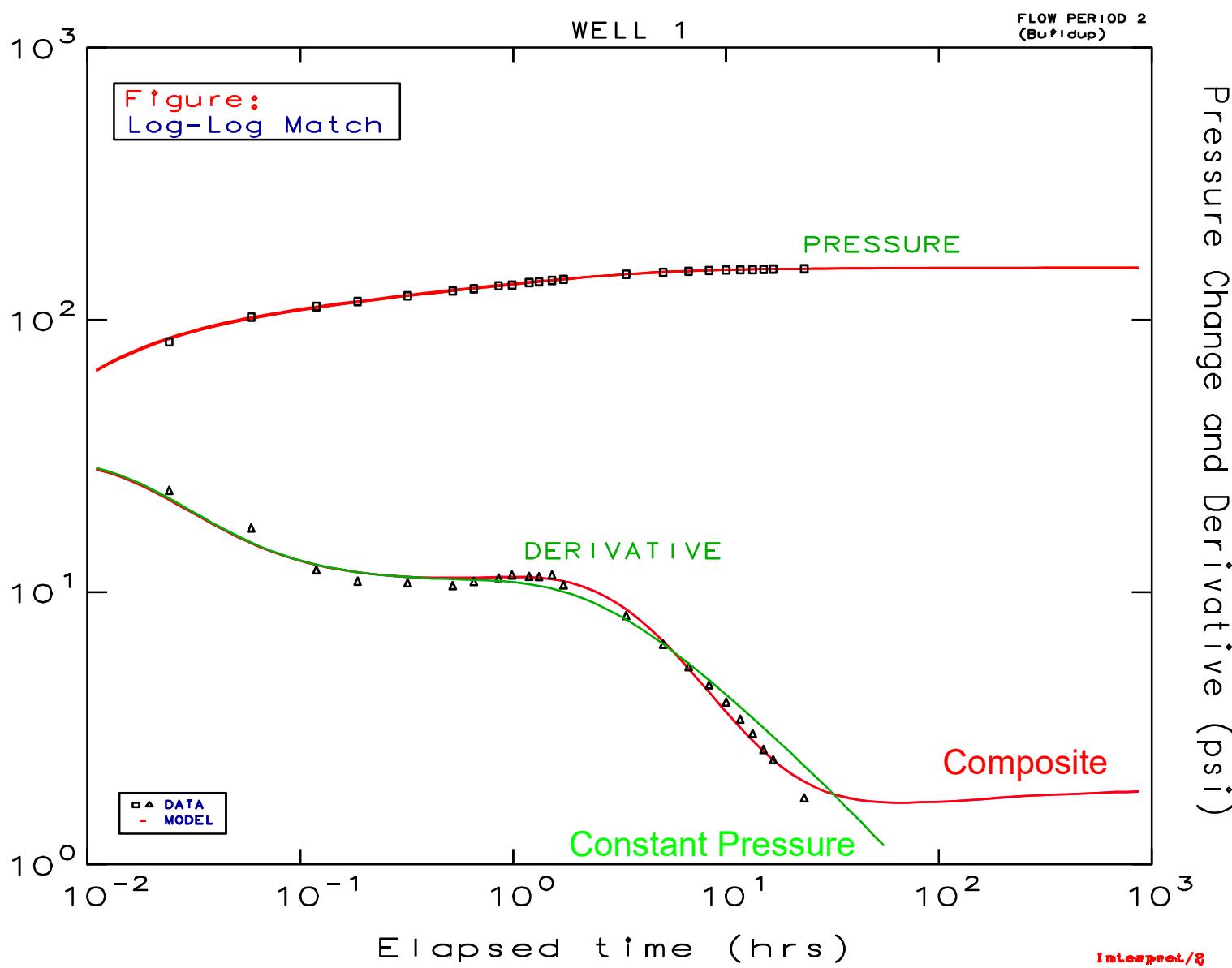
# COMPOSITE BEHAVIOUR



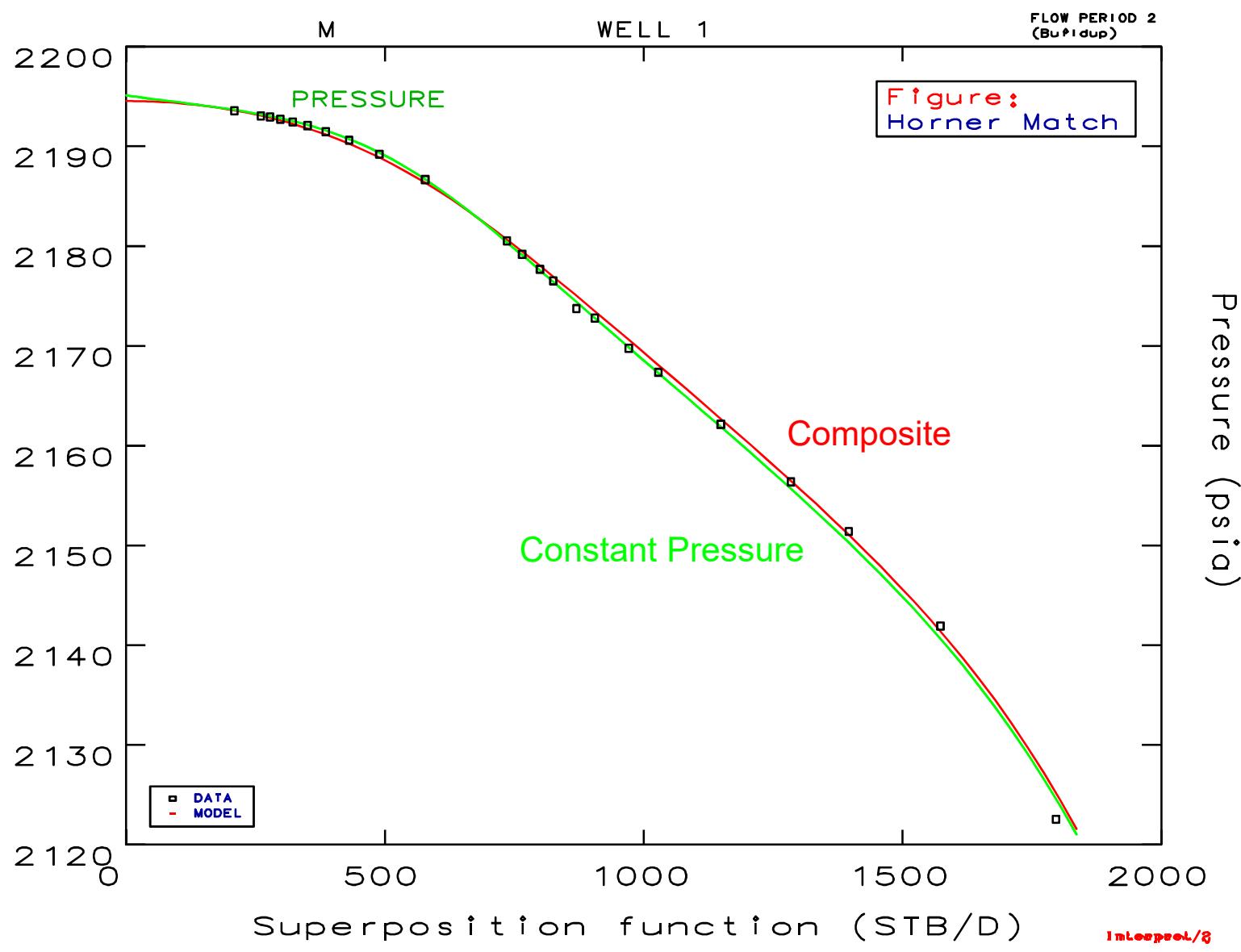
# COMPOSITE BEHAVIOUR



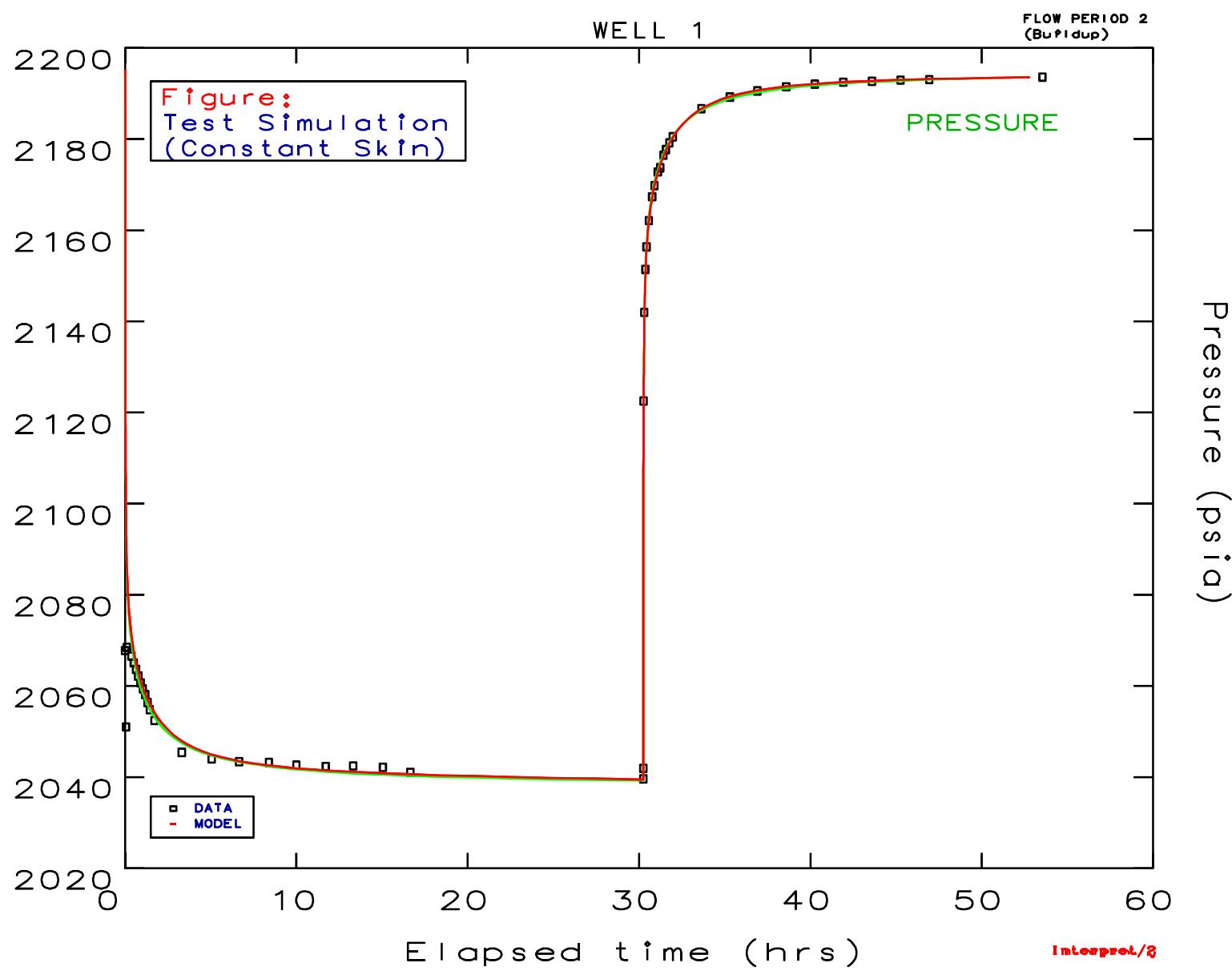
# COMPOSITE BEHAVIOUR



# COMPOSITE BEHAVIOUR

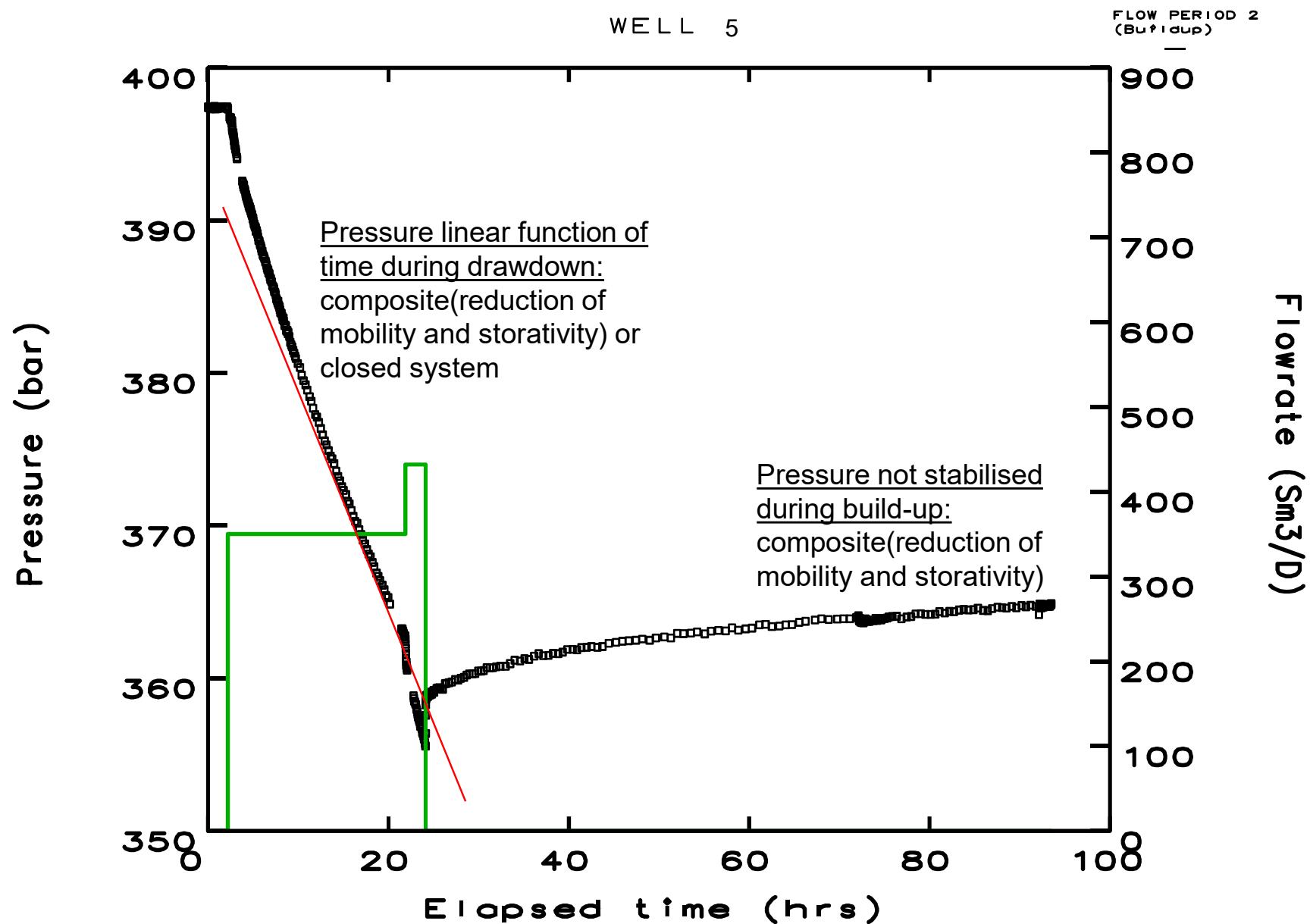


# COMPOSITE BEHAVIOUR



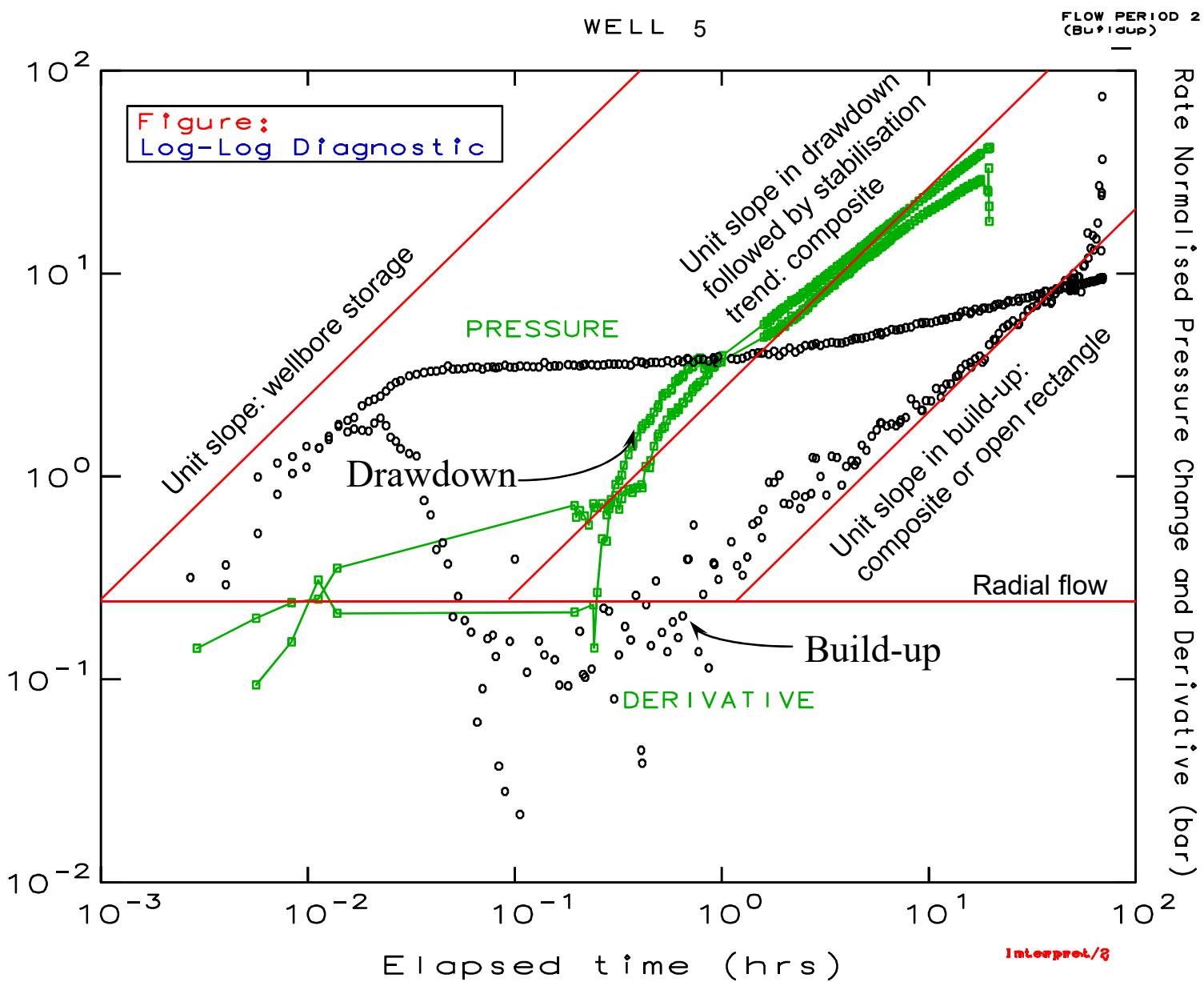
# COMPOSITE BEHAVIOUR

## Water well in Croatia



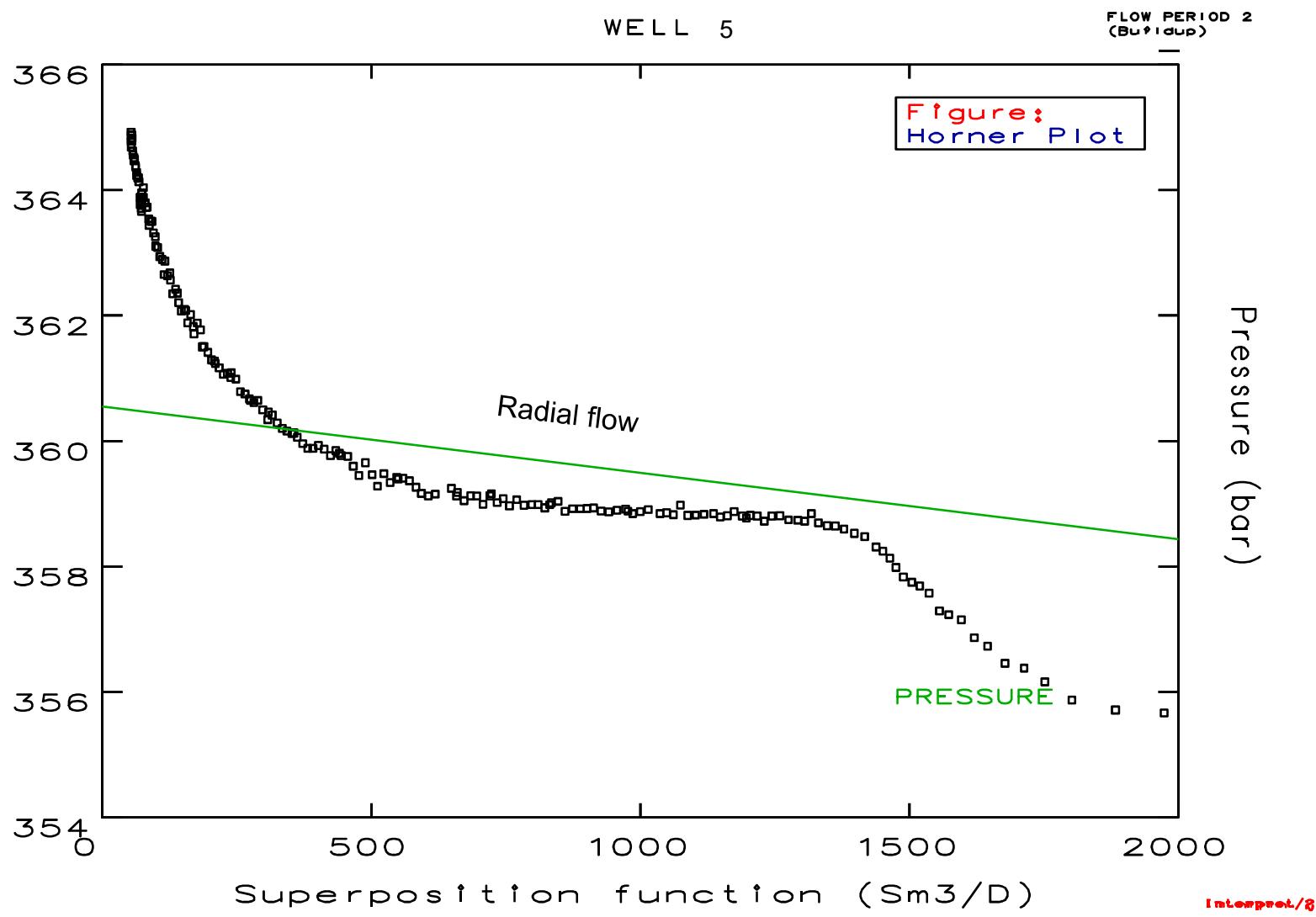
# COMPOSITE BEHAVIOUR

## Water well in Croatia



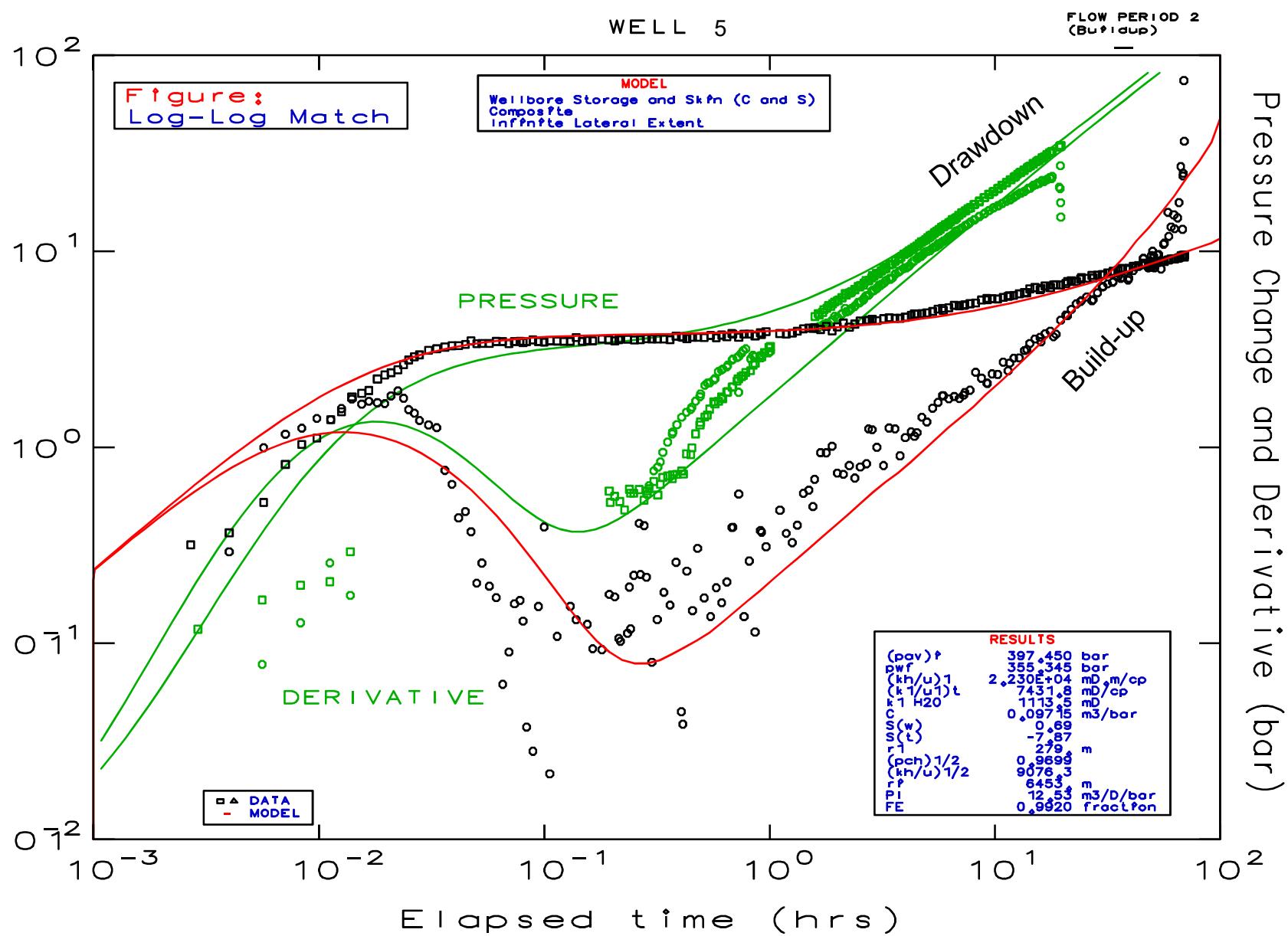
# COMPOSITE BEHAVIOUR

## Water well in Croatia



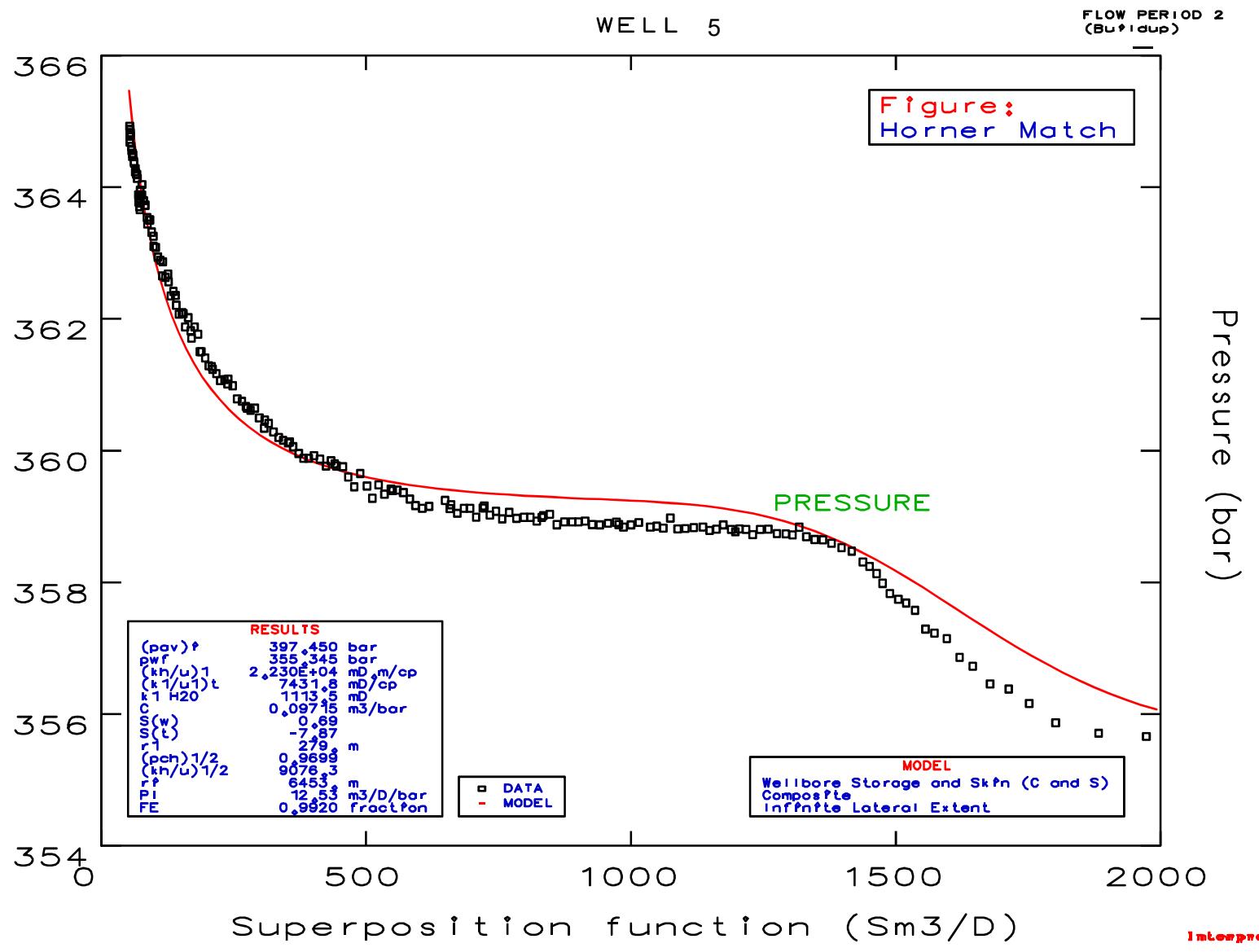
# COMPOSITE BEHAVIOUR

## Water well in Croatia



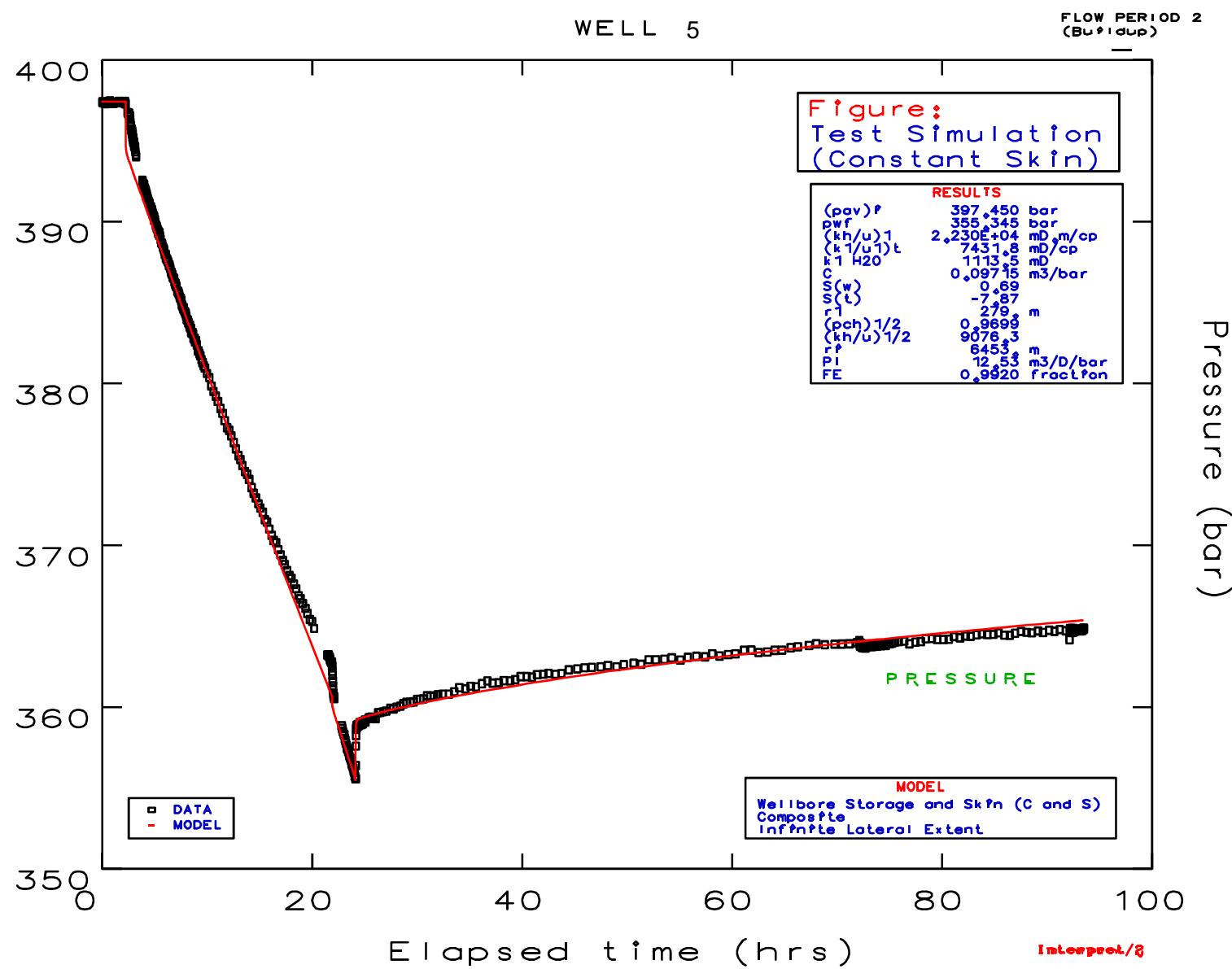
# COMPOSITE BEHAVIOUR

## Water well in Croatia



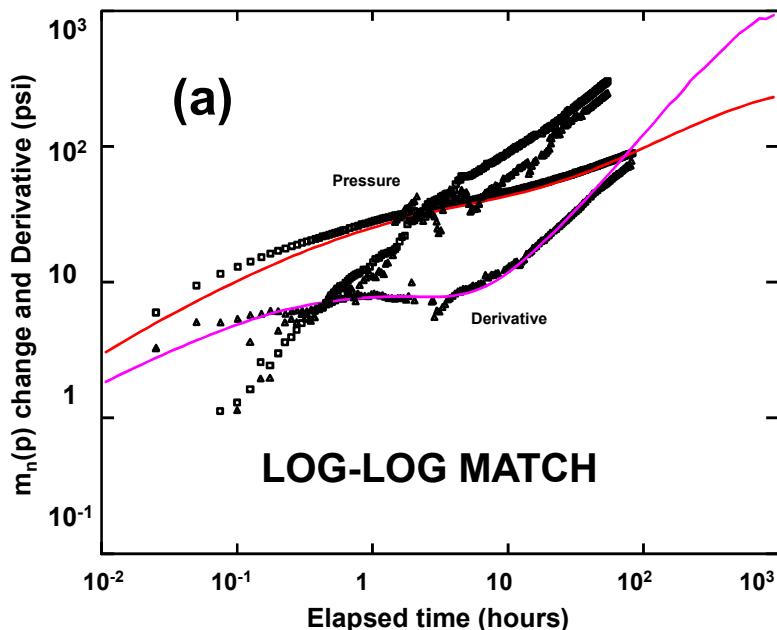
# COMPOSITE BEHAVIOUR

## Water well in Croatia



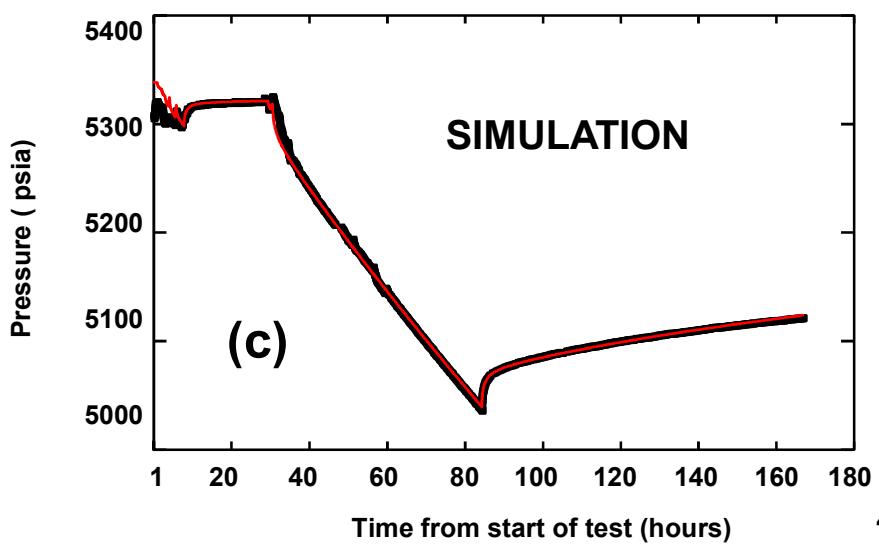
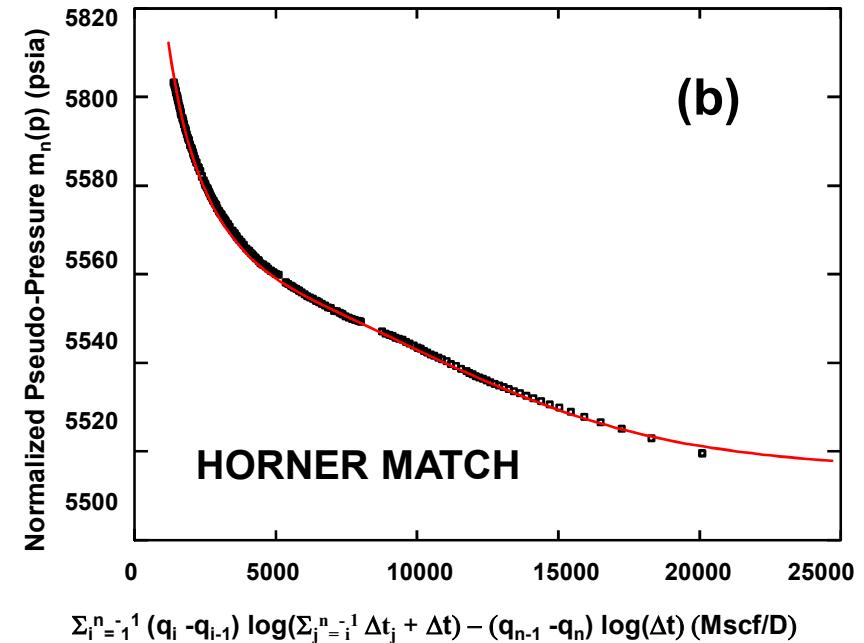
# COMPOSITE BEHAVIOUR

## Gas well off-shore Louisiana

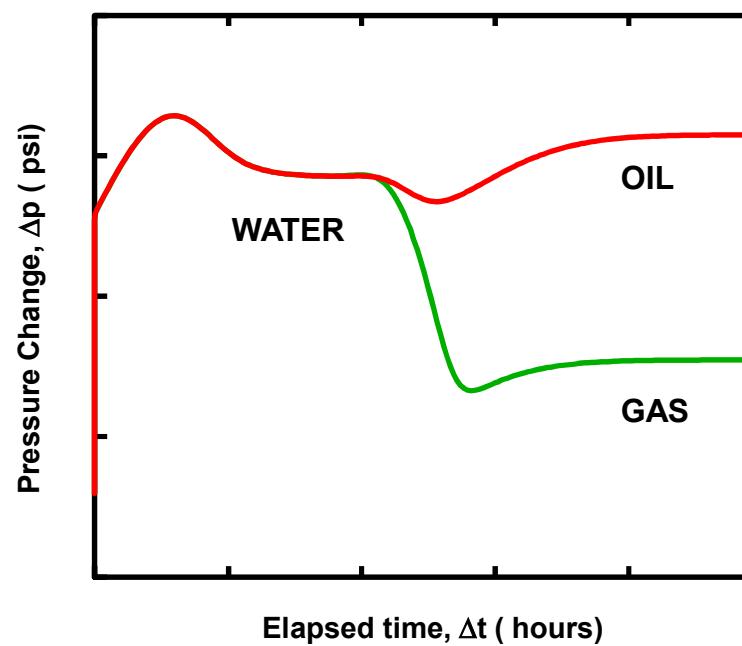
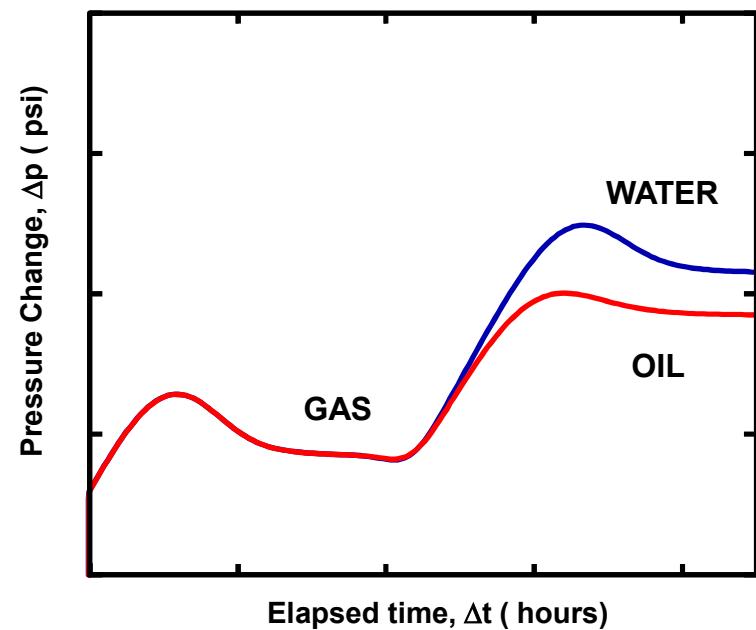
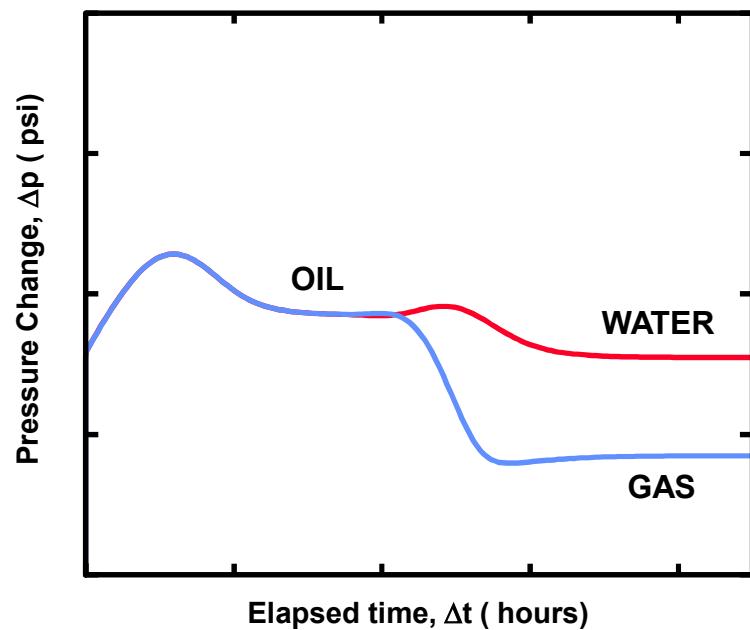


Type Curve   

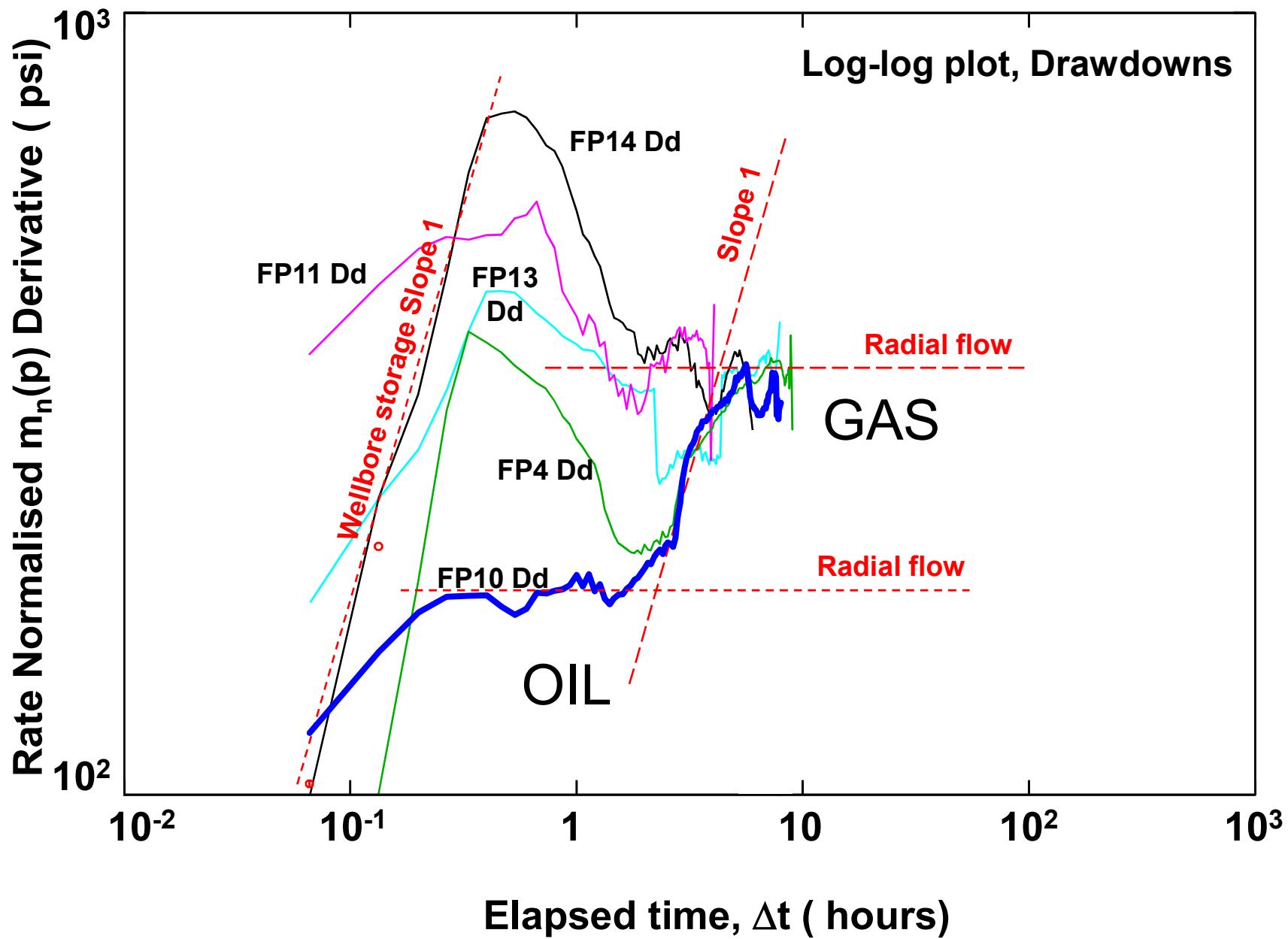
Data   



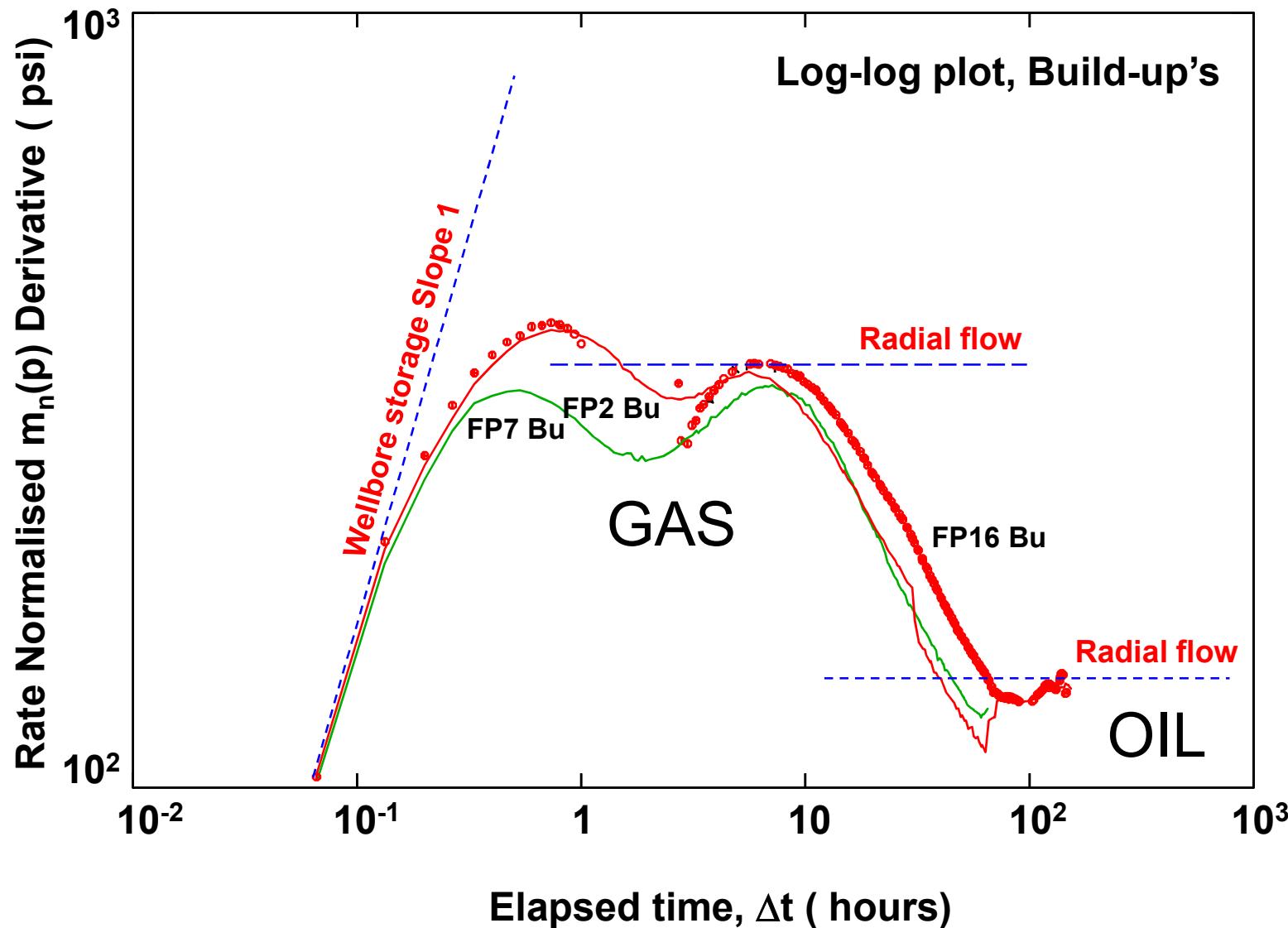
# COMPOSITE BEHAVIOUR DUE TO FLUIDS



# VOLATILE OIL WELL IN RUSSIA



## VOLATILE OIL WELL



# VOLATILE OIL WELL

